
METHODS
OF PHYSICAL EXPERIMENT

THz Wiggler Applied for Measurements of Electron Bunch Longitudinal Structure in FEL¹

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Abstract—The infrared undulator manufactured at JINR and installed at FLASH in 2007 is used for longitudinal bunch shape measurements in the range of several tenths of a micrometer. The presented electromagnetic wiggler is intended for generating a narrow-band THz radiation to measure the longitudinal electron bunch structure in FELs with an electron energy of several tens of MeV. This is a planar electromagnetic device with six regular periods, each 30 cm long. The K parameter is varied in the range 0.5–7.12 corresponding to the range $B = 0.025$ – 0.356 T of the peak field on the axis. The wiggler is simulated for 19.8 MeV/c corresponding to the possible FEL option at PITZ. The wavelength range is 126 μm – 5.1 mm for this electron beam momentum. The 3D Opera simulations of the THz wiggler are discussed. A new PITZ photocathode laser system is proposed for the optimized performance of the high-brightness electron beam. The main goal is a production of 3D ellipsoidal electron bunches with homogeneous charge density. The electromagnetic wiggler is supposed to be used for measuring the longitudinal shape of these electron bunches.

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JINR FAR INFRARED UNDULATOR AT FLASH

The FLASH was equipped with an infrared electromagnetic undulator, tunable over a K -parameter range from 11 to 44, and capable of produces radiation up to 200 μm at 500 MeV and up to 50 μm at 1 GeV [1–5]. The undulator is used for longitudinal electron bunch measurements. It was designed and constructed at JINR according to the FLASH requirements. The undulator period is 40 cm, the number of periods is nine, and the magnetic field is varied in a range of 0.1–1.1 T. The output undulator radiation has following parameters: the wavelength in the range of 5–200 μm , the peak power of ~ 4 MW, the micropulse energy of 1 mJ, and the micropulse duration of 0.5–6 ps.

The energy radiated by the FIR undulator is determined by the number of electrons per bunch N and the form-factor of an electron bunch $F(\lambda)$:

$$\varepsilon_{\text{coh}} = \varepsilon_e \times \left[N + N(N-1) |F(\lambda)|^2 \right],$$

where ε_e is the energy radiated by a single electron. The form-factor is determined by the temporal profile of the electron beam and, e.g., for Gaussian bunches with the r.m.s. length σ it yields $|F(\lambda)|^2 = \exp(-2\pi\sigma/\lambda)^2$. When the wavelength is larger than the bunch length, the coherent radiation dominates. In this case measuring the spectrum can yield the form-factor and thus the charge distribution and the bunch

leading spike length. The Gaussian fit (Fig. 1) corresponds to the r.m.s. leading spike length of $\sigma_{\text{ls}} = 12$ μm . The r.m.s. duration of pulse radiation is $\tau_{\text{FIR}} = \sigma_{\text{ls}}/c = 40$ fs.

3D ELLIPSOIDAL ELECTRON BUNCH

A new photocathode laser system [6–8] is proposed for the high-brightness electron beam. The main goal is a production of 3D ellipsoidal electron bunches with charge density close to the homogeneous one. This corresponds to an almost linear space charge forces within the bunch and therefore to the minimi-

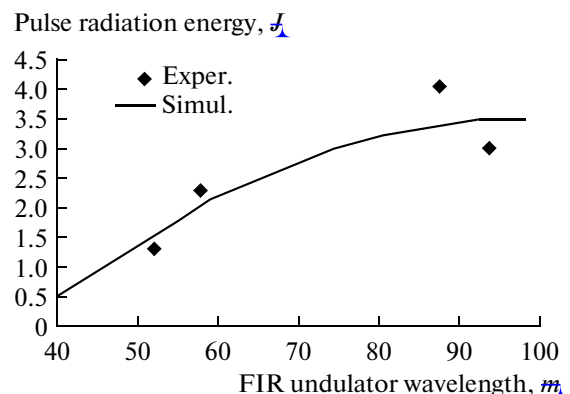


Fig. 1. Dependence of the FIR undulator pulse radiation energy on the wavelength.

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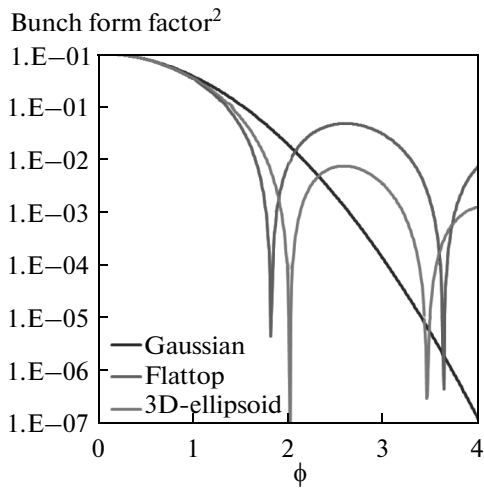


Fig. 2. Dependence of the squared form factor for the Gaussian (blue), flattop (red) and ellipsoidal (green) beams on $\varphi = \omega\sigma_z/c$.

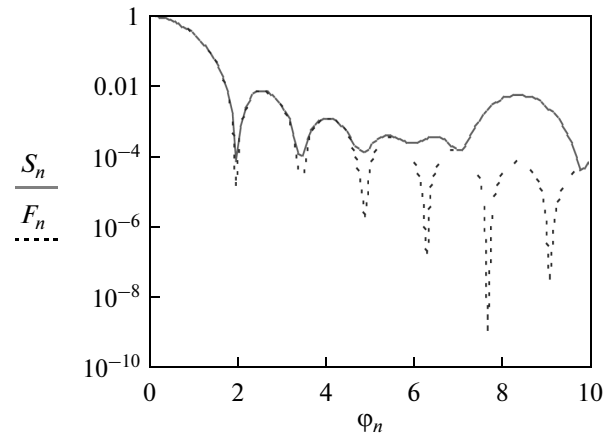


Fig. 3. Dependence of the squared form factor of the ellipsoidal bunch with an ideal 3D ellipsoidal shape (dashed line) and with border imperfection (solid line at $\delta = 0.1$ and $m = 3$) on $\varphi = \omega\sigma_z/c$.

zation of the space charge contribution to the overall beam emittance budget.

Beam dynamics simulations demonstrated a significant reduction in the transverse emittance of electron bunches produced by applying 3D ellipsoidal laser pulses to the rf photo gun [9]. Such a system capable of producing 3D quasi-ellipsoidal pulses is under development at the IAP RAS, Nizhny Novgorod, Russia. The Photo Injector Test facility at DESY, Zeuthen site (PITZ) develops high-brightness electron sources for modern Free Electron Lasers, like FLASH and the European XFEL. The photocathode laser system is one of the key issues for the photo injector optimization. Currently, the PITZ photocathode laser can generate cylindrical pulses with flattop temporal profiles. Tests of the new photocathode laser system with 3D shaped pulses are considered to be the next step in the high-brightness electron source optimization. The laser system developed at IAP RAS is intended to be installed at the PITZ accelerator for experimental tests with electron beam production. The electron bunches with mean momentum of up to 19.8 MeV/c and r.m.s. pulse duration of ~ 7.2 ps are expected in the PITZ accelerator with the new laser system. Installation of a magnetic chicane in PITZ permits the r.m.s. electron bunch duration reduced down to ~ 0.66 ps, which corresponds to the bunch length of 200 μm . Below we assume that the electron bunches will be compressed in the PITZ magnetic chicane.

The wiggler [10, 11] is proposed for measuring the longitudinal shape of the 3D ellipsoidal electron bunch. As it was done at FLASH, we plan to estimate the form factor of a 3D ellipsoidal electron bunch on the basis of the radiation energy measurements. For small angles, typical of radiation of PITZ relativistic electrons, transverse effects are strongly suppressed. For the 3D ellipsoidal bunch shape $(x^2 + y^2)/5\sigma_x^2 +$

$(ct)^2/5\sigma_z^2 \leq 1$, $S(x, y, t) = 1/(4\pi \times 5^{3/2}\sigma_x^2\sigma_z^2)$ the form factor is defined by the relation $F(\omega) = \int dx dy \int S(x, y, t) \exp(i\omega t) dt$. After the integration one obtains $F(\omega) = 3/(5\varphi^2) \{ \sin(5^{1/2}\varphi)/(5^{1/2}\varphi) - \cos(5^{1/2}\varphi) \}$, where $\varphi = \omega\sigma_z/c$. As it was mentioned above, the form factor of the Gaussian beam is $F(\varphi) = \exp(-\varphi^2/2)$. The dependences of the squared form factor $F(\varphi)^2$ on φ are shown in Fig. 2 compared to the Gaussian and flattop cases. Though dependencies for flattop and 3D ellipsoidal bunches show qualitatively similar behavior, they differ significantly from the Gaussian case.

The first experimental tests with the new photocathode laser system [6, 7] showed deviation of the generated laser pulses from the ideal 3D ellipsoidal shape. Finite border sharpness is one of such imperfections. In order to investigate the influence of the finite border sharpness on the electron beam emittance, beam dynamics simulations was performed [9]. Evaluations for the border thickness of 10% yield $\sim 10\%$ emittance growth [9].

The bunch border imperfection [6–8] is approximated by $(x^2 + y^2)/5\sigma_x^2 + (ct)^2/5\sigma_z^2 \leq 1 + \delta \sin(2\pi m ct/5^{1/2}\sigma_z)$, where $\delta \cong 0.1$ is the amplitude of the border oscillations, $m = 2$ or $m = 3$ is harmonic number. The square of form factor is equal to $F(\psi)^2 = \{ 3/(\psi^2) (\sin(\psi)/\psi - \cos(\psi)) \}^2 + \{ 9\pi^2 \delta^2 m^2 \sin^2(\psi) \} / \{ \psi^2 - (2\pi m)^2 \}^2$ at bunch border imperfection, where $\psi = 5^{1/2}\varphi$. The bunch border imperfection leads to large modification of square of the form factor at high $\varphi \cong 2\pi m/5^{1/2} \cong 8.5$ and $m = 3$ (Fig. 3). The square of the form factor is proportional to $F^2 \sim \delta^2$ at this φ .

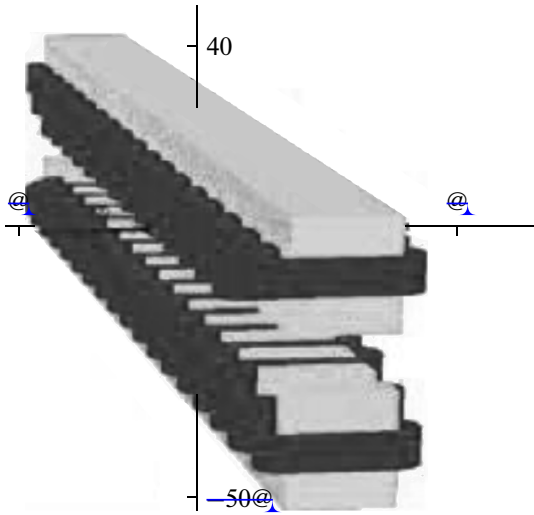


Fig. 4. TOSCA 3D simulation of the THz wiggler.

The square of form factor and the longitudinal length of a 3D elliptical bunch can be found from the energy radiation measurements with different wave-

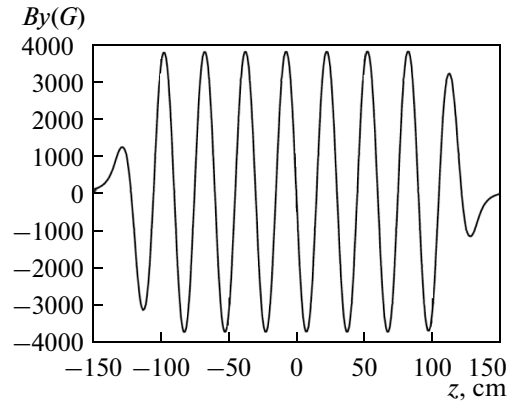


Fig. 5. Dependence of the wiggler magnetic field on the longitudinal coordinate.

lengths [3–5]. To obtain the bunch length and extract the imperfection of the ellipsoidal bunch shape, the phase range should be about $10 > \varphi > 0.32$, where $F(0.32)^2 = 0.9$. This phase range corresponds to the wavelengths of $124 \mu\text{m} < \lambda < 3.9 \text{ mm}$ for the bunch length of $\sigma_z = 200 \mu\text{m}$ after the compression.

Technical characteristics of the wiggler

Parameter of THz wiggler	value
Period length, mm	300
Number of full periods	7
Number of poles including end-pieces	14 + 4
Maximum wiggler parameter, K_{rms}	7.12
Peak field on axis, T	0.356
Minimum field on axis, T	0.025
Electron momentum, MeV/c	19.8
Maximum wave length, mm	5.1
Minimum wave length, mm	0.12
Clear gap, mm	100
Position accuracy of magnetic axis, mm	0.5
Angular precision of magnetic axis, mrad	0.5
Field flatness at ± 20 mm off-axis (horizontally), %	-0.1...+0.5
First field integral I1, G cm	50
Second field integral I2, G cm ²	500
Stability and reproducibility of magnetic axis, mm/ μrad	$\pm 0.1/\pm 50$

THz WIGGLER FOR BUNCH SHAPE MEASUREMENTS

The design of the THz wiggler [10, 11] (Fig. 4 and table) is based on the FLASH undulator constructed at JINR [1–5].

As follows from the 3D TOSCA simulations of the magnetic field (Fig. 5), its transverse component is smaller than -0.1% at the aperture of 20 mm (Fig. 6).

The first wiggler peculiarity is related to a large clear gap between its main coils. The diffraction spot size of the radiation determines the diameter of the vacuum chamber and the wiggler gap. The diffraction angle and the spot radius of wiggler radiation are $\theta_d \cong (\lambda/2L)^{0.5}$ and $r_d \cong (\lambda L/2)^{0.5}/\pi$ respectively, where $L = 2.1$ m is the wiggler length and λ is the wavelength. The diffraction parameters θ_d/r_d are 29 mrad/2.1 cm at the wavelength of 3.9 mm.

The angle spread of the photon radiation $r = L\theta/6$ gives the same input in transverse size at the wiggler exit, where $\theta = K_{\text{rms}}/\gamma N_w^{1/2}$, γ is the relativistic factor, and N_w is the number of the wiggler periods. This size is 1.2 cm at the maximum field.

The second peculiarity of the wiggler is related to the trim coils. Four trim coils with individual power supplies should be installed in the wiggler. These trim coils permit the first and the second integrals to be compensated over the full wiggler length. However, it does not permit compensation of the integral over the period length. The first integral over the period length should be smaller than 50 G cm, and the second integral should be as low as 500 G cm². To meet the both

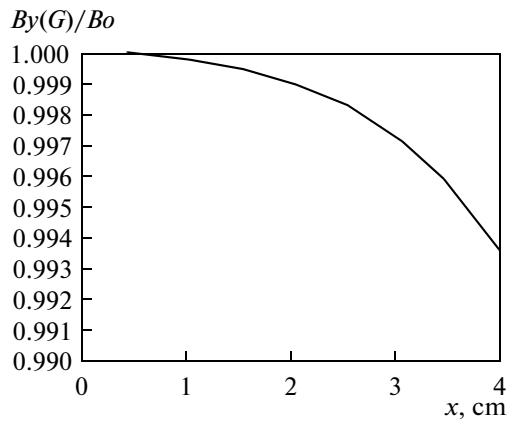


Fig. 6. Dependence of the normalized wiggler magnetic field at $I_w = 21.5$ kA turns on the transverse coordinate.

requirements, it is proposed to install an additional correction coil in each regular coil.

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