

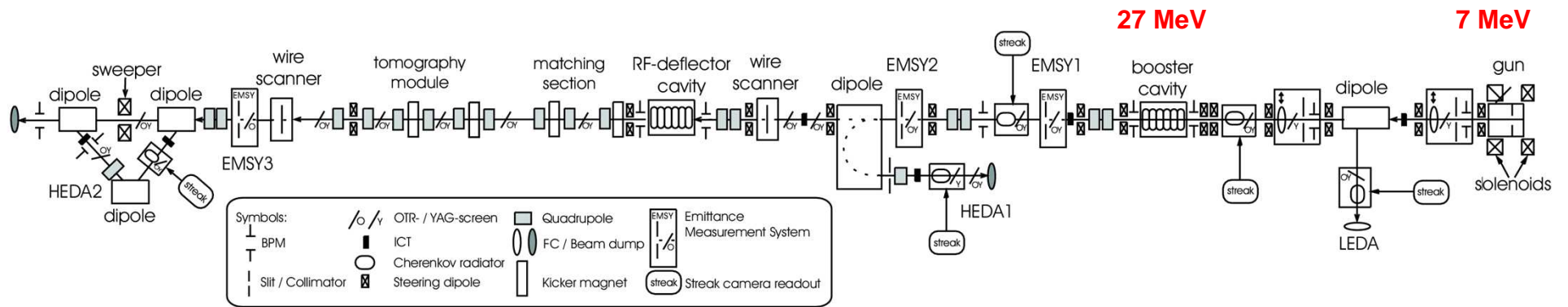
# Simulation of the different type of measurement with the RF deflecting structure at PITZ

1. PITZ2.0 design, new components
2. TDS basic principle, resolution and limitation
3. Longitudinal phase space measurement
4. Bunch length measurement
5. Slice emittance measurement
6. Summary

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Forschungsseminar SS 2012  
Humboldt-Universität zu Berlin  
8<sup>th</sup> of June 2012

# PITZ2.0 design

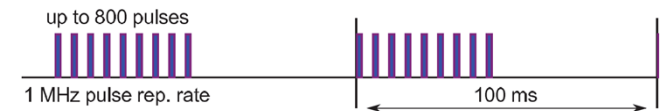


27 MeV

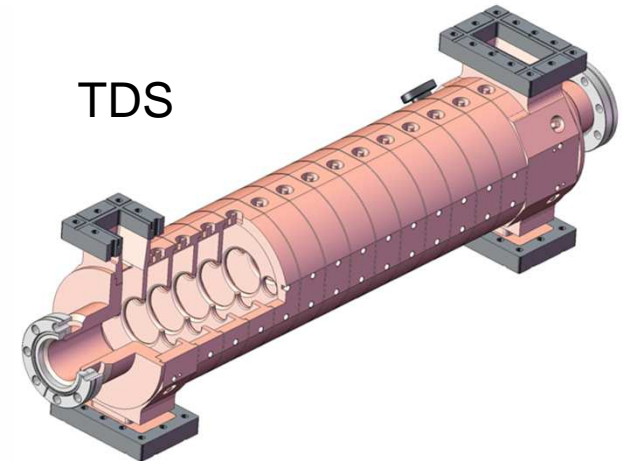
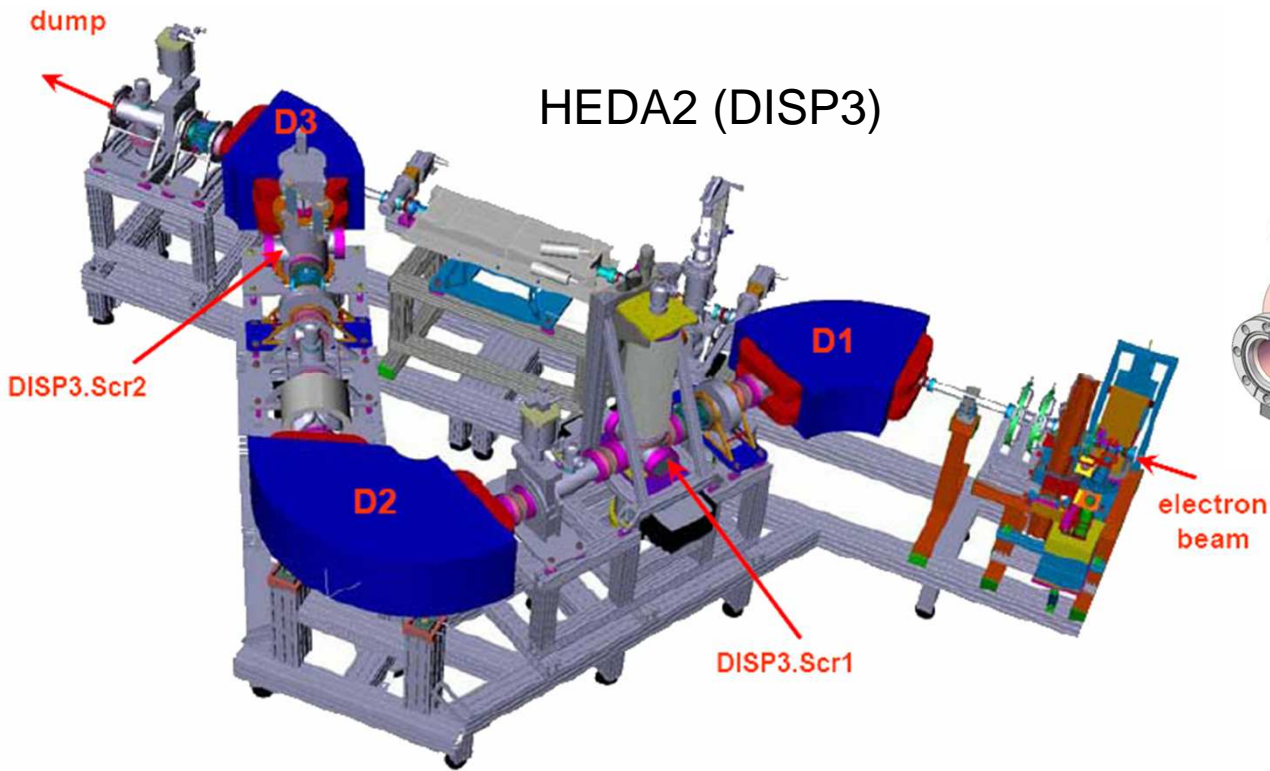
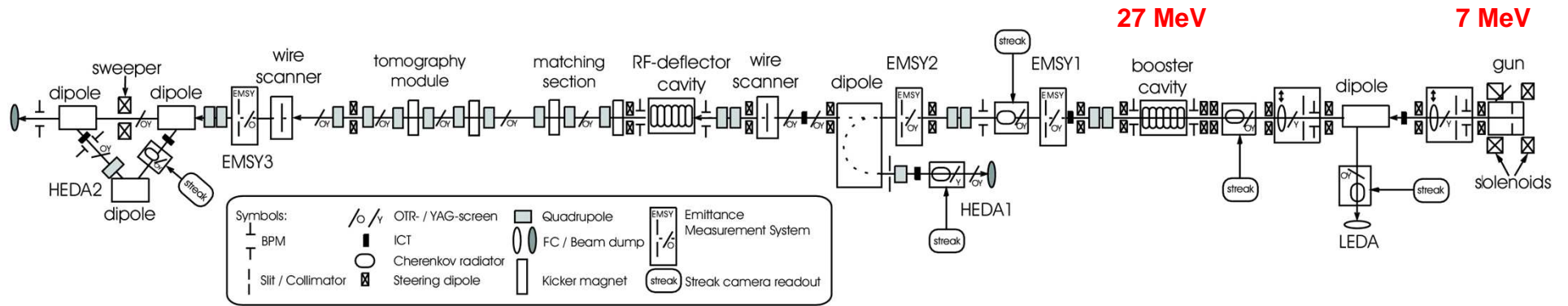
7 MeV

## Main parameters:

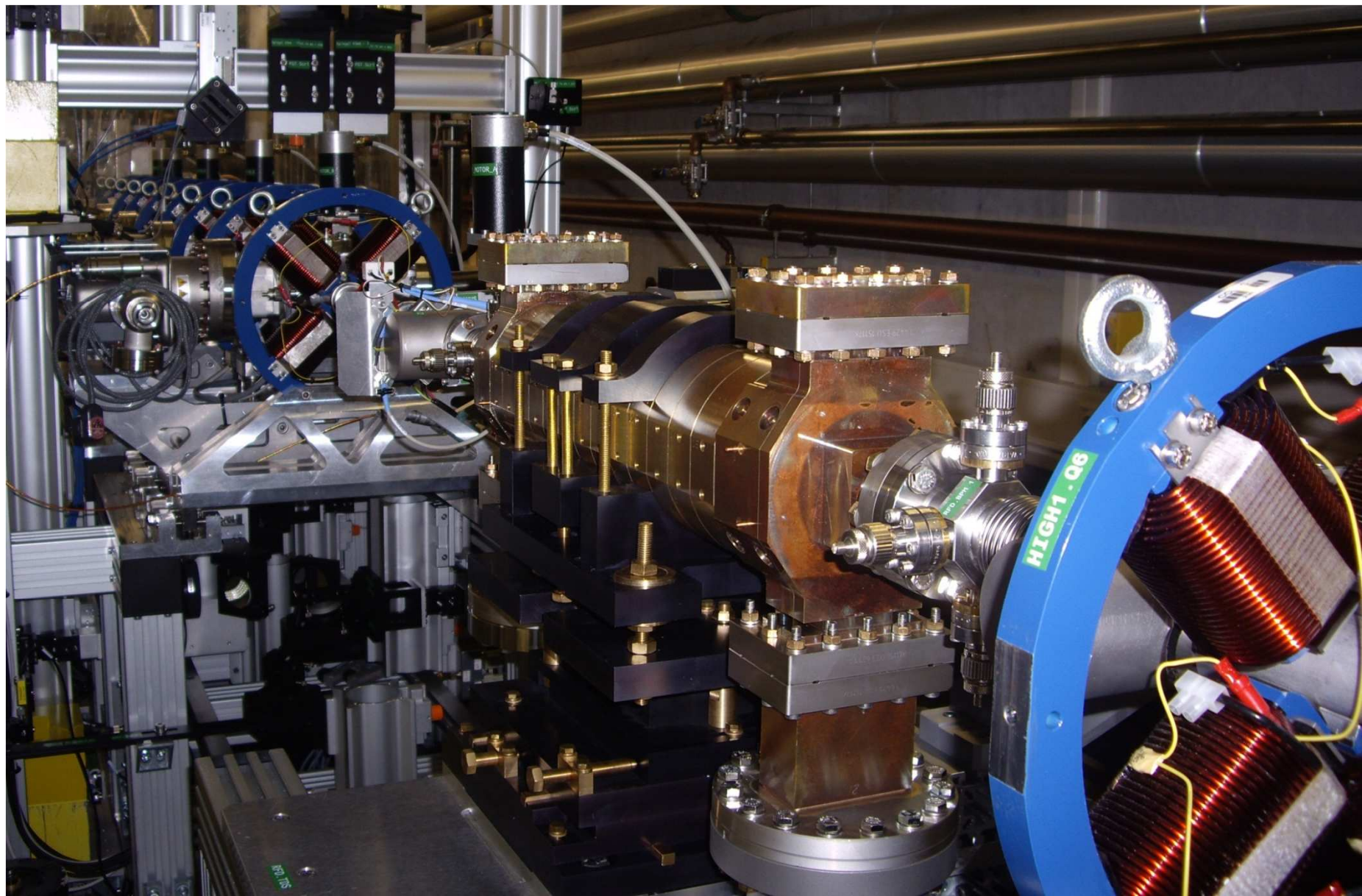
Bunch charge	1 pC ... 2 nC
Repetition rate	10 Hz
Beam energy after gun	1 ... 7 MeV
Beam energy after booster	1 ... 27 MeV
Number of bunches	1 ... 800
Bunch spacing	1 $\mu$ s
Laser pulse temporal shape	2 ps Gauss ... 22 ps flat-top



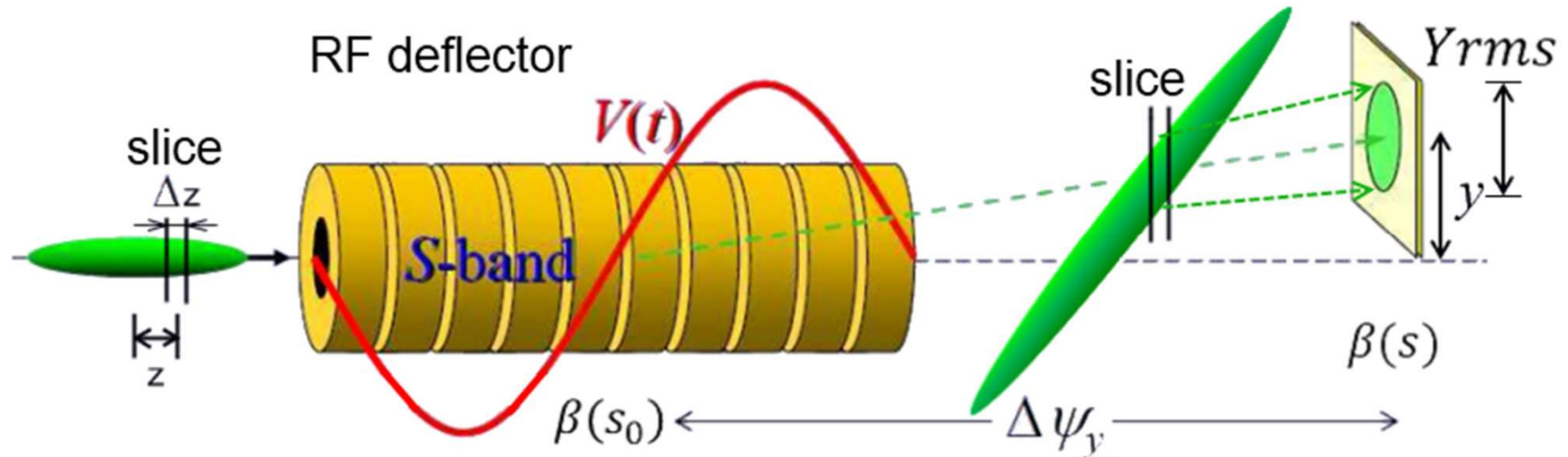
# PITZ2.0 design



# TDS in the PITZ beamline



# TDS basic principles



$$y = \theta \cdot L = \frac{eV_0 k}{pc} \cdot z \cdot L = S \cdot z,$$

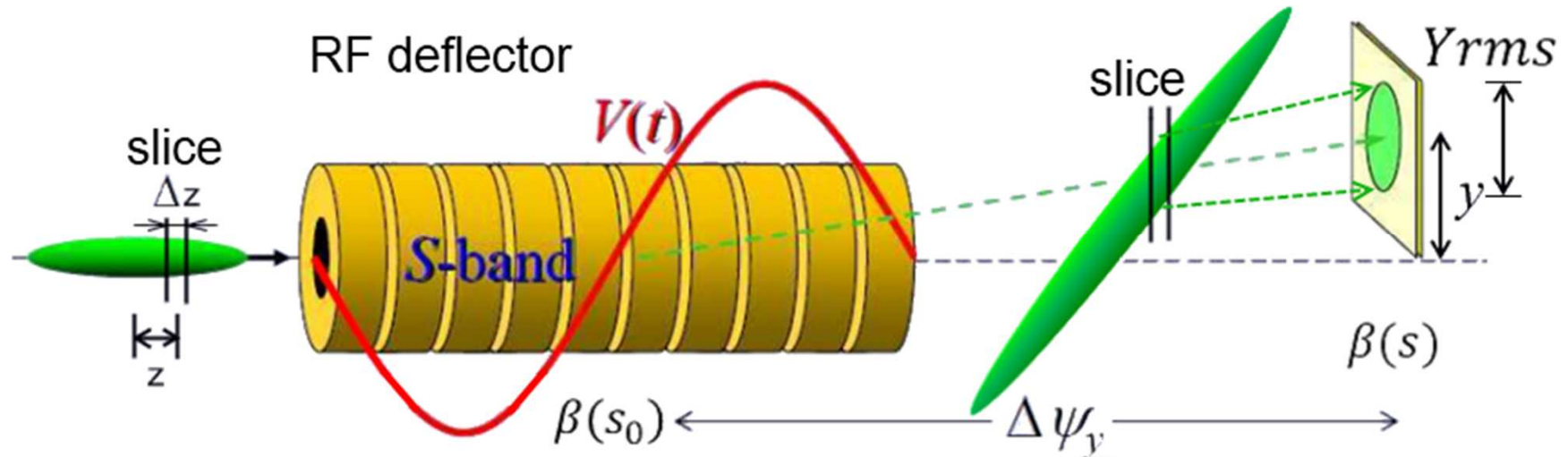
$$S = \frac{eV_0 k}{pc} L, \quad \text{in case of drift space}$$

$$S = \sqrt{\beta(s) \cdot \beta(s_0)} \cdot \sin(\Delta\psi_y) \cdot \frac{eV_0 k}{pc}$$

where  $z$  – slice longitudinal position,  
 $L$  – distance between TDS and screen,  
 $V_0$  – deflecting voltage,  $k$  – wave number,  
 $pc$  – beam momentum,  $S$  – shear parameter,  
 $y$  – slice vertical position at screen

in the general case, where  $\beta(s)$  - beta function at screen,  $\beta(s_0)$  – beta function at TDS position,  $\Delta\psi_y$  - beta function phase advance between TDS and screen.

# TDS Longitudinal resolution



- $\Delta z$  – slice length
- $V(t)$  – deflecting voltage (artistic view)
- $\beta(s_0)$  – beta function inside TDS
- $\beta(s)$  – beta function at screen
- $\Delta\psi_y$  – beta function phase advance
- $Y_{rms}$  – slice vertical RMS size at screen

$$y = S \cdot z; Y_{rms}^2 = \epsilon\beta(s) + (S \cdot \Delta z)^2,$$

$$y \geq Y_{rms},$$

$$S \cdot z \geq \sqrt{\epsilon\beta(s) + (S \cdot \Delta z)^2},$$

for  $\Delta z \rightarrow 0$ , we will get resolution length  $\sigma_z$  as:

$$\sigma_z = \frac{\sqrt{\epsilon\beta(s)}}{S} = \frac{\sqrt{\epsilon_{N,y}/\gamma}}{\sqrt{\beta(s_0)} \cdot \sin(\Delta\psi_y)} \cdot \frac{pc}{eV_0 k}$$



# TDS Longitudinal resolution

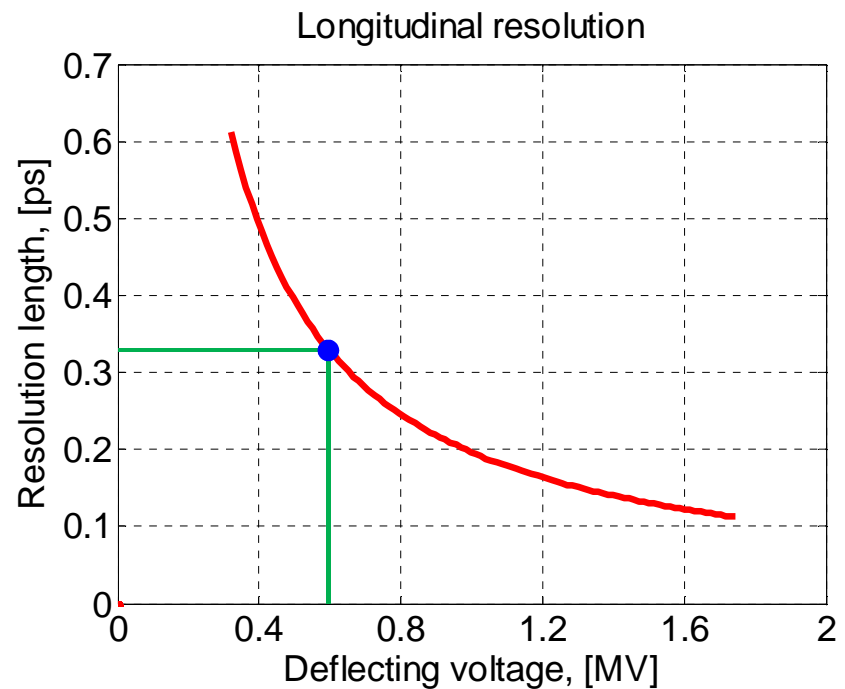
$$\sigma_z = \frac{\sqrt{\varepsilon\beta(s)}}{S} = \frac{\sqrt{\varepsilon_{N,y}/\gamma}}{\sqrt{\beta(s_0)} \cdot \sin(\Delta\psi_y)} \cdot \frac{pc}{eV_0k}$$

For TDS deflecting voltage 0.6MV  
parameter S will be about 3.2, and for  
transverse RMS beam size 0.3 mm at  
screen (TDS OFF), longitudinal resolution  
will be 0.1 mm or 0.3 ps.

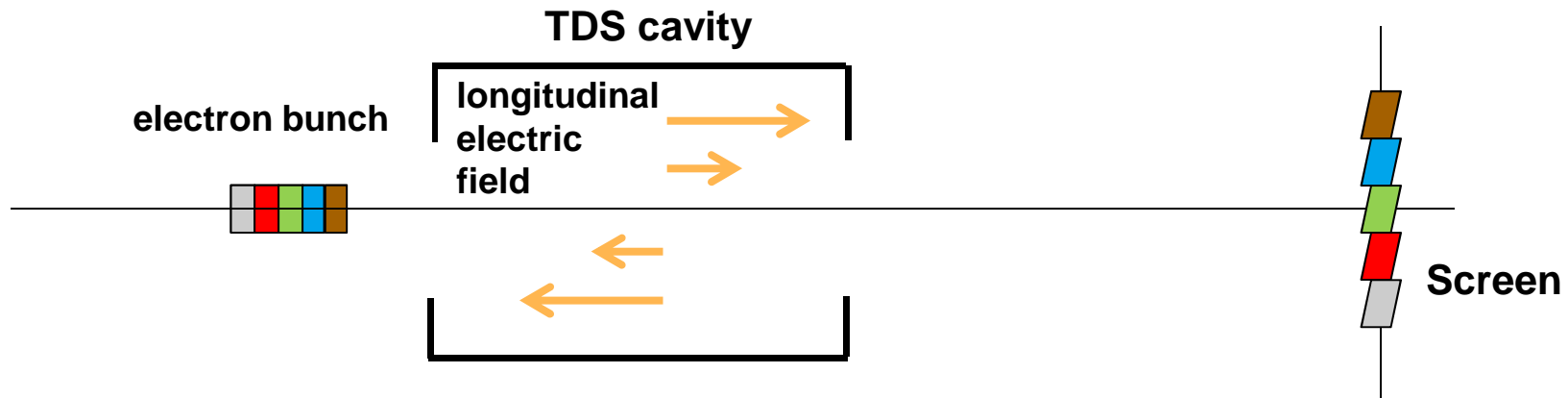
PITZ bunch typical parameter:

charge: 1 nC

length: 8 mm (24 ps)



# TDS induced energy gain?



Panofsky-Wenzel  
theorem

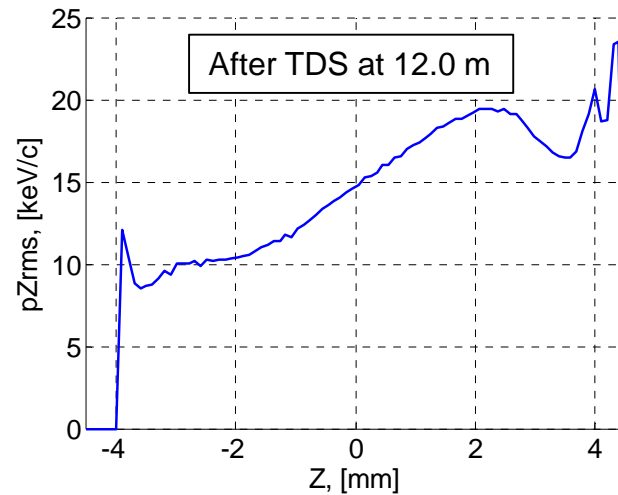
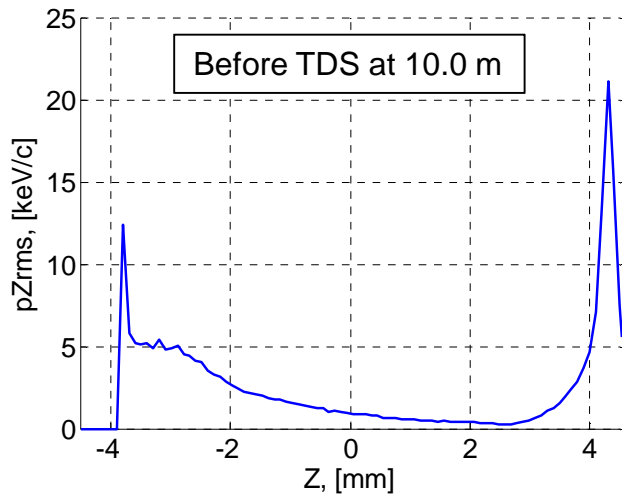
$$\frac{\partial}{\partial z} F_{\perp} = -\nabla_{\perp} F_{\parallel}$$

$$F_{\perp} = -\nabla_{\perp} \int_{-\infty}^{+\infty} eE_{\parallel} dz$$

$$\sigma_{\delta} = \frac{eV_0 k}{p_0 c} \cdot \sigma_y(s_0)$$



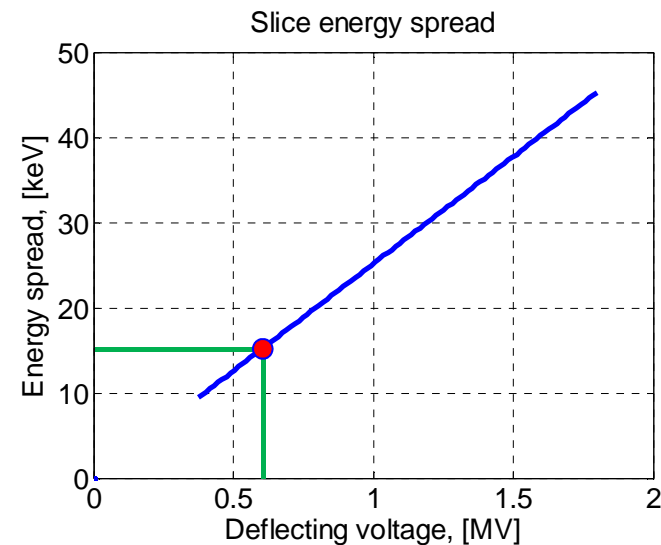
# TDS induced energy spread



For  $V_0 = 0.6$  MV, and  
beam size inside TDS  
 $\sigma_y = 0.4$  mm

$$\sigma_\delta = \frac{eV_0 k}{p_0 c} \cdot \sigma_y(s_0)$$

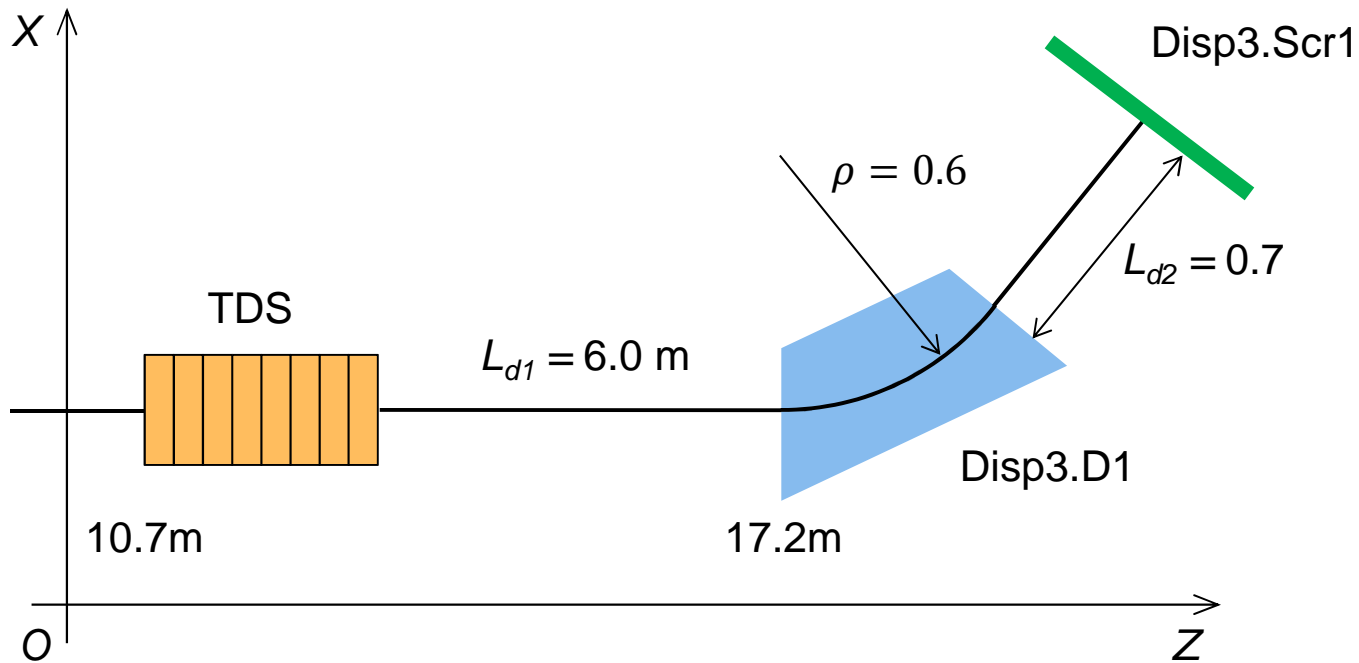
For the  $V_0 = 0.6$  MV, relative energy spread will be  $7 \cdot 10^{-4}$ , which is about 15 keV for 25 MeV beam.



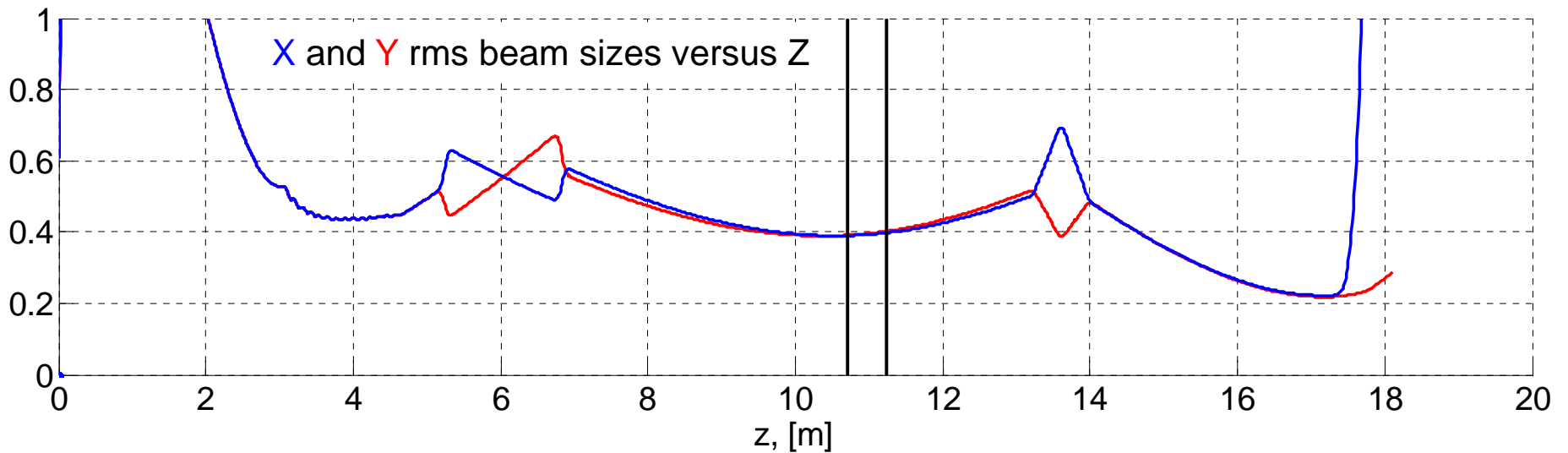
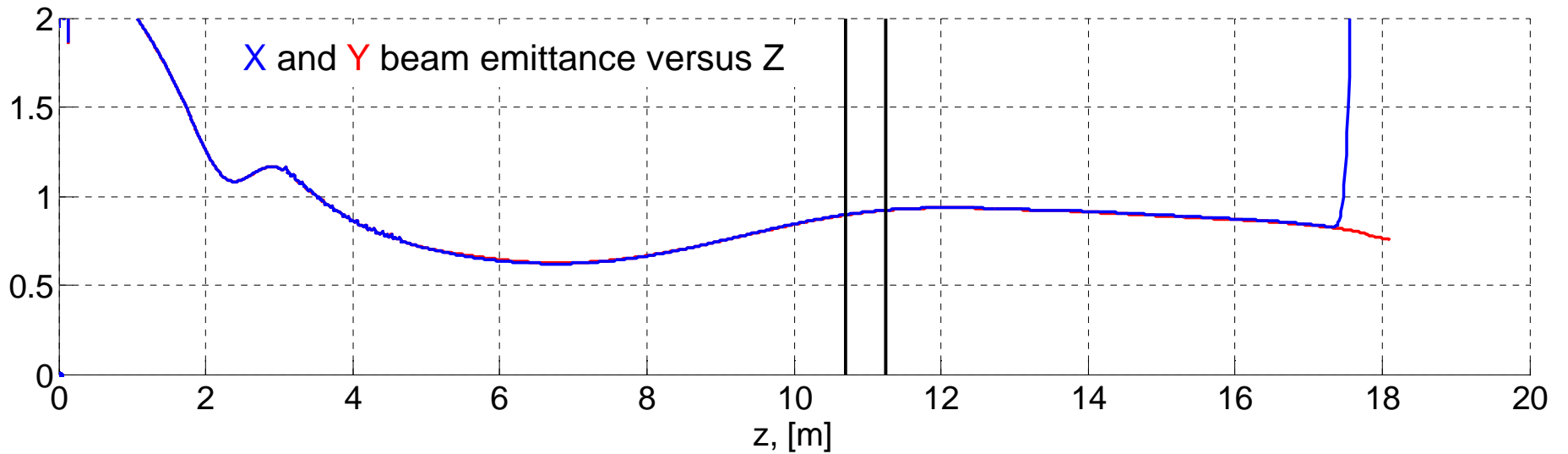
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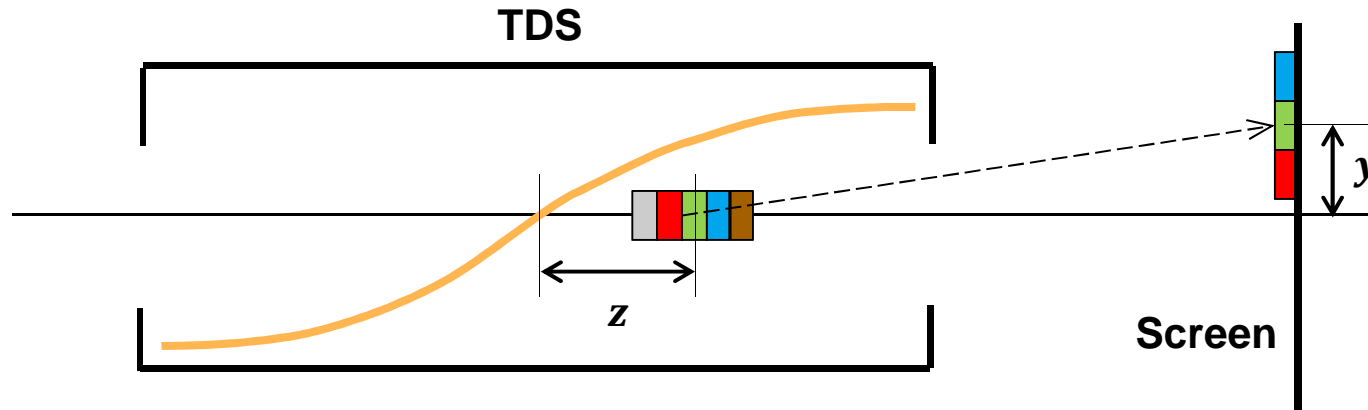
# TDS measurement setup



# TDS beam optics, emittance and beam size



# TDS calibration



$$S = \sqrt{\beta(s) \cdot \beta(s_0)} \cdot \sin(\Delta\psi_y) \cdot \frac{eV_0 k}{pc}$$

$$y = S \cdot z,$$

$$z = \beta \cdot c \cdot \Delta t = \frac{\beta \cdot c \cdot \Delta\varphi}{2 \cdot \pi \cdot f},$$

$$y = \frac{S \cdot \beta \cdot c}{2 \cdot \pi \cdot f} \cdot \Delta\varphi = \frac{S \cdot \beta \cdot c}{360 \cdot f} \cdot \Delta\Phi$$

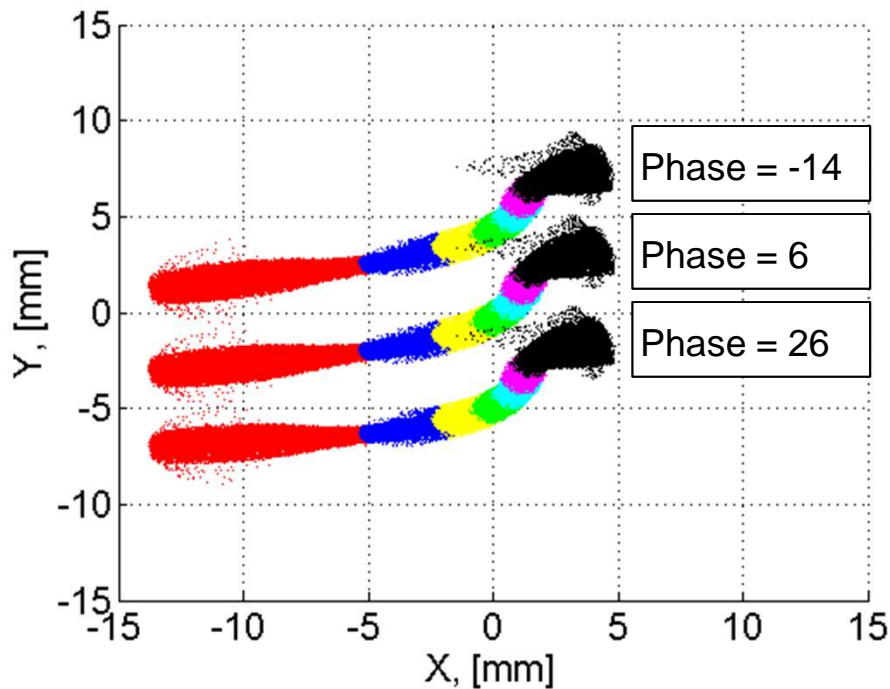
$$y = K_1 \cdot \Delta\Phi, \text{ where}$$

$$K_1 = \frac{S \cdot \beta \cdot c}{360 \cdot f}$$

or

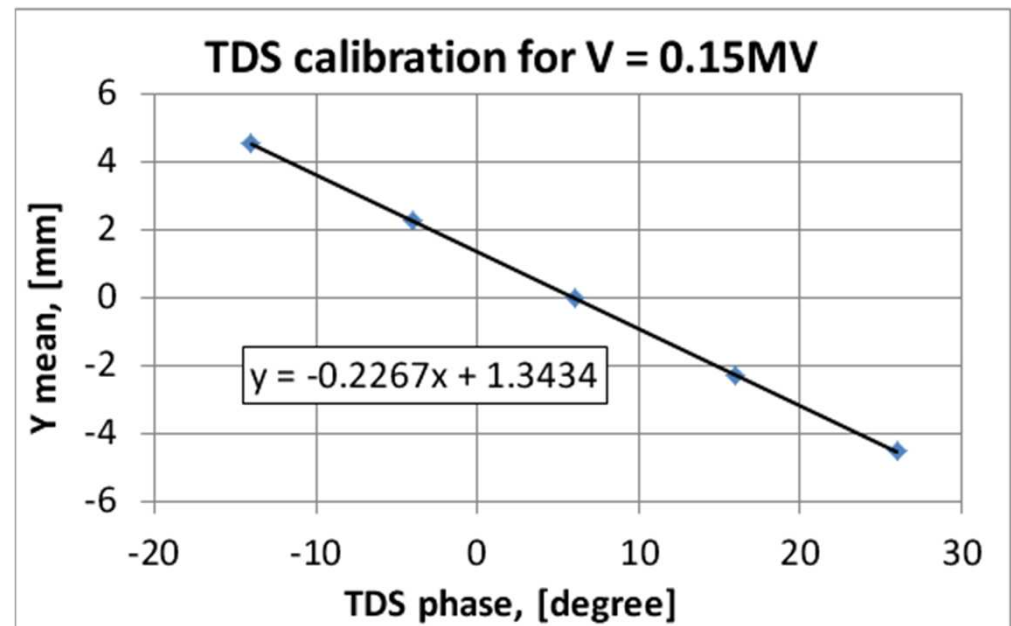
$$S = \frac{K_1 \cdot 360 \cdot f}{\beta \cdot c}$$

# TDS calibration, beam position versus RF phase

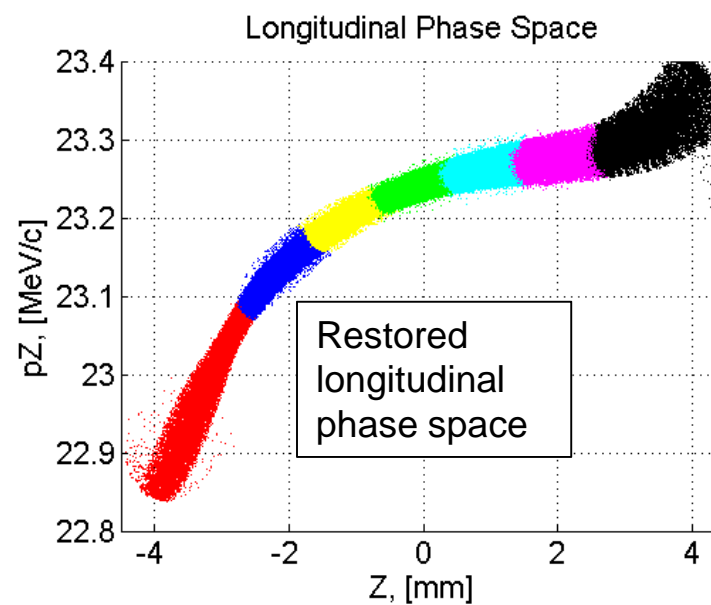
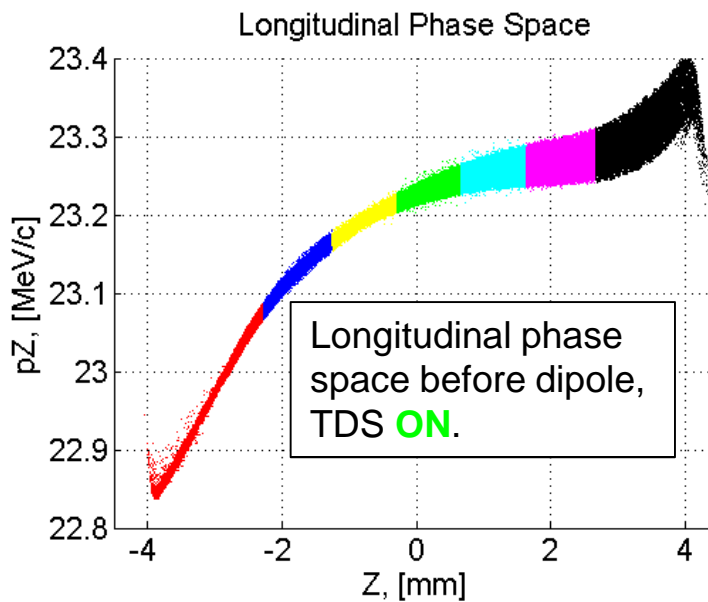
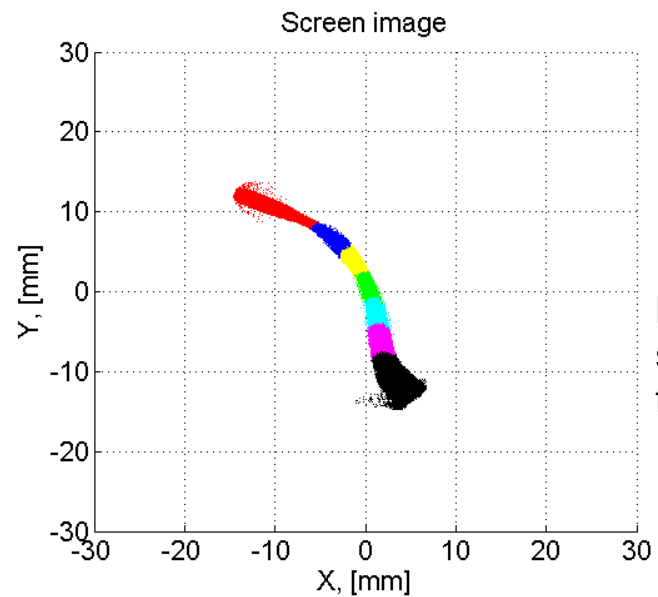
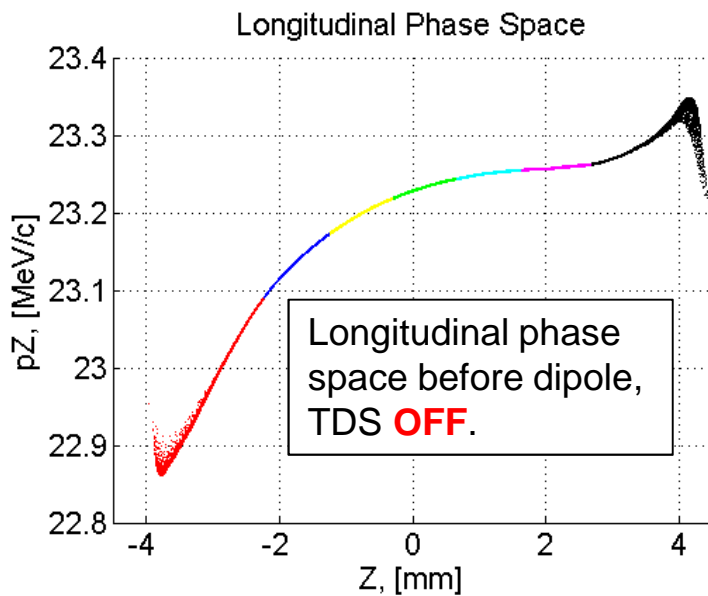


Bunch image for three different TDS RF phase, 0.15MV deflecting voltage.

For  $K_1 = 0.2267 \cdot 10^{-3}$   
 $S = 0.817$  (0.15MV), or  
 $S = 3.266$  (0.60MV)

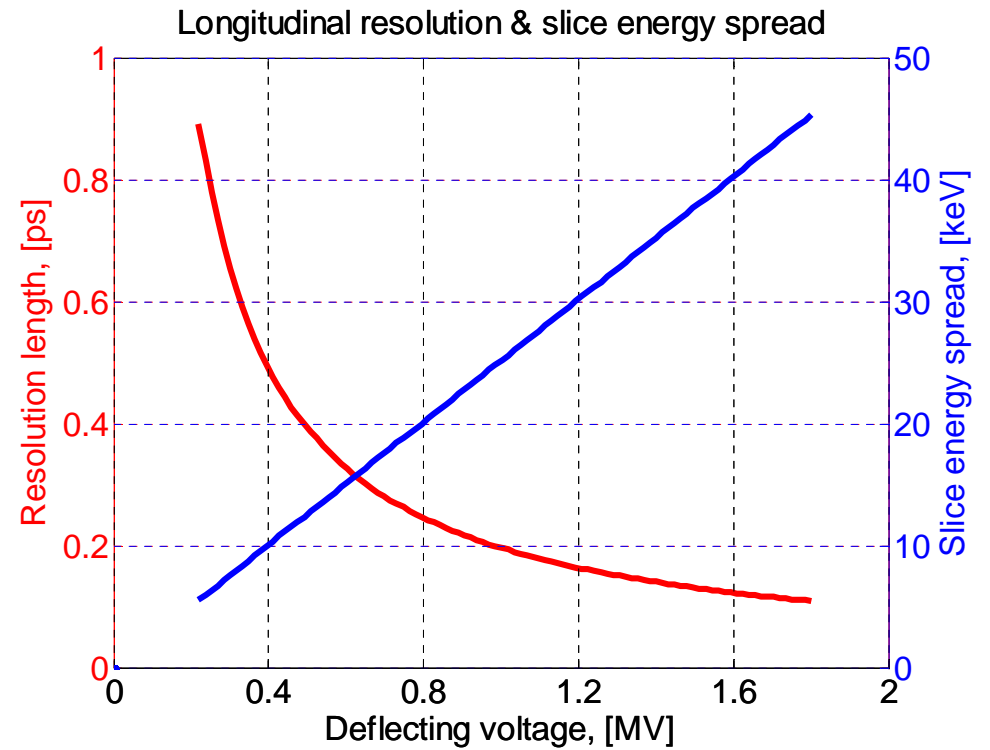


# TDS longitudinal phase space measurement



# Summary

- TDS longitudinal resolution for 0.6 MV deflecting voltage – 0.3 ps.
- TDS induced slice energy spread is about 15 keV.

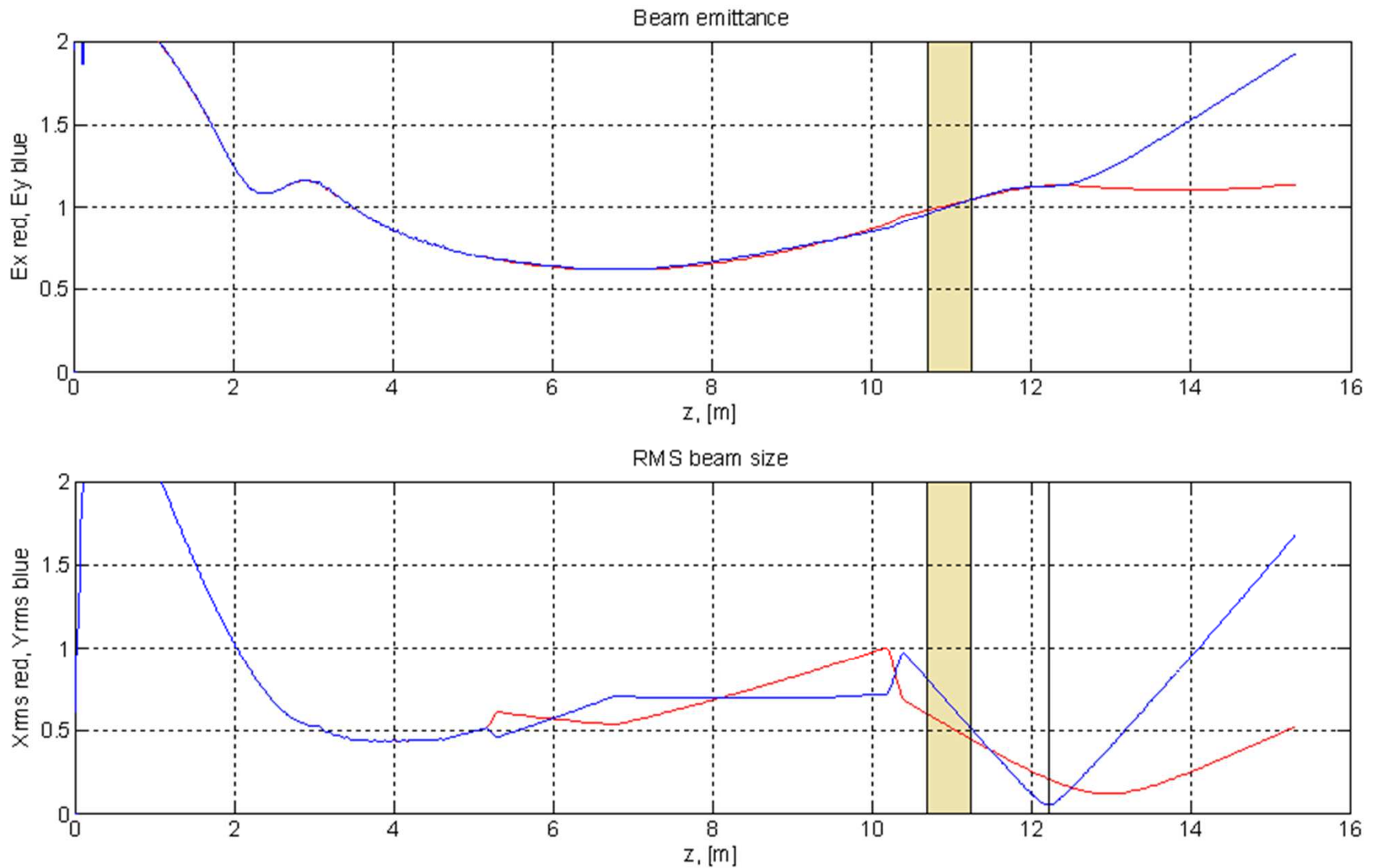




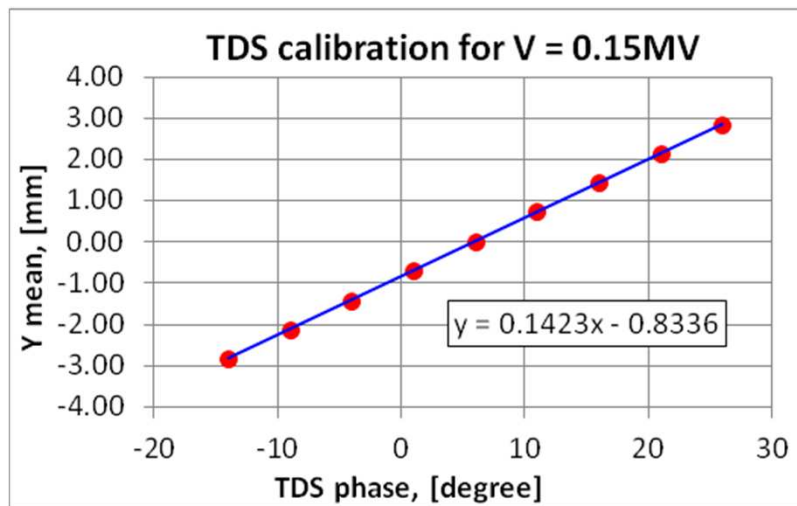
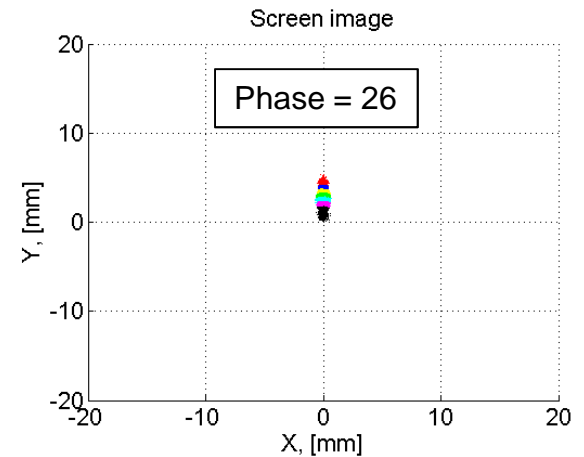
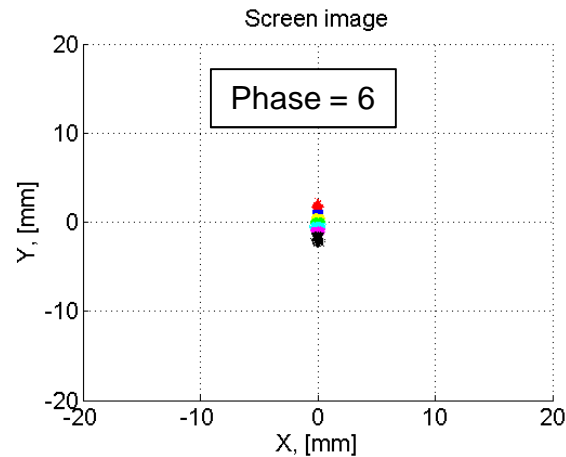
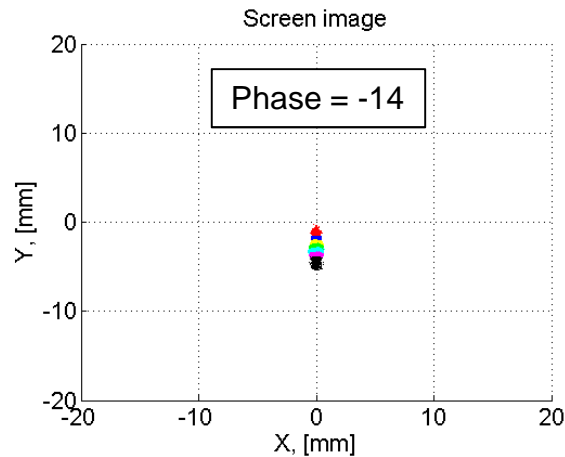
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# Beam optics, ASTRA simulation, 1nC



# TDS calibration at PST.Scr1, 1nC bunch charge



$$S = \frac{K_1 \cdot 360 \cdot f}{\beta \cdot c} = 0.51$$

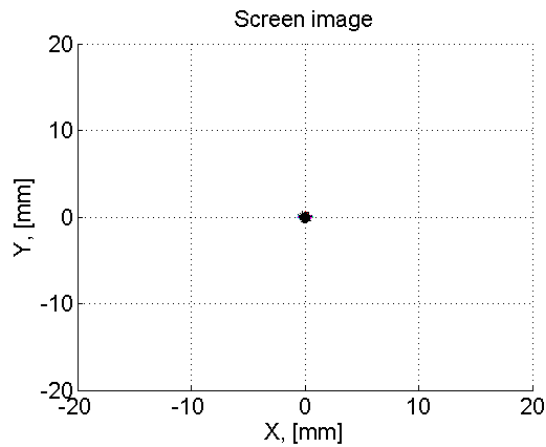
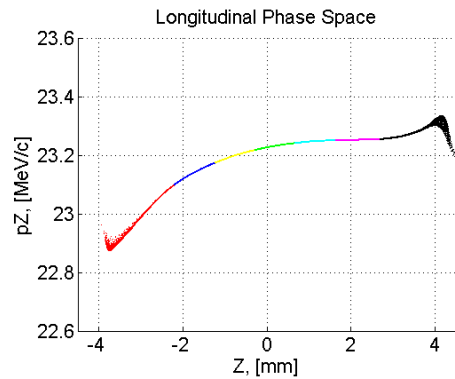
$$S(0.6MV) = 2.046$$

$$S(1.2MV) = 4.092$$



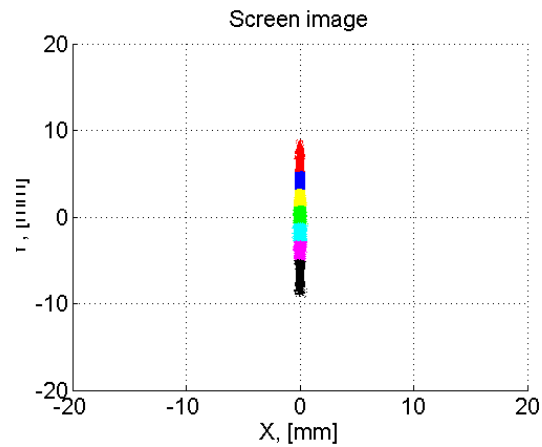
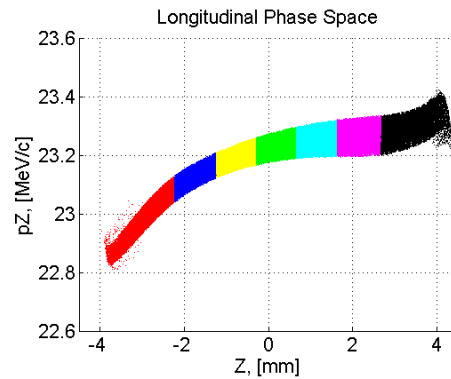
# First screen after TDS at 12.238m (PST.Scr1), 1nC

$V_0=0.0\text{MV}$



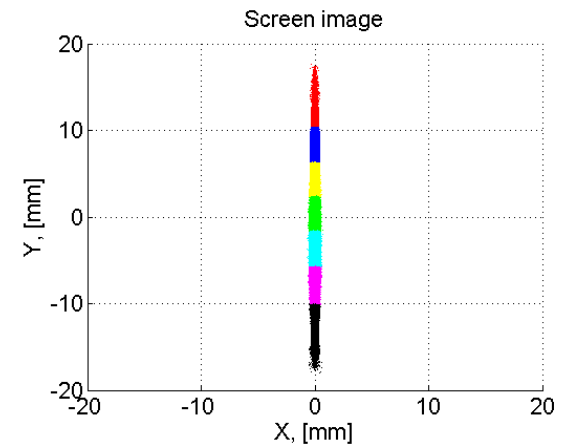
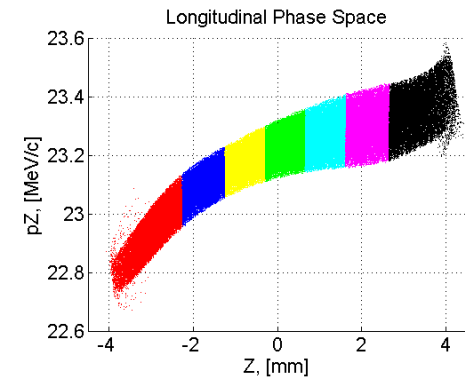
$X_{rms} = 0.21\text{mm}$   
 $Y_{rms} = 0.05\text{mm}$

$V_0=0.6\text{MV}$



$S = 2.0$   
 $\sigma_z = 25\mu\text{m} = 80\text{fs}$

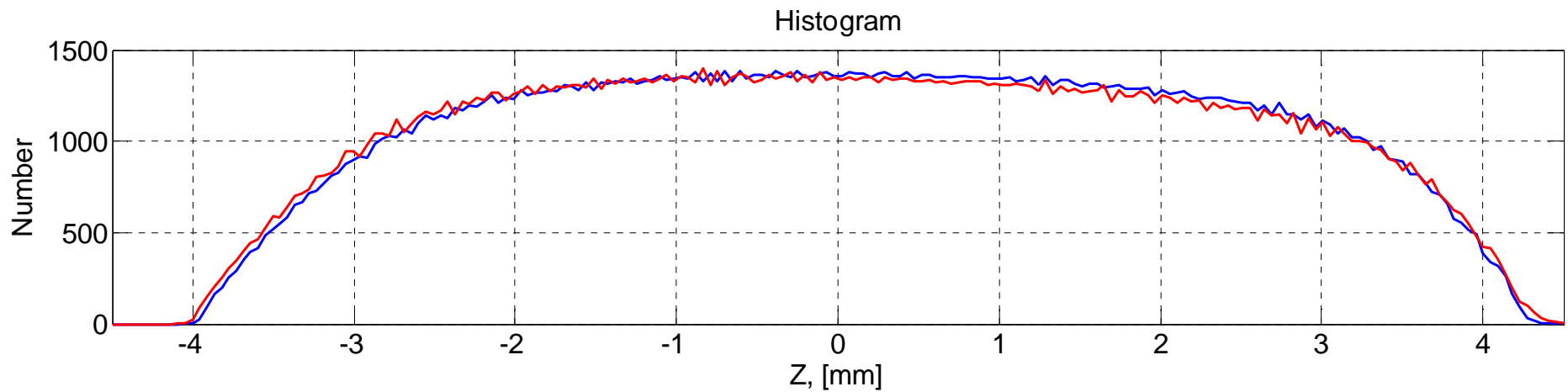
$V_0=1.2\text{MV}$



$S = 4.0$   
 $\sigma_z = 12\mu\text{m} = 40\text{fs}$



# Bunch longitudinal profile, 1nC

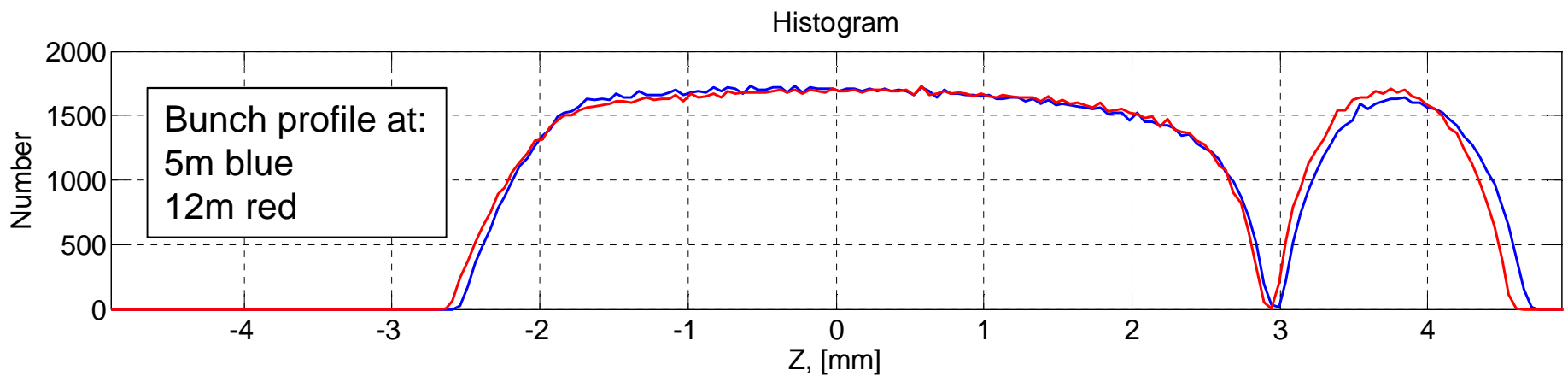
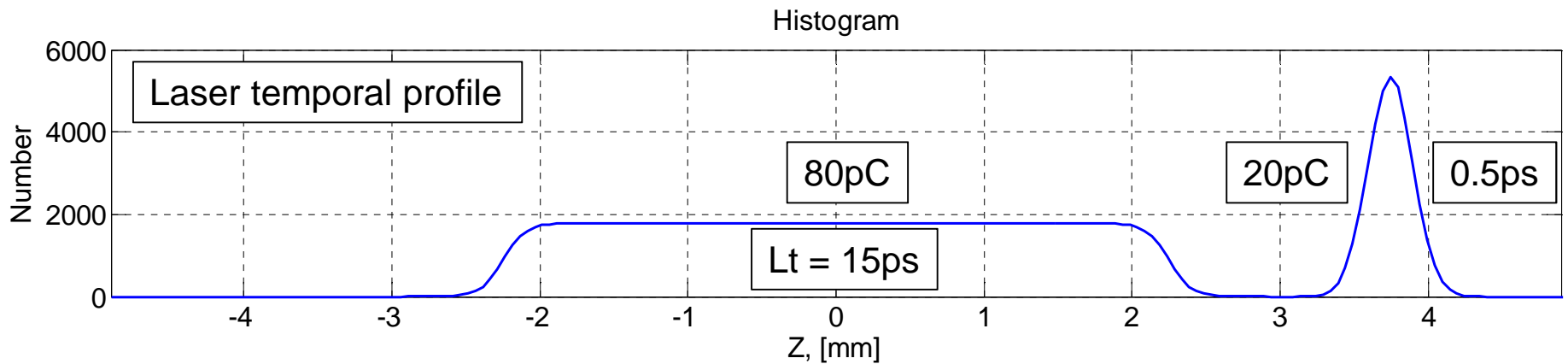


Blue line – bunch longitudinal profile at screen position

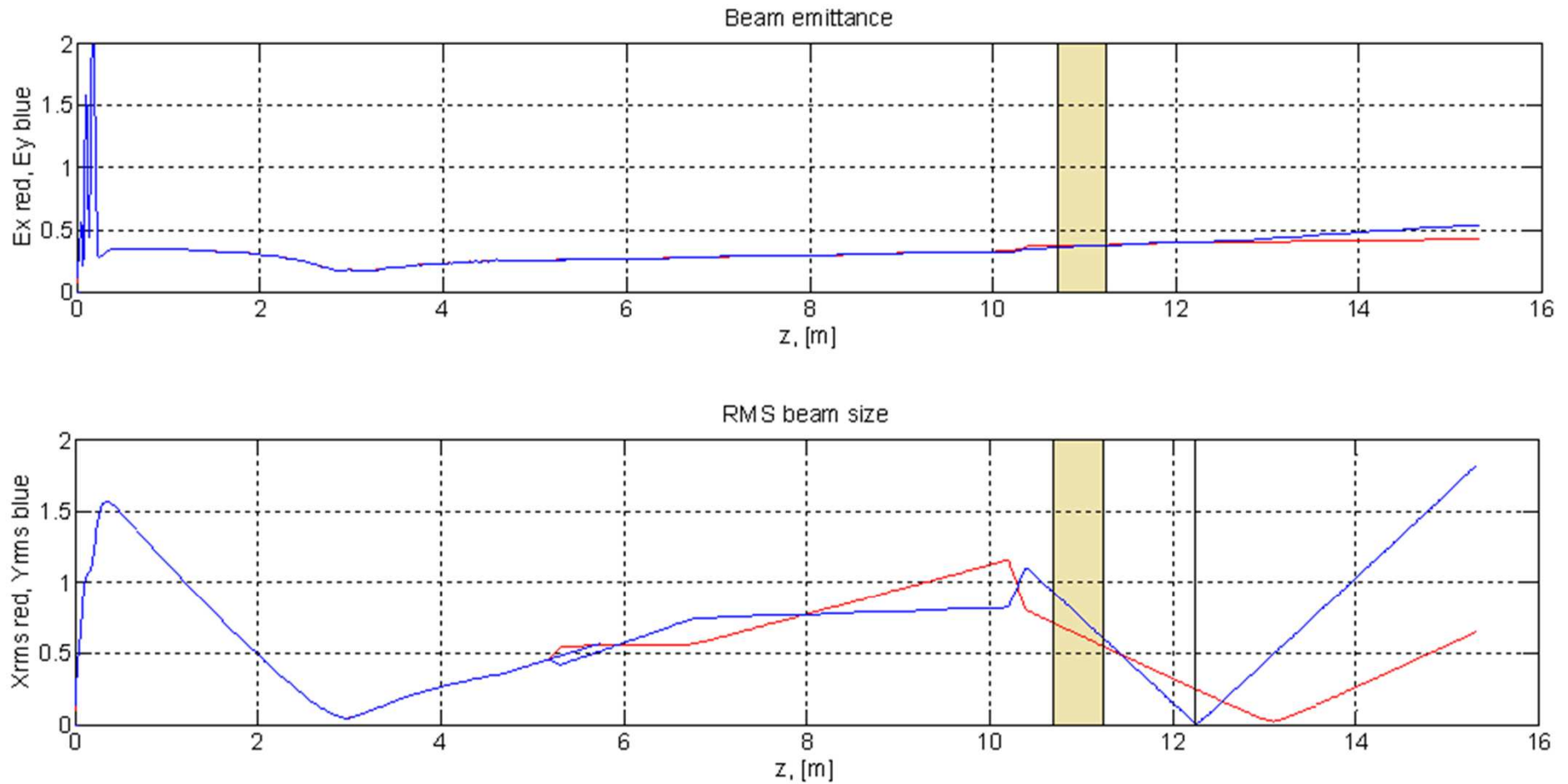
Red line – vertical profile of bunch image at screen scaled with  $S = 4.1$ .



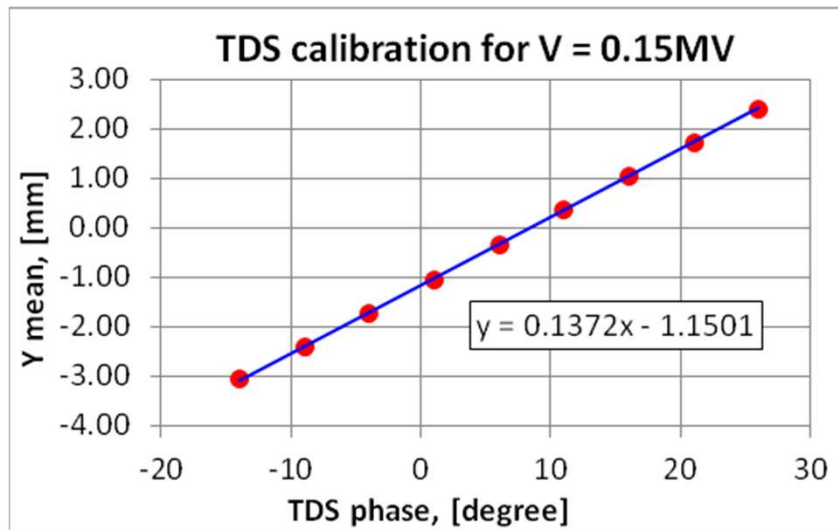
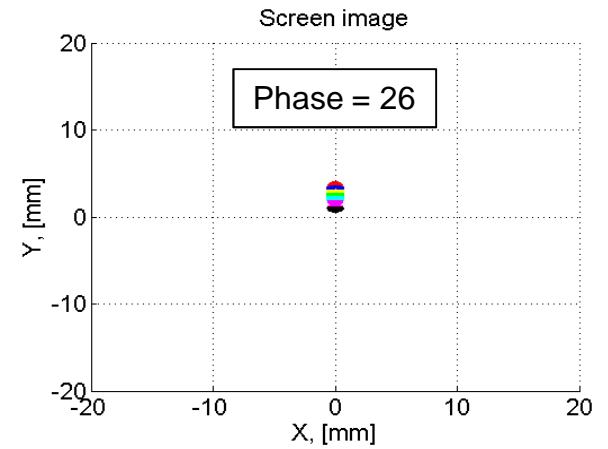
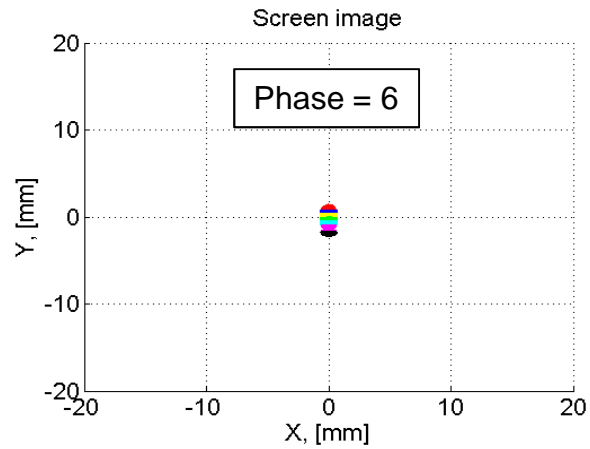
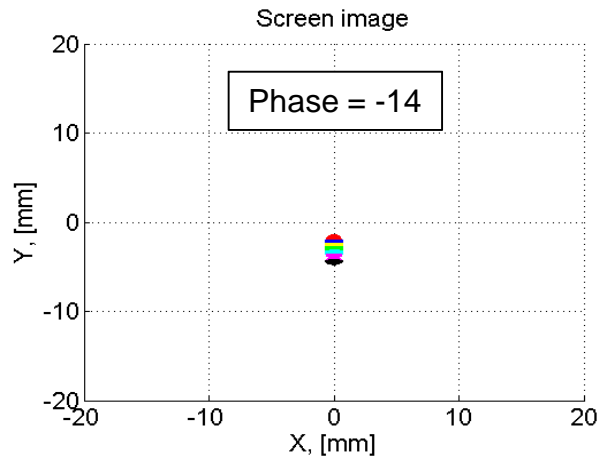
# Simulation with 100pC, special profile



# Beam optics, ASTRA simulation, 100pC



# TDS calibration at PST.Scr1, 100pC bunch charge



$$S = \frac{K_1 \cdot 360 \cdot f}{\beta \cdot c} = 0.49$$

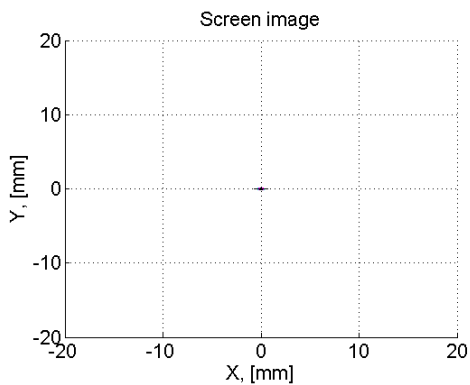
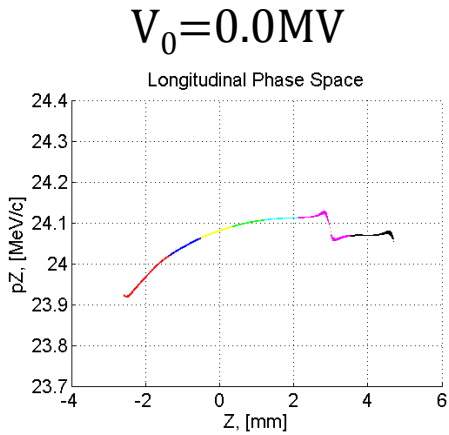
$$S(0.6MV) = 1.977$$

$$S(1.2MV) = 3.954$$

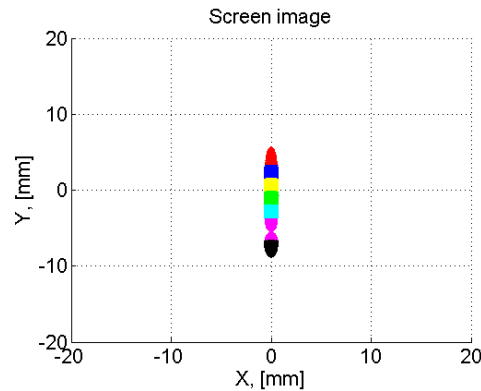
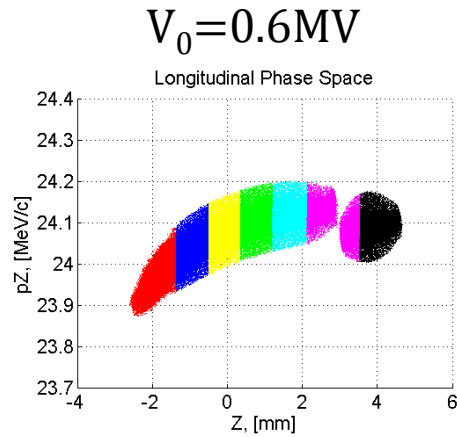




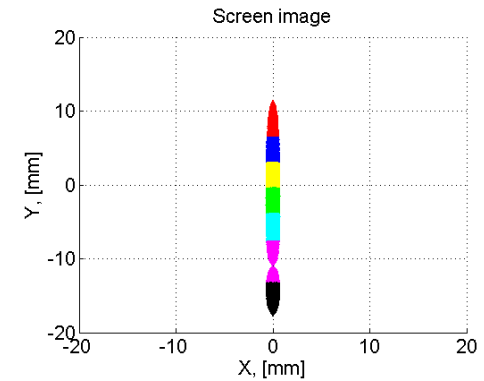
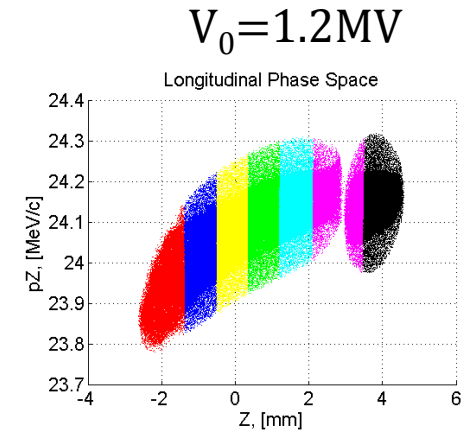
# First screen after TDS at 12.238m (PST.Scr1), 100pC



$X_{rms} = 0.256\text{mm}$   
 $Y_{rms} = 0.024\text{mm}$

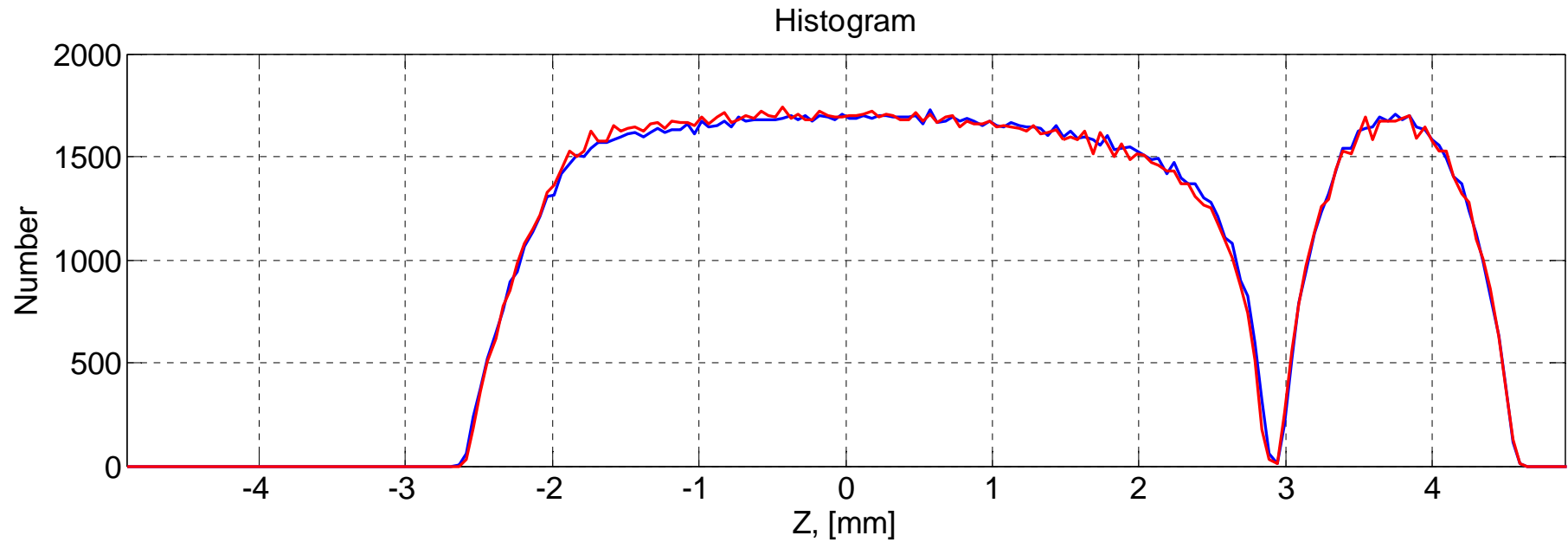


$S = 2.0$   
 $\sigma_z = 12\mu\text{m} = 40\text{fs}$



$S = 4.0$   
 $\sigma_z = 6\mu\text{m} = 20\text{fs}$

# Bunch longitudinal profile, 100pC



Blue line – bunch longitudinal profile at screen position

Red line – vertical profile of bunch image at screen Scaled with  $S = 4$

# Conclusion

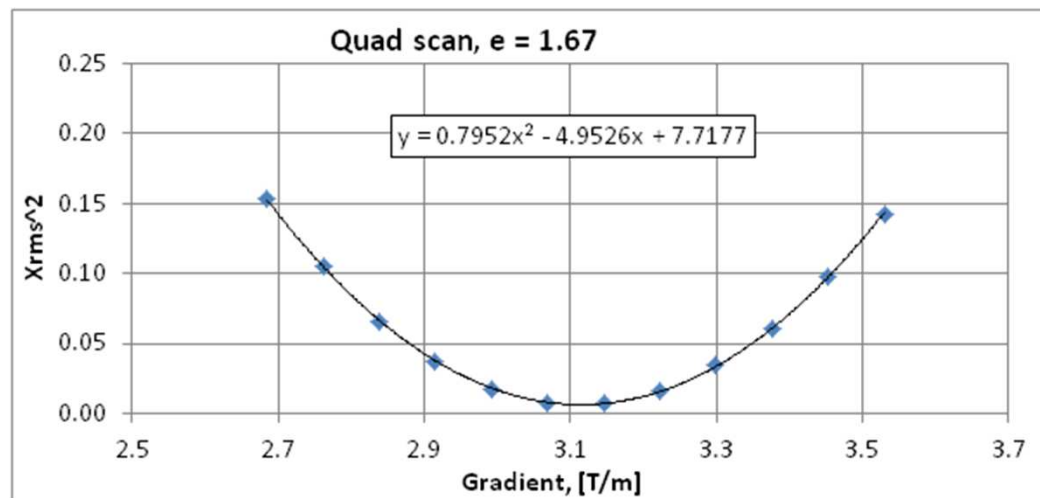
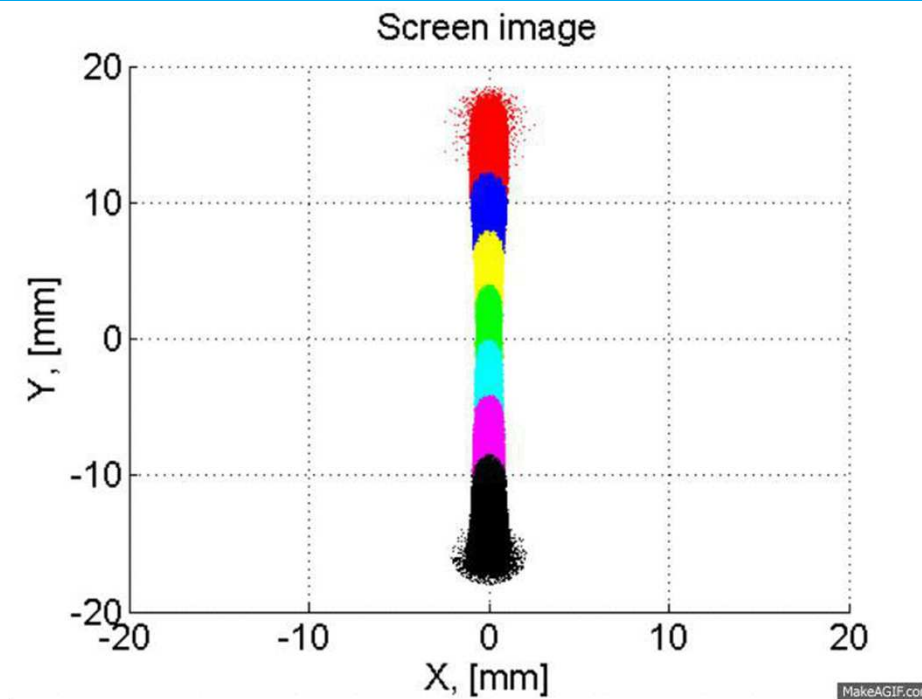
- > Measured bunch longitudinal profile looks identical to the real one (both are results of simulation).
- > Achievable longitudinal resolution is **6 $\mu\text{m}$**  or **20fs** for **100pC** bunch, and **12 $\mu\text{m}$**  or **40fs** for **1nC** bunch charge.



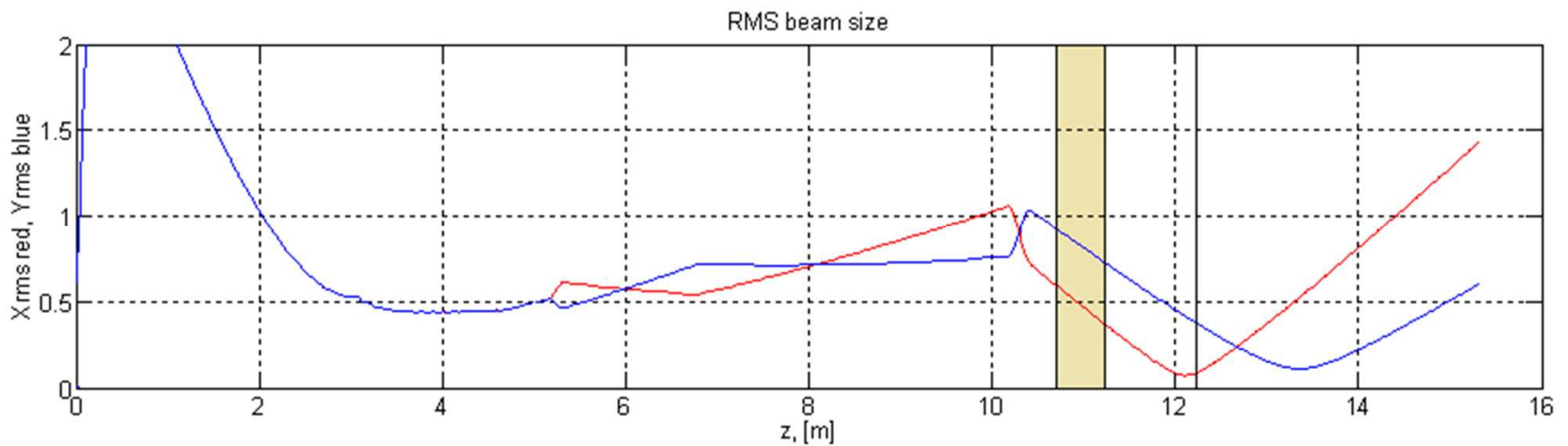
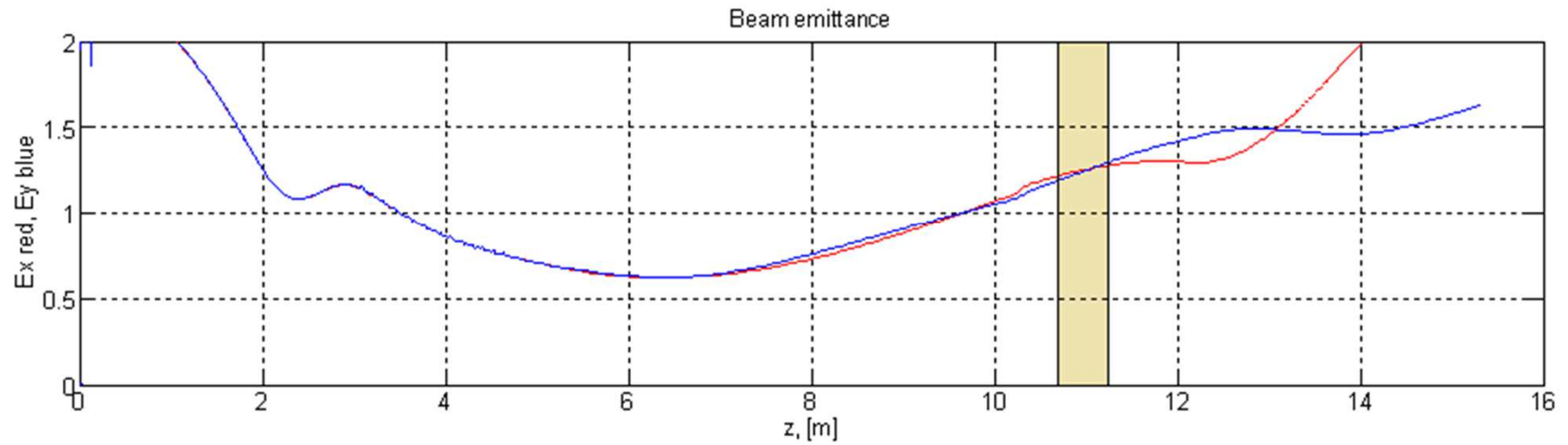
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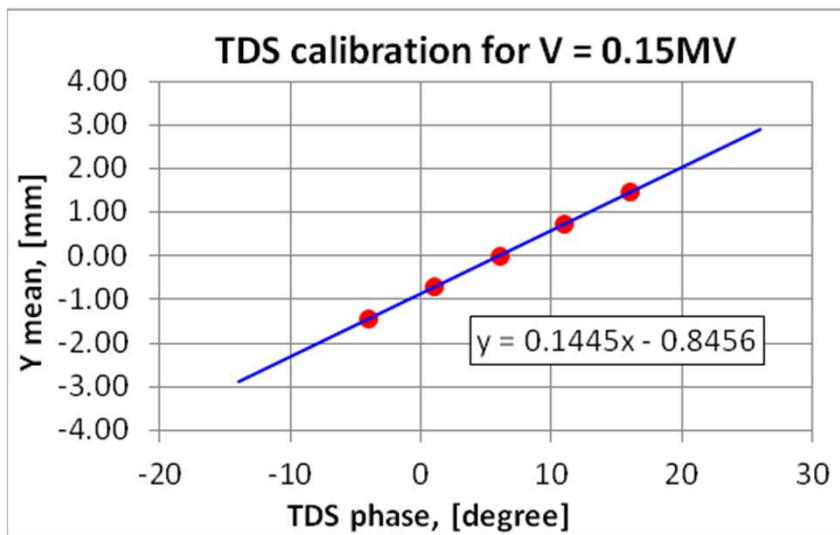
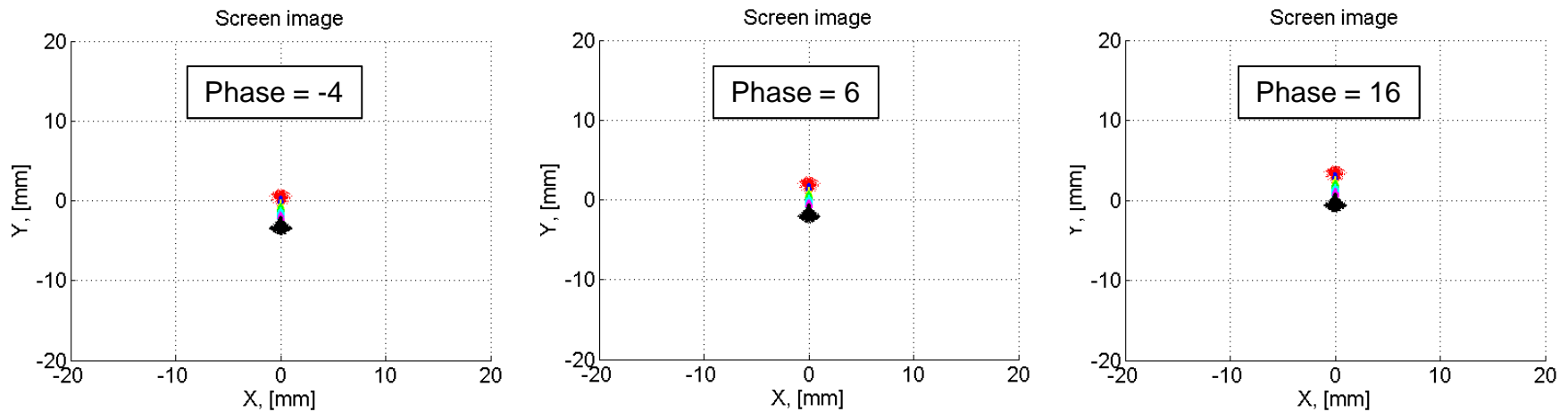
# Quad scan (H1.Q6) with TDS deflecting voltage 1.2 MV.



# Beam optics, ASTRA simulation, 1nC



# TDS calibration at PST.Scr1, 1nC bunch charge



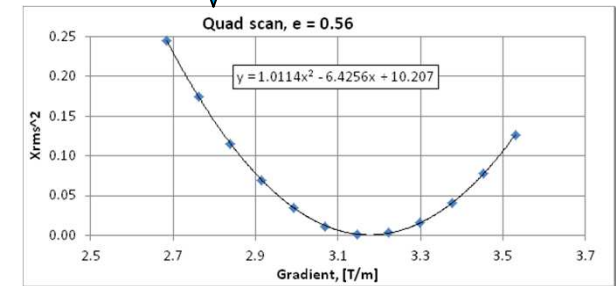
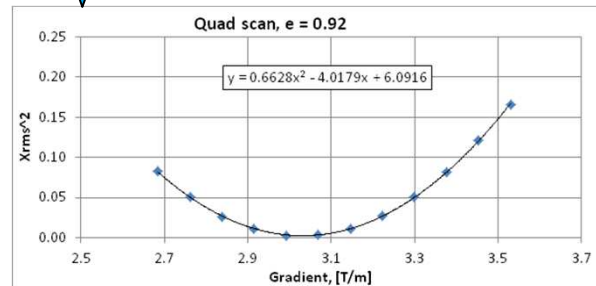
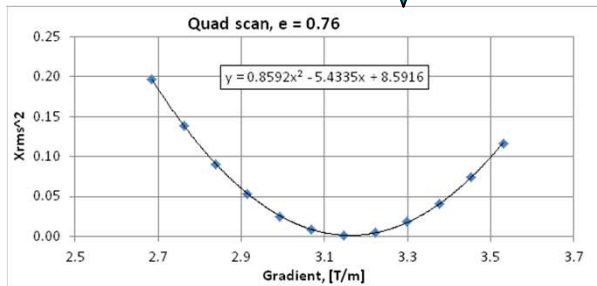
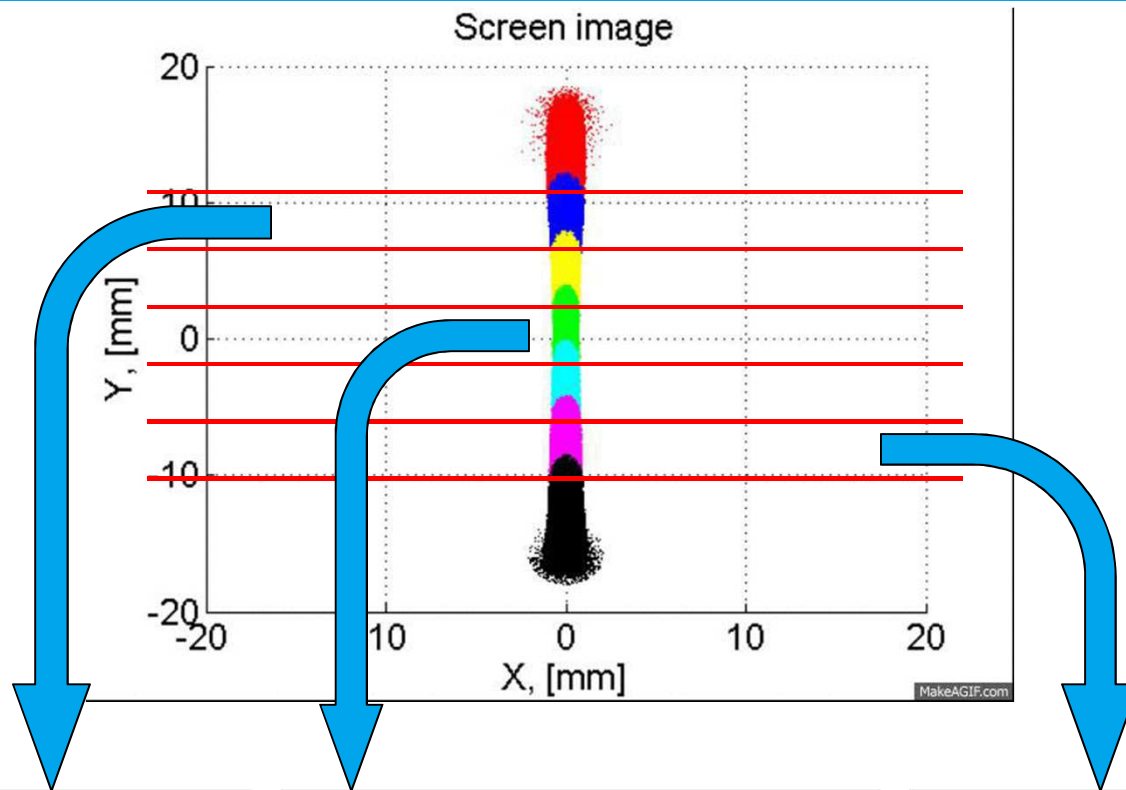
$$S = \frac{K_1 \cdot 360 \cdot f}{\beta \cdot c} = 0.5121$$

$$S(0.6MV) = 2.083$$

$$S(1.2MV) = 4.165$$

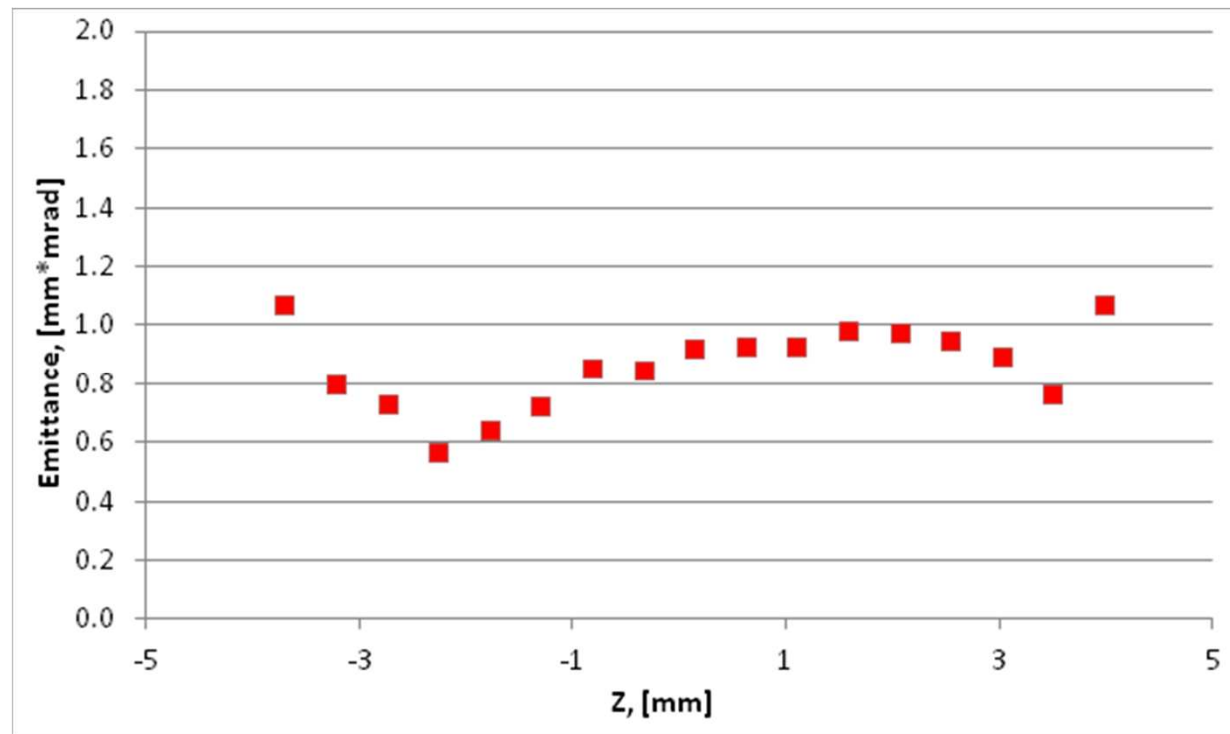


# Quad scan (H1.Q6) with TDS deflecting voltage 1.2 MV.

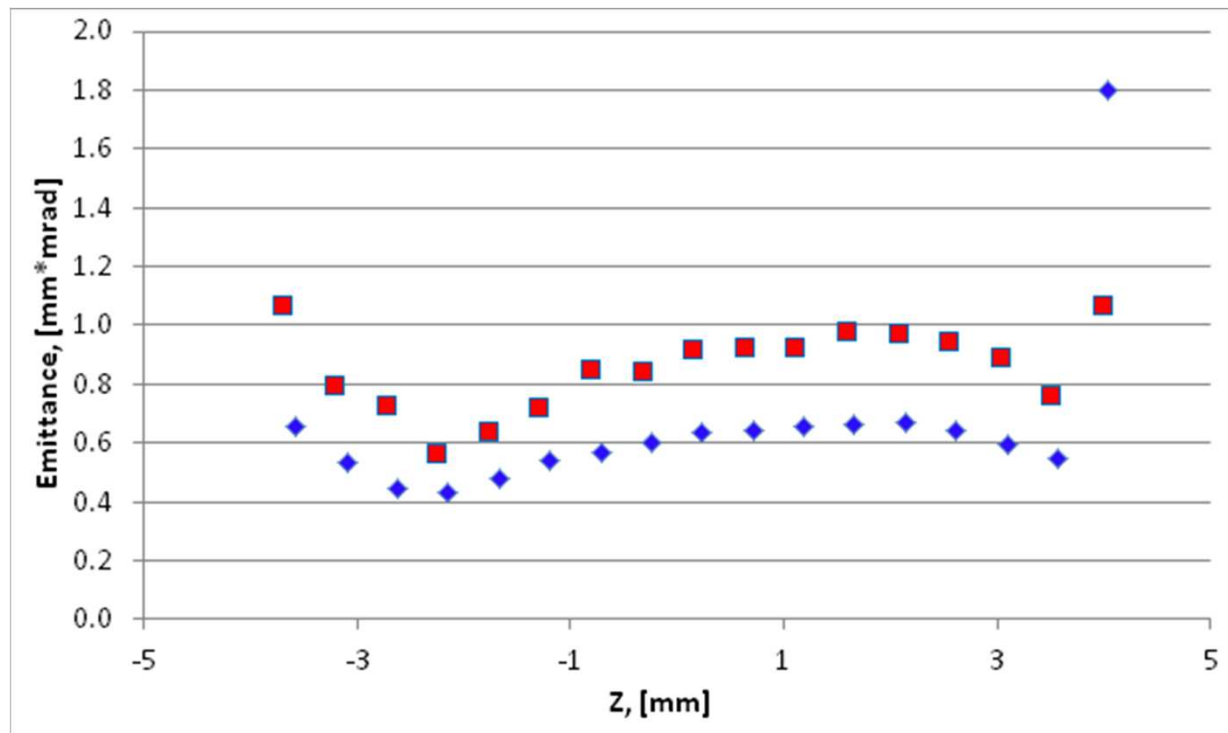




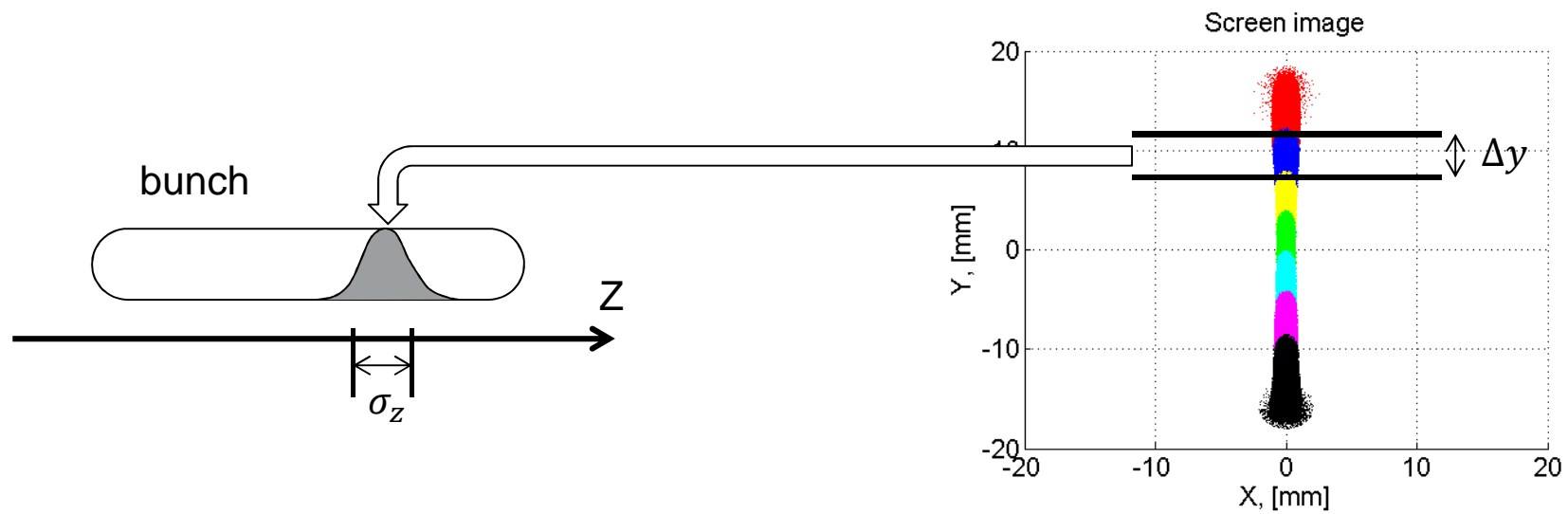
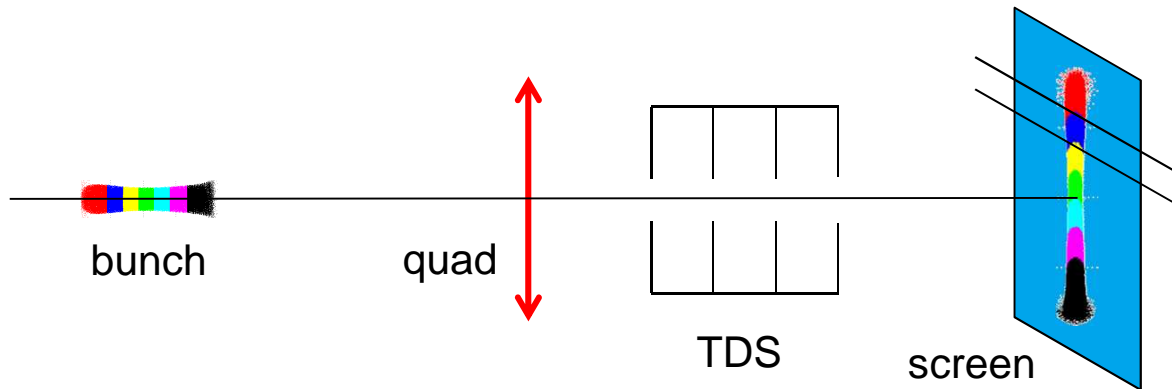
# Quad scan summary



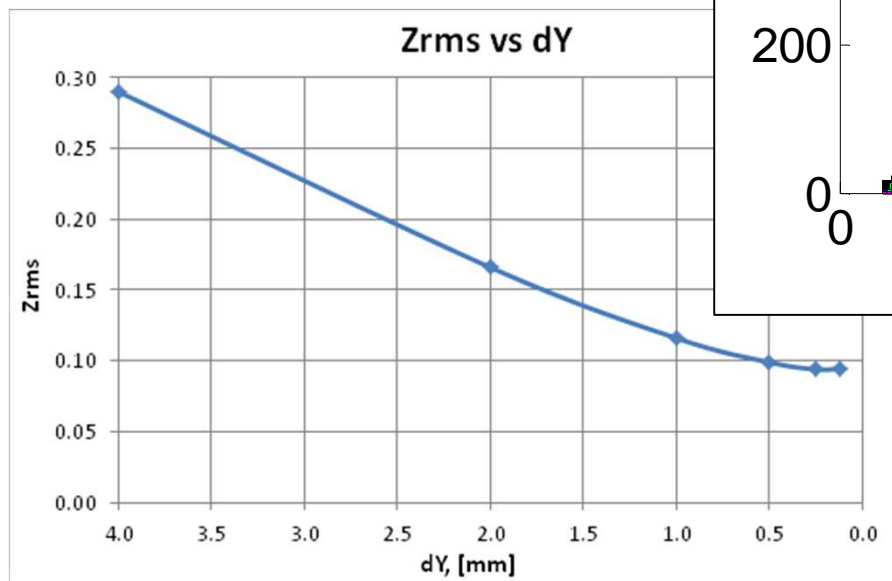
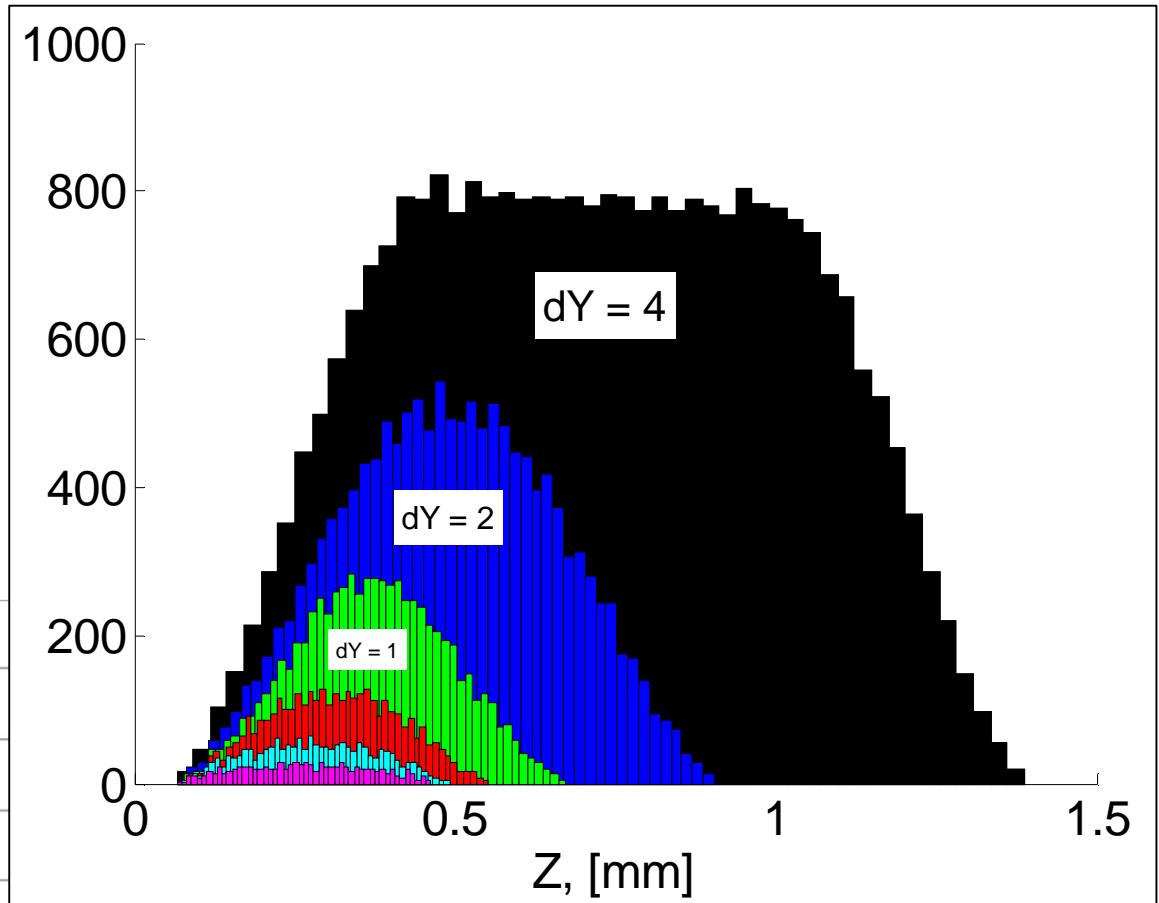
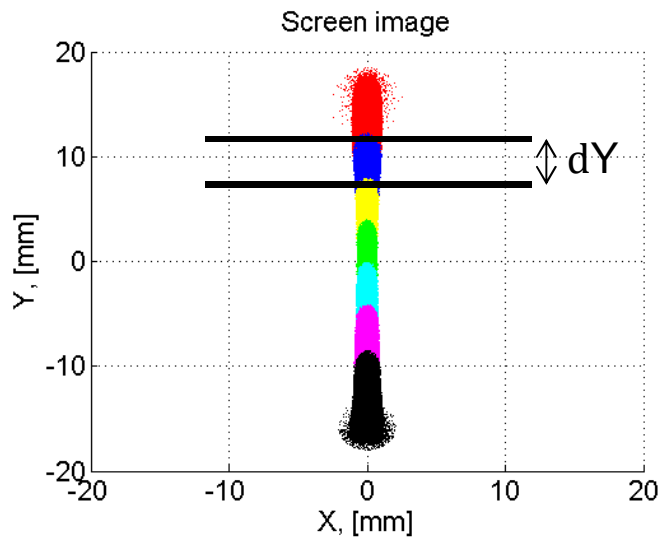
# Quad scan summary, compare results



# Longitudinal resolution



# Slice resolution, slice length $Z_{rms}$ and stripe width $dY$



# Conclusion

- > Slice emittance measurement simulation done in ASTRA for 1nC bunch charge
- > Achieved longitudinal resolution is about 0.1mm\* (RMS), which gives us about 80 slices per bunch.

\*for Gaussian distribution  $\text{RMS} = 0.1\text{mm}$  corresponds to  $\text{FWHM} = 0.24\text{mm}$



# Summary

- > Simulation of the longitudinal phase space measurement, bunch length measurement and slice emittance measurement were done with the ASTRA simulation code.
- > Simulated results are in good agreement to what was expected.
- > Achievable resolutions are:
  - 0.3 ps (0.1 mm) for longitudinal phase space measurement
  - 0.04 ps (0.012 mm) for bunch length measurement
  - 0.3 ps (0.1 mm) for slice emittance measurement

