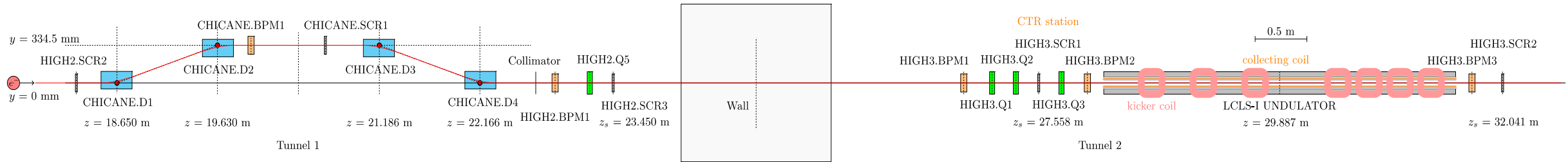


# Summary of PITZ BC commissioning studies

## PITZ Physics Seminar (PPS)



Ekkachai Kongmon

**PITZ**, 21 September 2023

HELMHOLTZ



# Outline

**PITZ Bunch Compressor**

**Beam trajectory simulation**

**Dispersion studies**

**Beam matching**

# PITZ Bunch Compressor

## PITZ magnetic bunch compressor

Specifications	Details
<b>LCLS-I undulator</b>	
Type	planar hybrid (NdFeB)
K-value	3.585 (3.49)
Support diameter / length	30 cm / 3.4 m
Vacuum chamber size	11 mm x 5 mm
Period length ( $\lambda_u$ )	30 mm
Periods / a module	113 periods
<b>e-beam</b>	
Beam momentum	17 – 22 MeV/c
Transvers rms beam size ( $\sigma_x, \sigma_y$ ) (Gaussian beam)	1 mm
e-beam peak current (I)	~200 – 400 A
Bunch charge	2 nC
<b>Radiation</b>	
Radiation wave length	~100 $\mu\text{m}$ (~ 17 MeV/c)

### 1D Model for FELs

$$\rho = \left[ \frac{I}{\gamma^3 I_A} \frac{\lambda_u^2}{2\pi\sigma_x\sigma_y} \frac{(K \times [JJ])^2}{32\pi} \right]^{1/3}$$

$$[JJ] = J_0(\xi) - J_1(\xi) \quad \xi = \frac{K^2}{2(2 + K^2)}$$

Maximum relative energy spread for the compression cases ( $\delta$ ) <  $\rho \approx 1\%$

$$\Delta z = R_{56} \delta_p$$

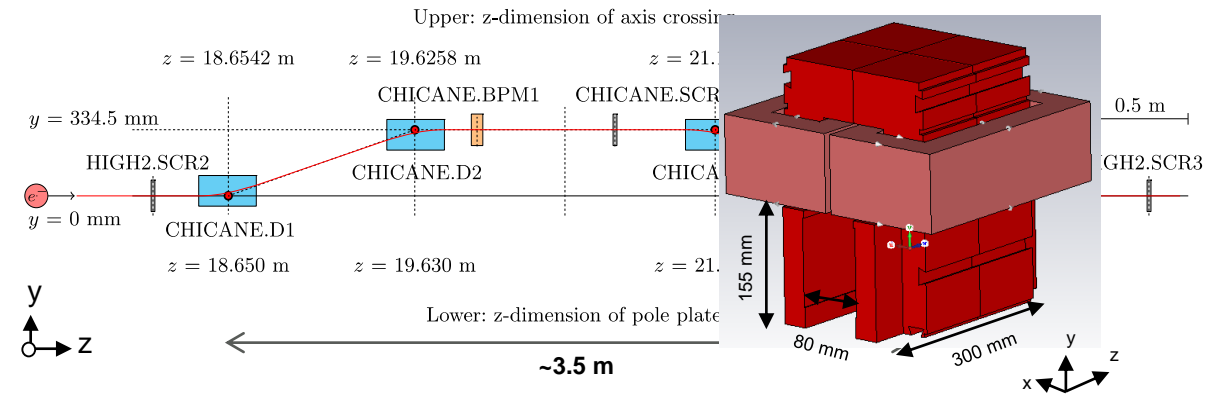
$$\delta \approx 1\%$$

$$\Delta z = 0.18 \text{ cm (6 ps)}$$

$$R_{56} = 0.180 \text{ m}$$

**Used to define geometry of the BC**

### Setup of the BC



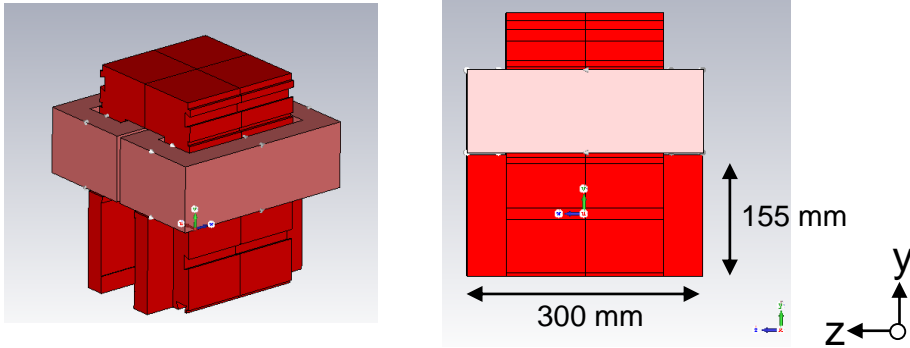
- Designed beam trajectory from **hard edge model** (modified from HERA dipoles)
- Vertical bending direction
- Bending angle : 19 deg.
- $R_{56} \approx -2\theta_0^2 \{ (L_{12} + \frac{2}{3} L_B) \} \rightarrow \sim 0.198 \text{ m}$

**Concept → match R56 between beam and BC**

# Beam transportation

# Chicane magnet

## Magnetic field, simulation vs. measurement



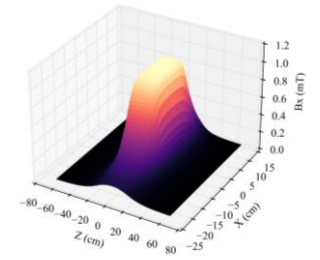
### Parameters

- Applied current : **1 A**
- Number of coil turns : 1332 turns per coil
- Maximum magnetic field in x-direction ( $B_x$ ) at  $(x, y) = (0, 0)$  along z-direction : **0.04235 T**

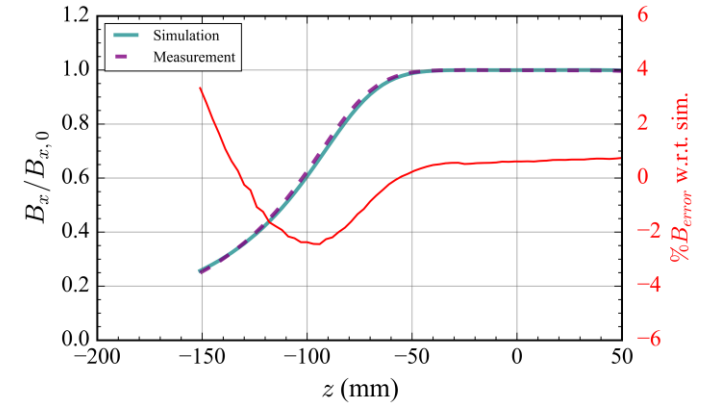
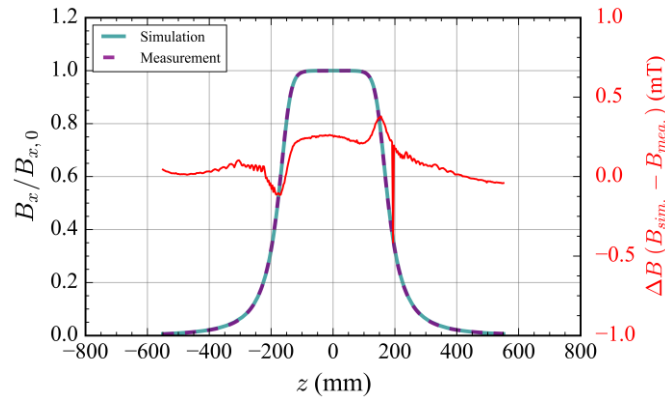
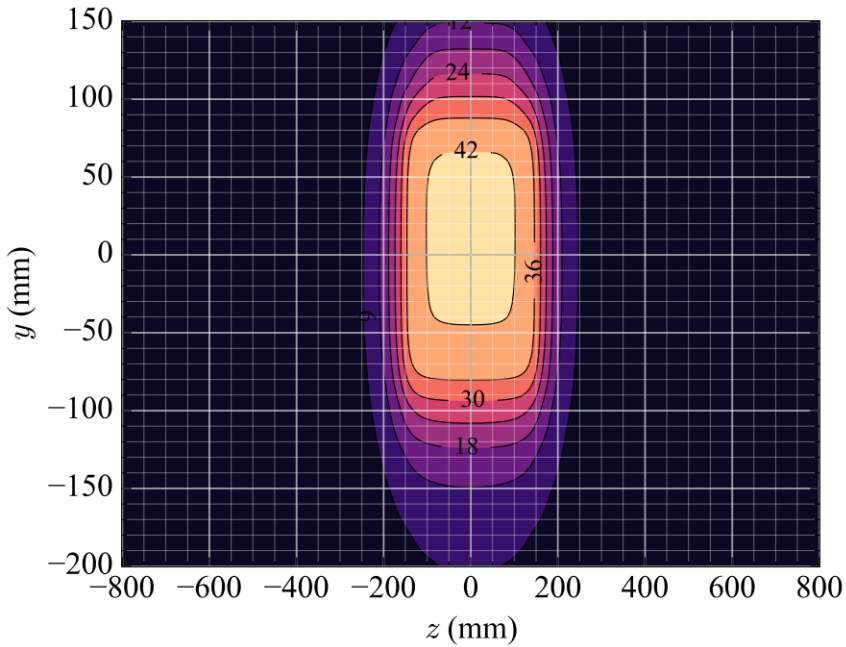
### Export 3D magnetic field (dimensions)

- D1 and D4 z : -850, 850, y : -70, 350 step 4 mm, x : -30, 30 step 1
- D2 and D3 z : -860, 860, y : -224, 100 step 4 mm, x : -30, 30 step 1

1 V.s = 1 T.m<sup>2</sup> From CST (V.s/m<sup>2</sup> = T)



Plane:  $x = 0$

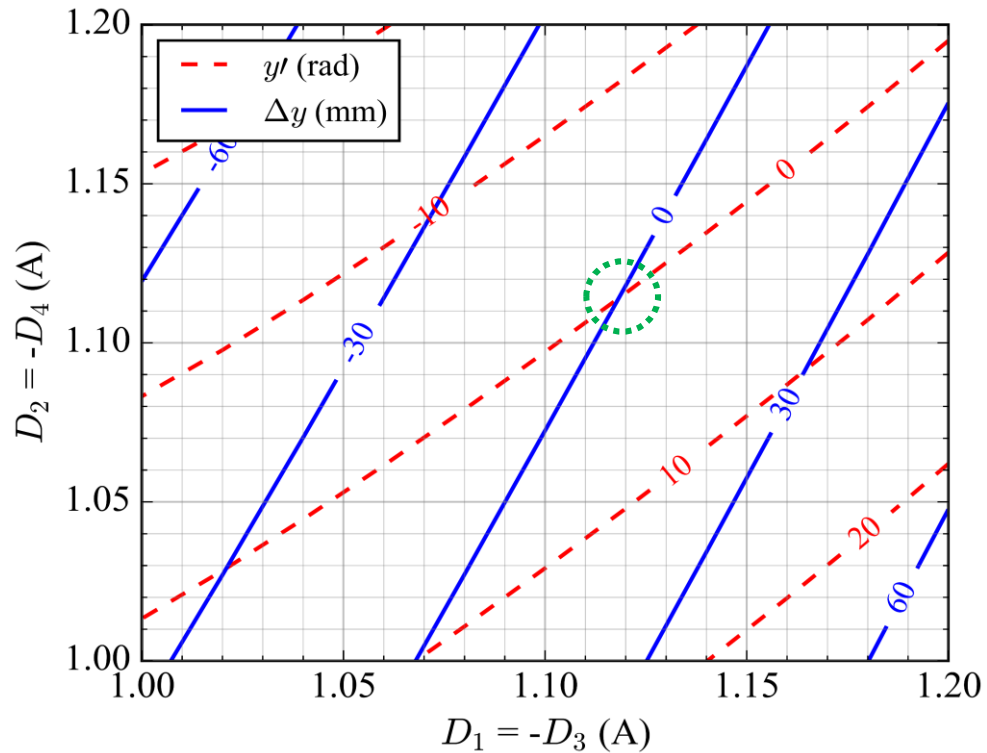


# Beam trajectory simulations

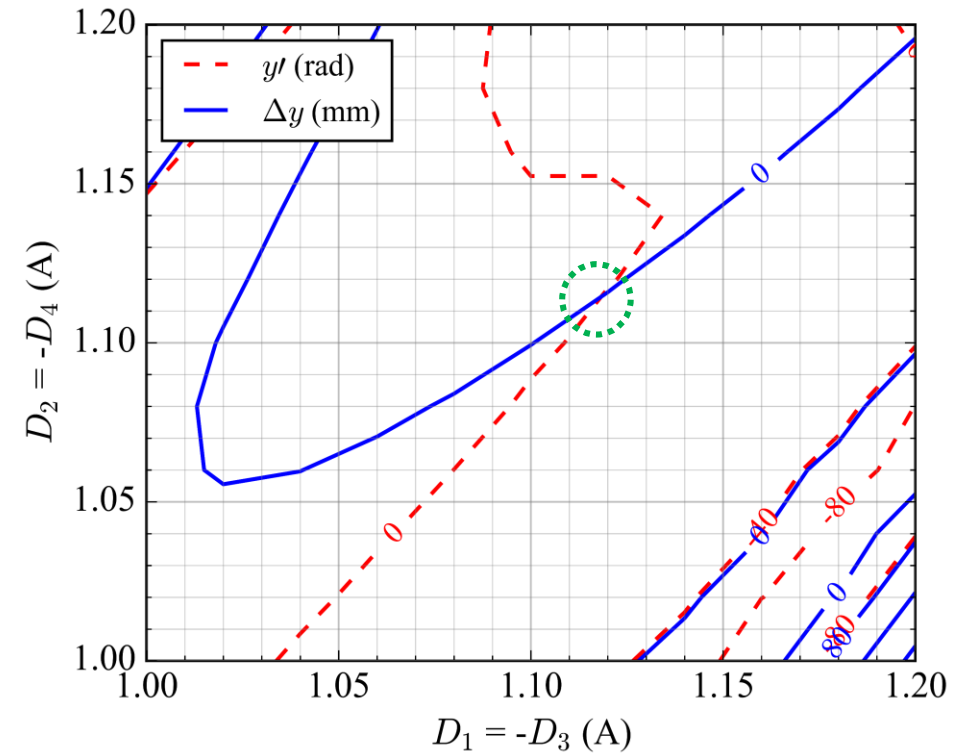
**D1 = D3 and D2 = D4**

- Average beam momentum : 17 MeV/c
- Bunch charge : **250 pC**

At Center of BC

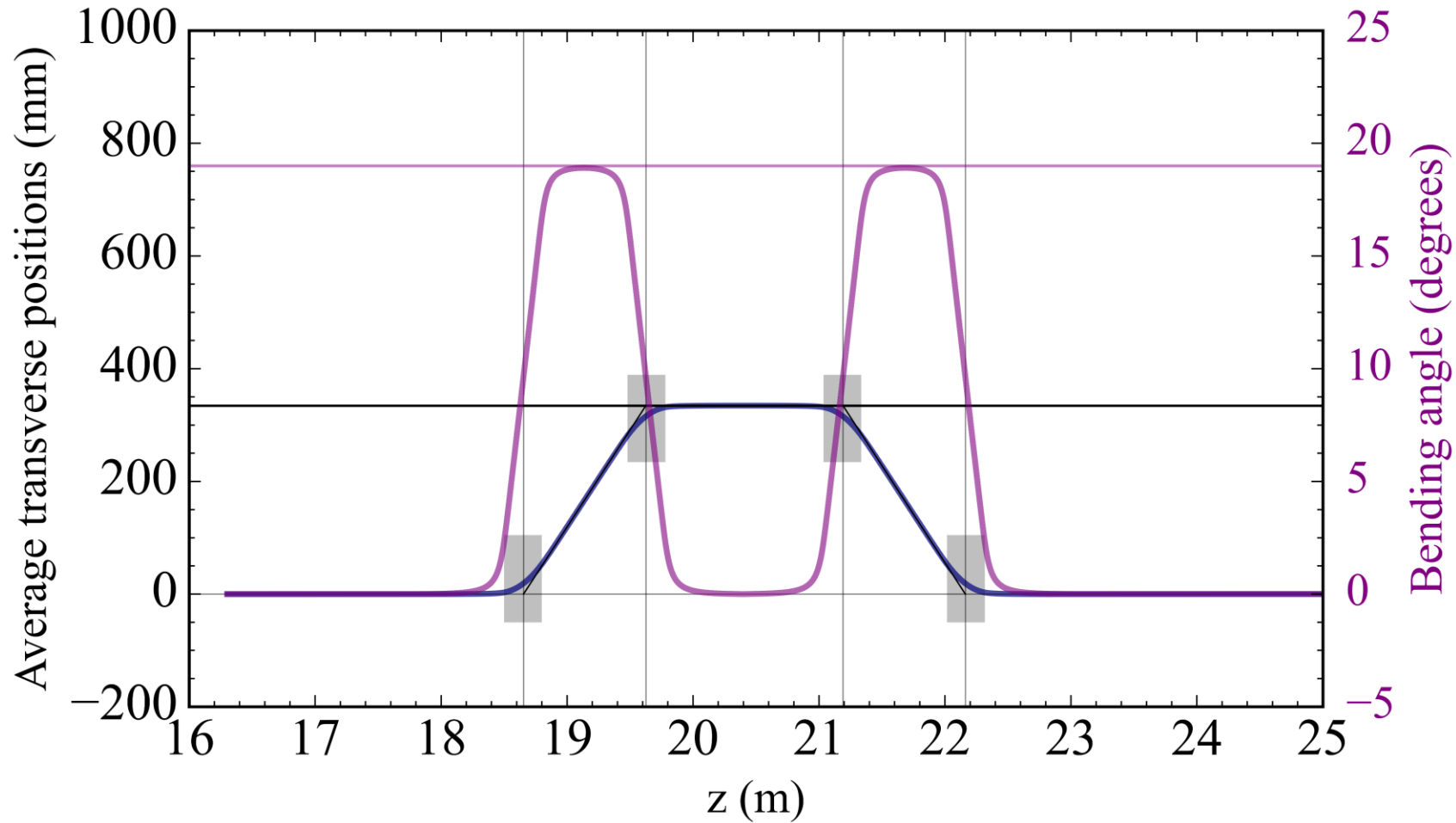


After BC



# Beam trajectory simulations

2D scan current with the condition  $D1 = D4$  and  $D2 = D3$



# Dispersion studies

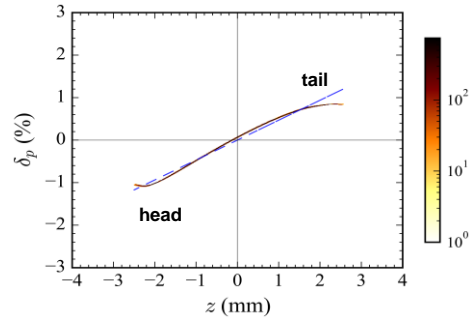


# Dispersion studies

## PITZ magnetic bunch compressor

### Electron properties

- Positive chirp
- Energy spread < 1 %



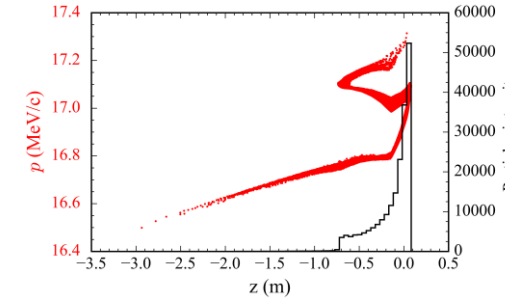
### Compression factor

$$C = (1 + h_i R_{56})^{-1}$$

Full-compression  $C \rightarrow \infty$

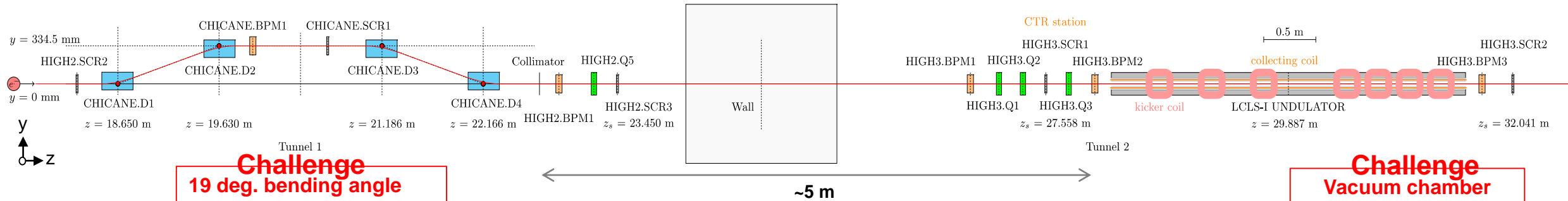
$$R_{56} = -\frac{1}{h_i} = -\frac{1}{slope}$$

Bunch charge 250 pC



### Peak currents

- Before : 53.066 A
- After : 265.148 A



**Challenge**  
19 deg. bending angle

**Challenge**  
Vacuum chamber  
size : 11 mm x 5 mm

### Objective beam parameters for electron beam transportation

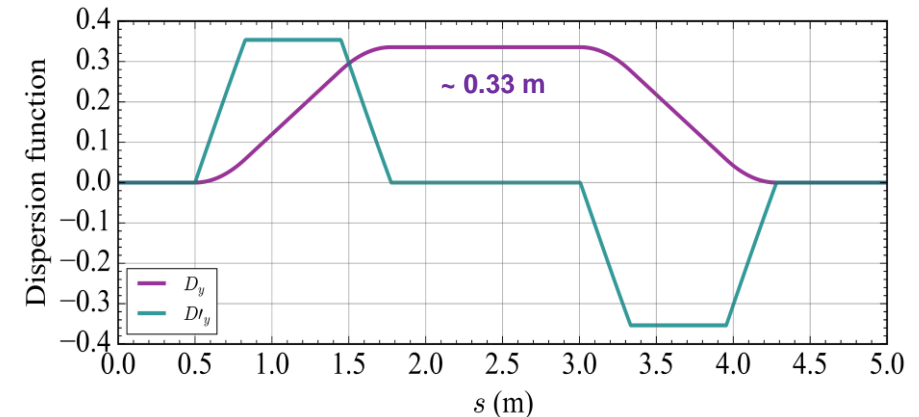
- Dispersion
  - Zero and constant dispersions after BC
  - Constant dispersions between D2 and D3
- On-axis trajectory
- Emittance !!!!!

Drift space between D1 and D2

$$D_2 = D_1 + \lambda D'_1$$

Bending angle

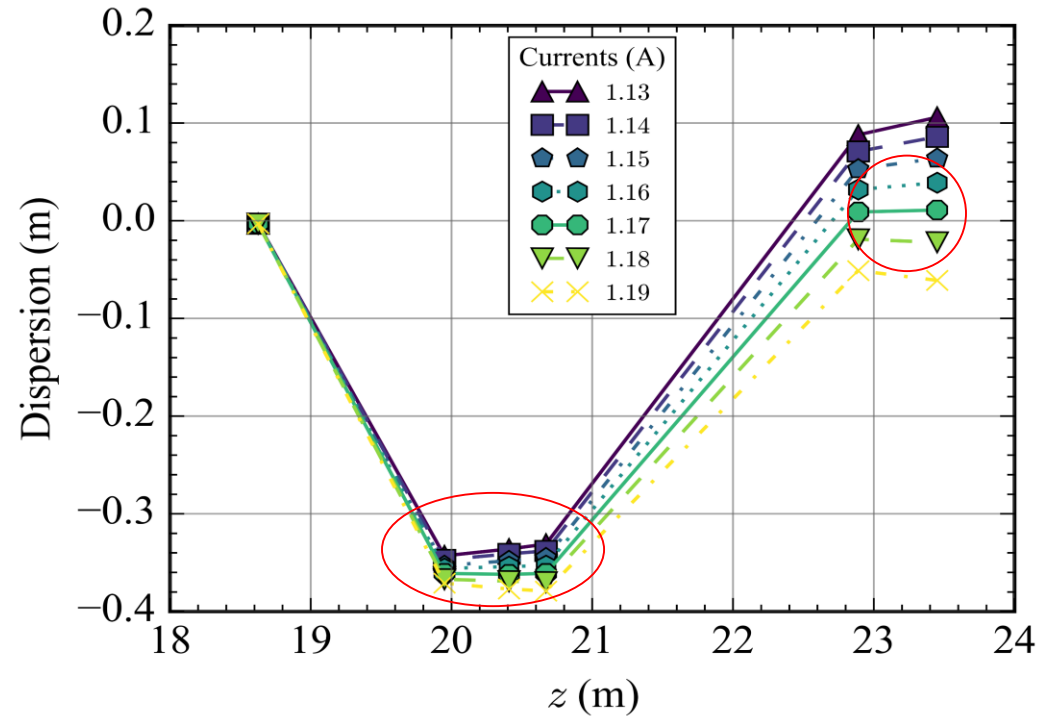
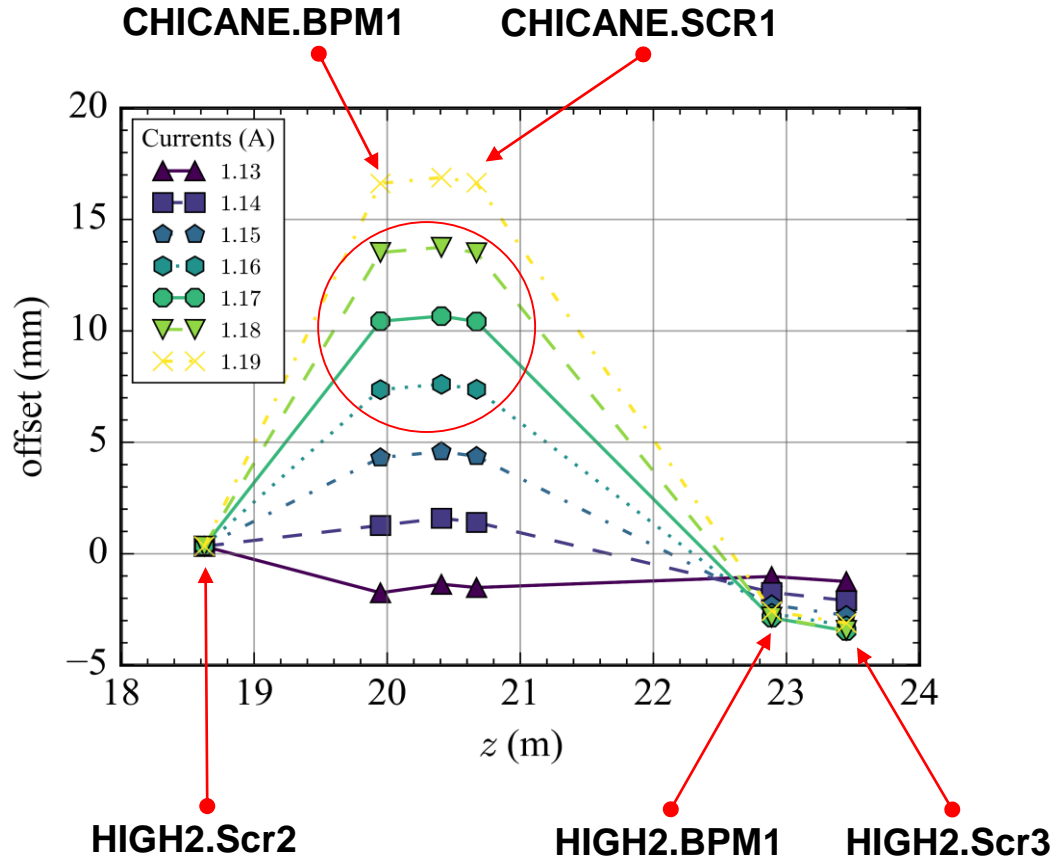
$$D'_1 = \sin(\theta)$$



# Dispersion studies

## Dispersion simulation for identical currents cases

$$D(z) = \frac{\langle x_{i,B}(z) \rangle - \langle x_{i,A}(z) \rangle}{\delta}$$



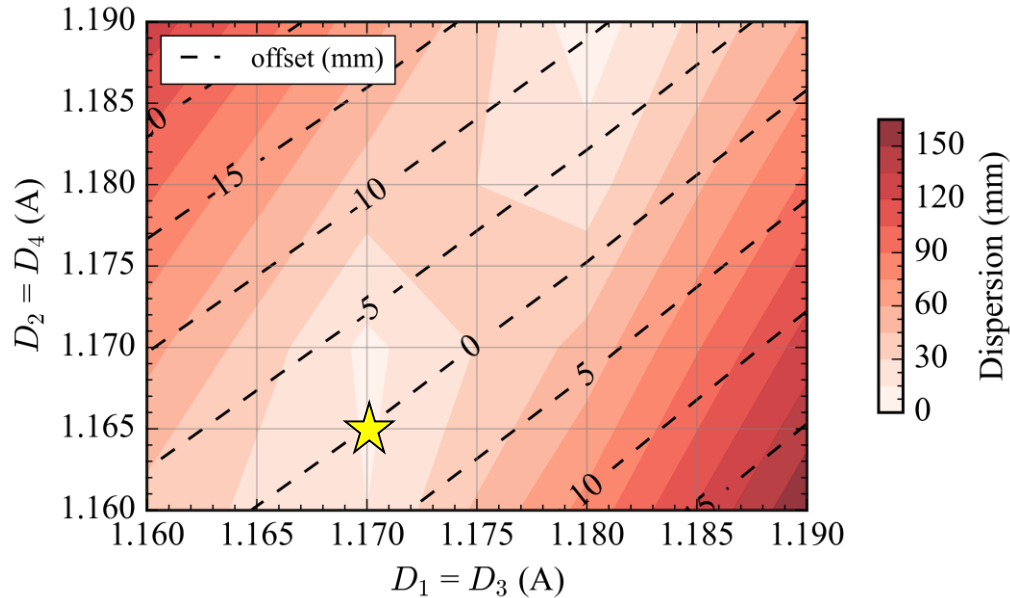
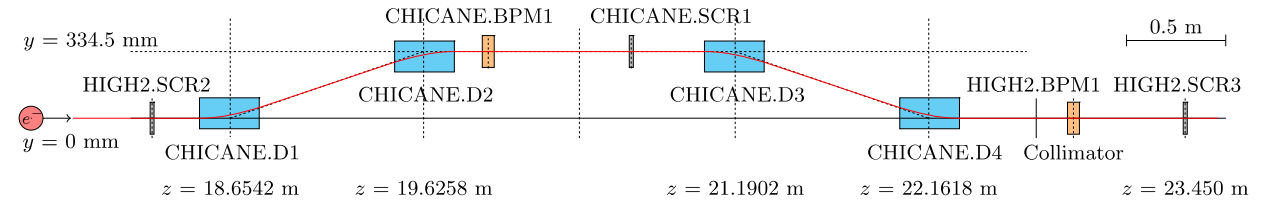
Zero dispersion after chicane → positive offset at chicane arm (between D2 and D3)

# Dispersion studies

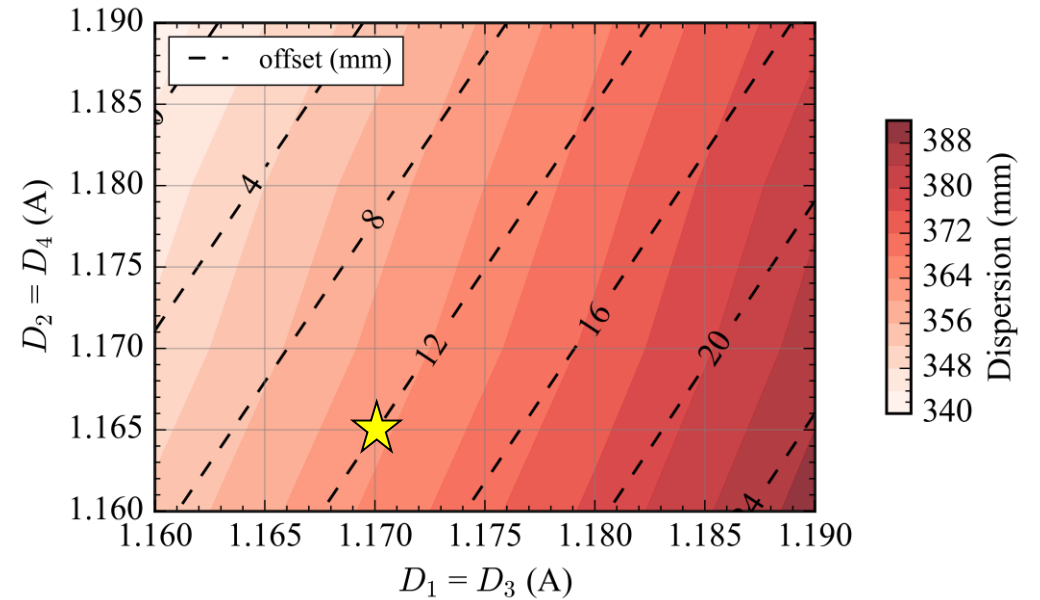
## Symmetric currents method

$D1 = D3, D2 = D4$

Beam pipe radius : 30 mm



**HIGH2.Scr3**

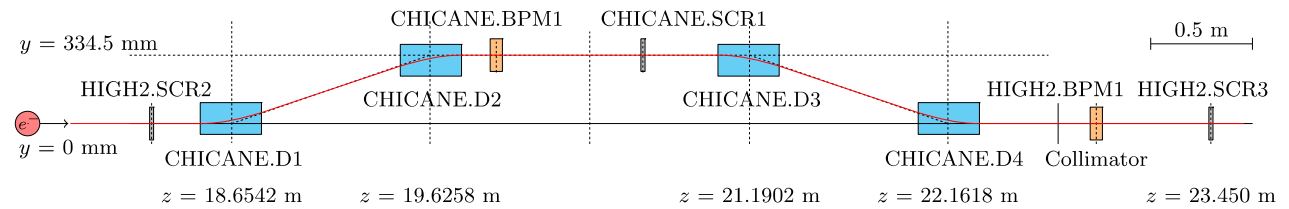
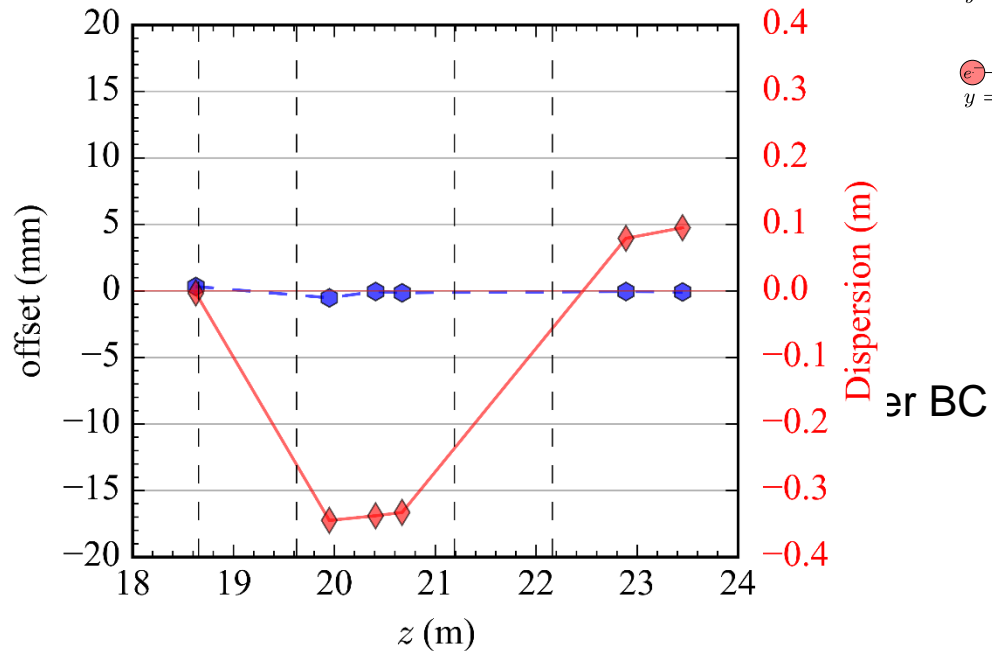


**CHICANE.SCR1**

- Zero dispersion after BC
- ~ 12 mm offset between D2 and D3

# Dispersion studies

## Independent currents method



Vertical offset between D2 and D3  $\leq 10$  mm

Dispersion at HIGH2.SCR3  $\leq 0.02$  m

Vertical angle at HIGH2.SCR3  $\leq 0.5$  mrad

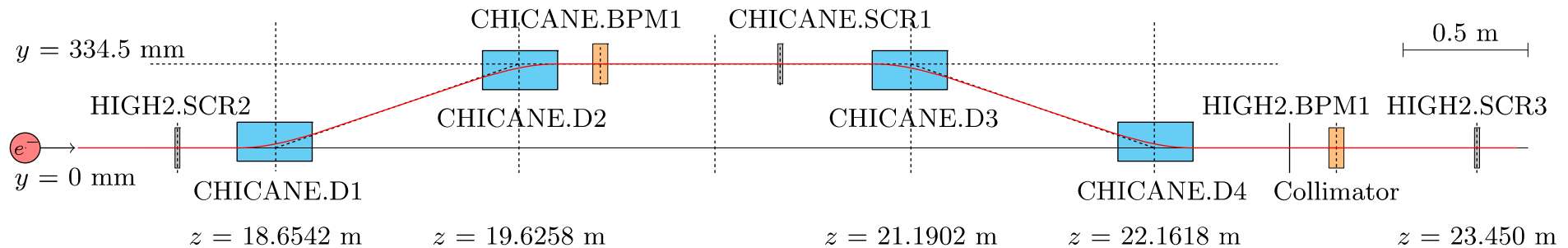
Offset at HIGH2.Scr3  $\leq 1$  mm

Screen	Position(m)	D1(A)	D2(A)	D3(A)	D4(A)	Offset (mm)	Dispersion (m)
Chicane.BPM1	19.950	1.163	1.159	1.163	1.163	8.663	0.358
Center D2 and D3	20.408					9.431	0.358
Chicane.Scr1	20.671					9.500	0.356
HIGH2.BPM1	22.889					0.990	0.020
HIGH2.Scr3	23.450					0.951	0.020

# Dispersion studies

## Dispersion measurements

- Beam momentum:  $\sim 17$  MeV/c
- Bunch charge : 250 pC



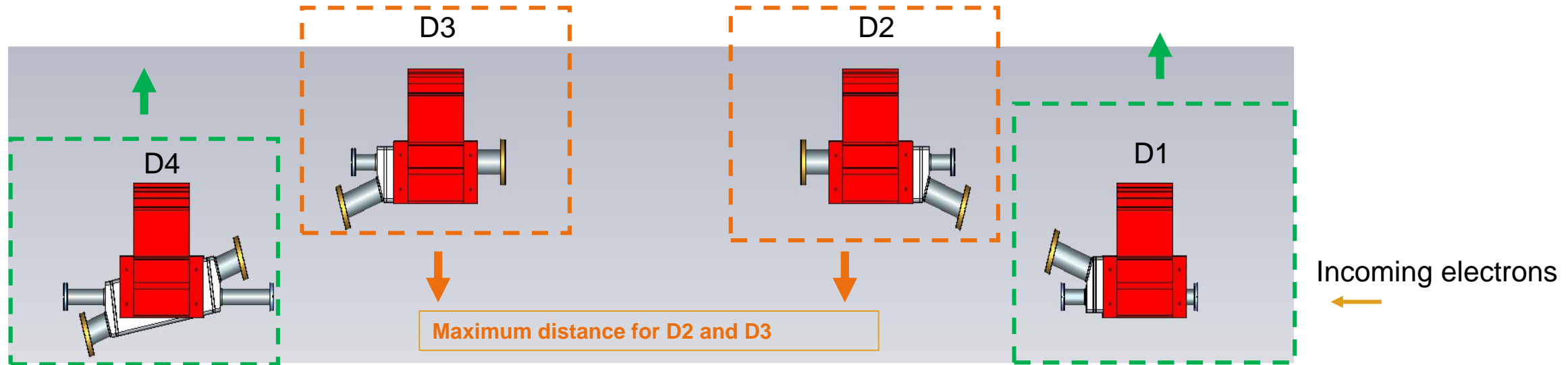
Measurement parameters	Symmetric currents method (D1 = -D3, -D2 = D4)	Independent currents method (Fixed offset, scan D3 and D4 tuning)
Dispersion after chicane	$\sim 0.00$ m	$\sim 0.03$ m (minimum)
Beam angle after chicane	$\sim 7$ mrad	$\sim 1$ mrad
Beam offset chicane arm	$\sim 12$ mm	$\sim 8.5$ mm

# Moving BC dipoles

## For correcting dispersion

Move D2 and D3 **downward** → corrected dispersion and beam transverse offset between D2 and D3

Move D1 and D4 **upward** → corrected dispersion and **beam transverse offset** after D4



# Moving BC dipoles

## Independent currents method

Dispersion *before* moving dipole magnets in the vertical direction

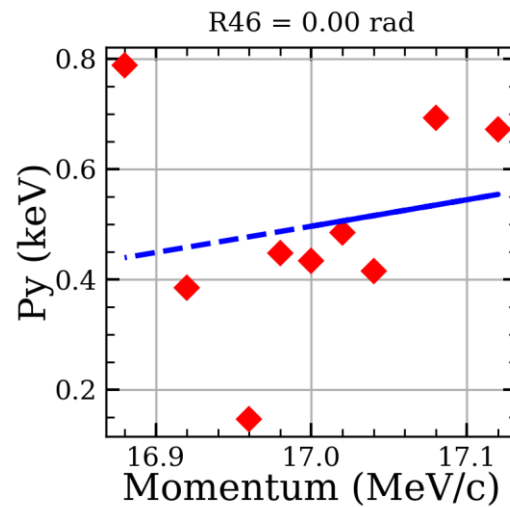
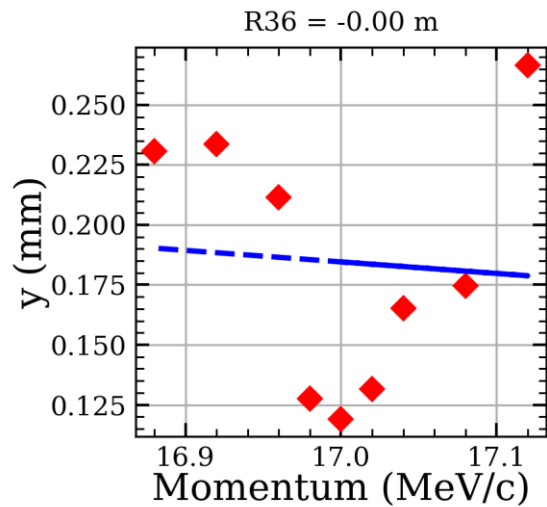
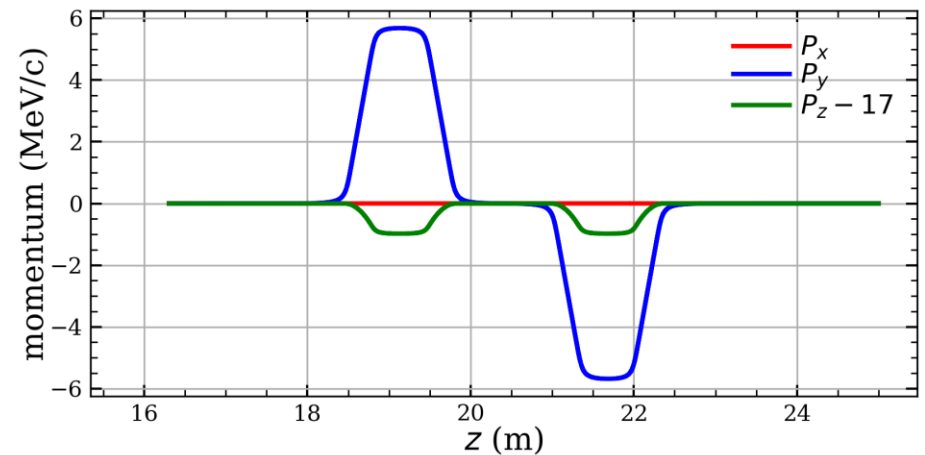
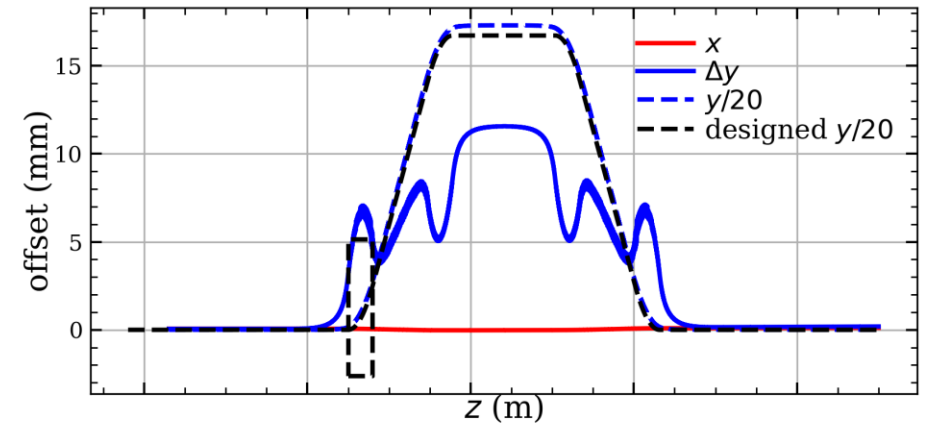
$$D1 = D4 = 0 \text{ mm}$$

$$D2 = D3 = 0 \text{ mm}$$

Using method  $D1 = D4$  and  $D2 = D3$

$$D1, D2, D3, D4 = [-1.1714, 1.1693, 1.1693, -1.1714] \text{ A}$$

Courtesy X.-K. Li



# Moving BC dipoles

## Independent currents method

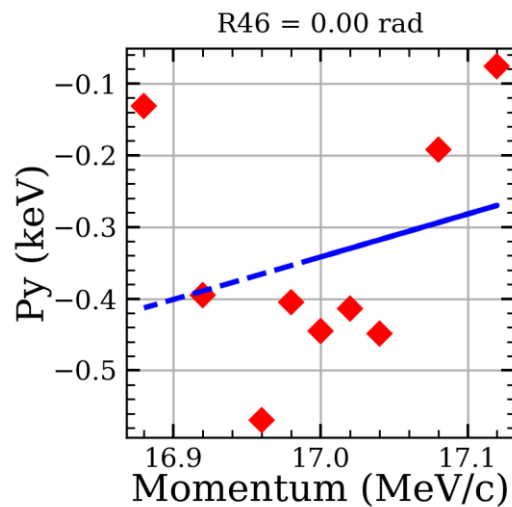
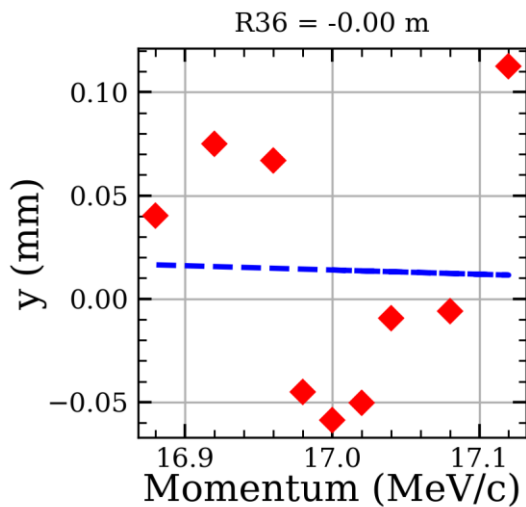
Dispersion *after* moving dipole magnets in the vertical direction

$$D1 = D4 = +6 \text{ mm}$$

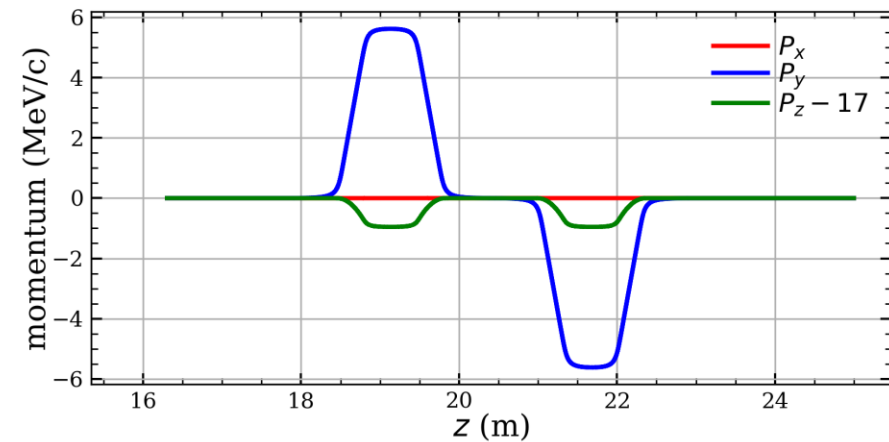
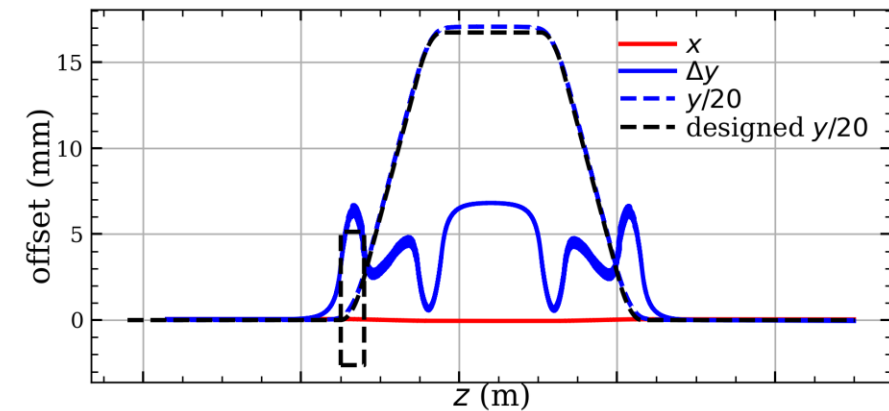
$$D2 = D3 = -3.5 \text{ mm}$$

Using method  $D1 = D4$  and  $D2 = D3$

$$D1, D2, D3, D4 = [-1.1560, 1.1552, 1.1552, -1.1560]$$



Courtesy X.-K. Li





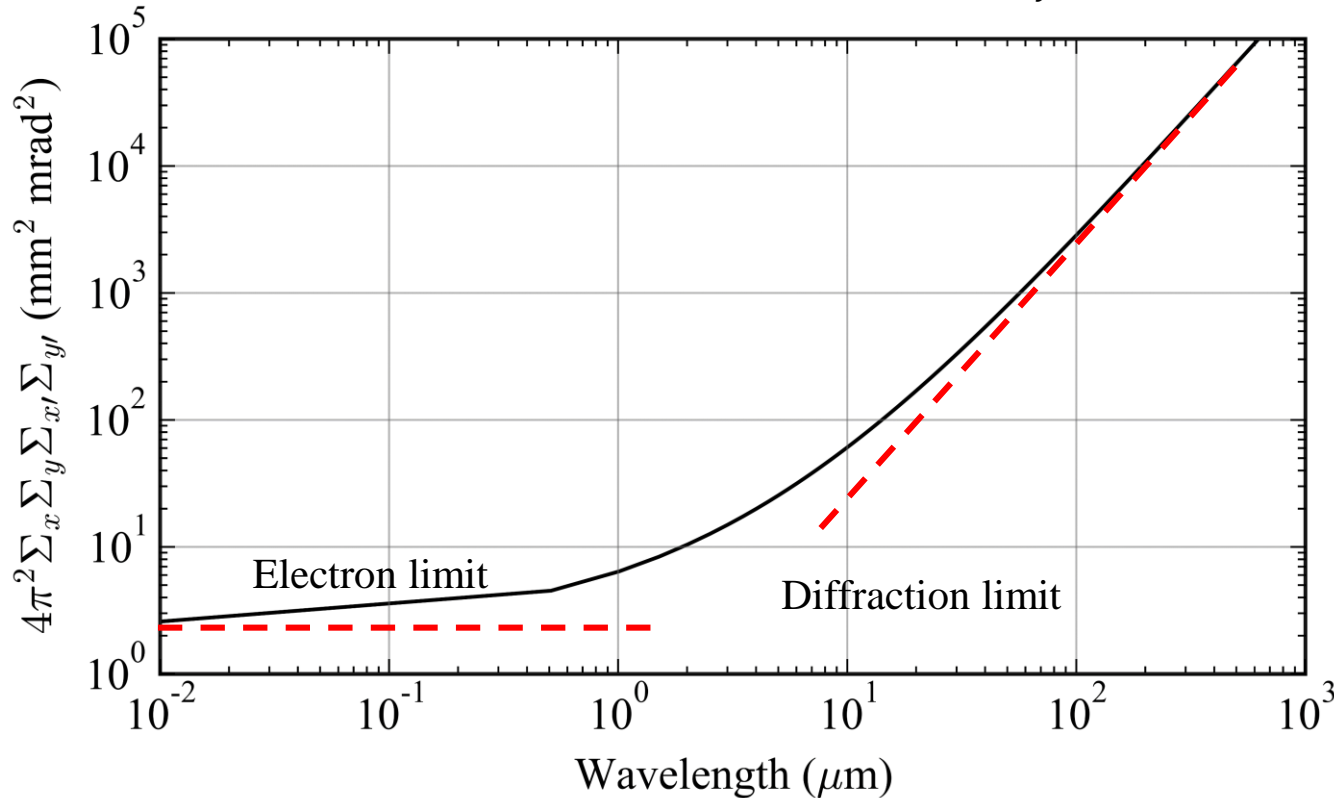
# Beam matching

# Beam matching

## Diffraction limit

$$\mathfrak{B} = \frac{\dot{N}_{ph}}{4\pi^2 \Sigma_x \Sigma_y \Sigma_{x'} \Sigma_{y'} \frac{d\omega}{\omega}}$$

Phase space volume  $\rightarrow 4\pi^2 \Sigma_x \Sigma_y \Sigma_{x'} \Sigma_{y'}$



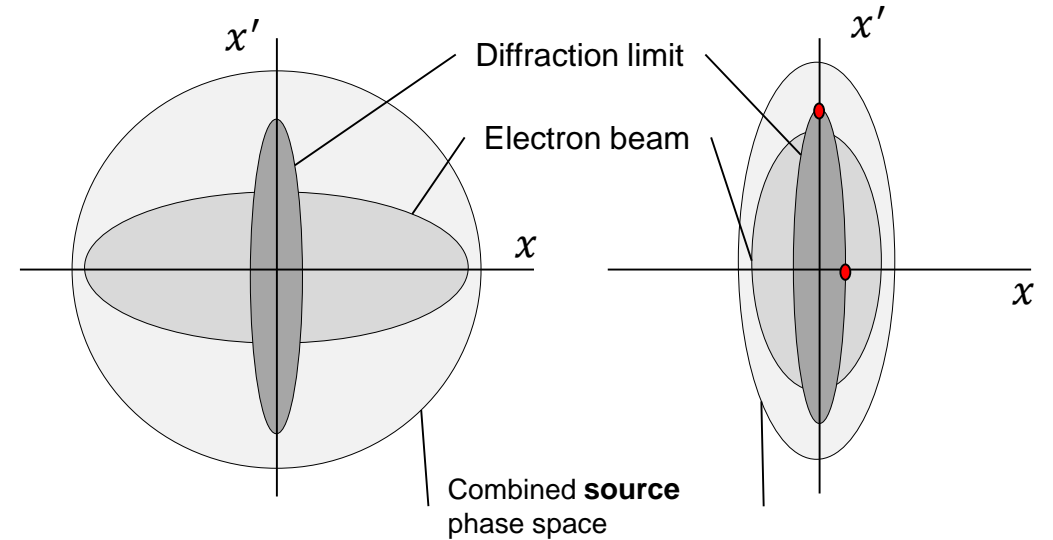
!!! No advantage to gain when  $\sigma_r \gg \sigma_{x,y}$  and  $\sigma_{r'} \gg \sigma_{x',y'}$

E.g., matching condition for **LCLS-I** undulator at **PITZ**

$$\sigma_{b,x} = 0.65 \text{ mm}, \sigma_{b,y} = 0.25 \text{ mm}$$

$$\sigma'_{b,x} = 0.33 \text{ mrad}, \sigma'_{b,y} = 1.20 \text{ mrad}$$

Undulator length ( $L$ ) = 3.4 m Radiation wavelength ( $\lambda$ ) = 100  $\mu\text{m}$



Beam emittance much be smaller than the diffraction limit

$$\epsilon_{x,y} \leq \frac{\lambda}{4\pi}$$

It is easier to achieve this condition for long wavelength

# Beam matching

## Finding optimum “beta”

$$\lambda_r = 100 \mu\text{m} \quad \text{THz}$$

$$\epsilon_{ph,x,y} = 8 \text{ mm.mrad}$$

(Diffraction limited emittance)

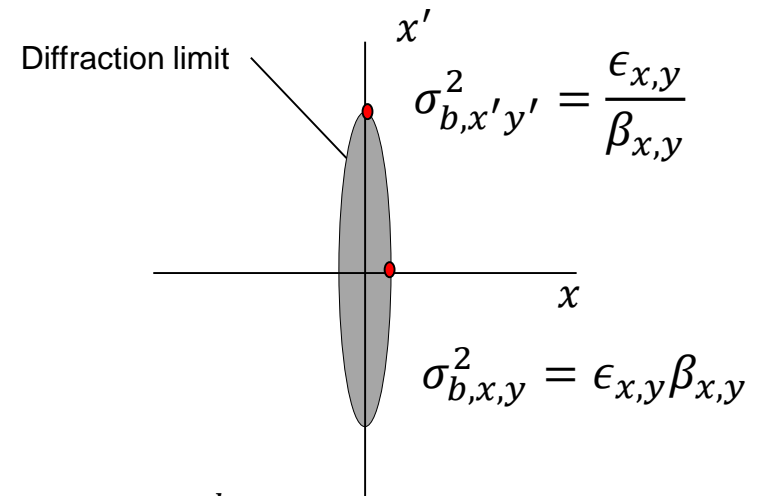
Finding the optimum focusing for optimum matching

$$\sigma_{b,x,y}^2 = \epsilon_{x,y} \beta_{x,y} \quad \text{and} \quad \sigma_{b,x'y'}^2 = \frac{\epsilon_{x,y}}{\beta_{x,y}}$$

After including **diffraction limit**

$$\sigma_{tot,x} \sigma_{tot,x'} = \sqrt{\epsilon_x \beta_x + \sigma_r^2} \sqrt{\frac{\epsilon_x}{\beta_x} + \sigma_{r'}^2}$$

Betatron function at the **source point**



Minimum at  $(\frac{d}{\beta_x} \sigma_{tot,x} \sigma_{tot,x'} = 0)$

$$\beta_x = \frac{\sigma_r}{\sigma_{r'}} = \frac{L}{4\pi} \rightarrow 0.27 \text{ m}$$

**LCLS-I** undulator length ( $L$ ) = 3.4 m

Similarly for y 
$$\beta_y = \frac{\sigma_r}{\sigma_{r'}} = \frac{L}{4\pi} \rightarrow 0.27 \text{ m}$$

# Beam matching

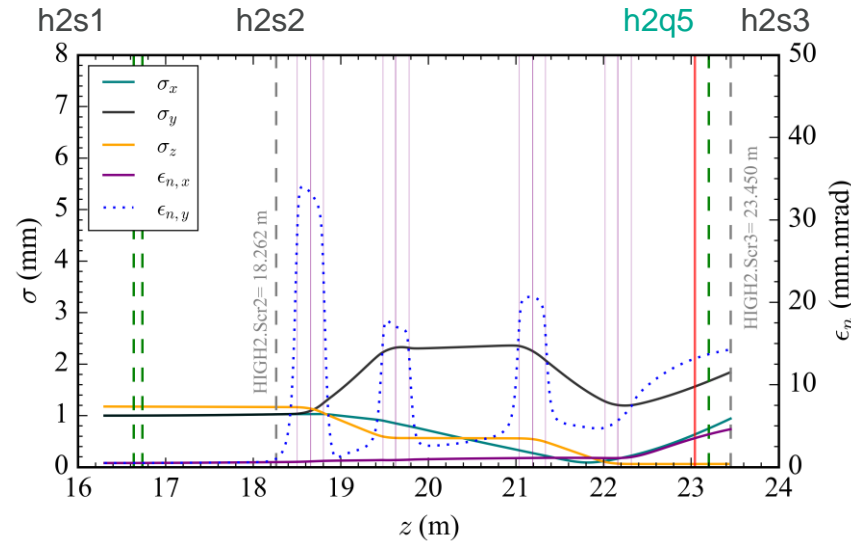
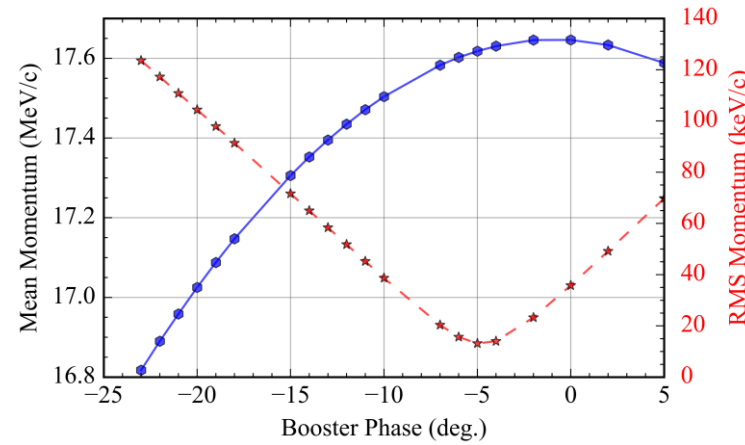
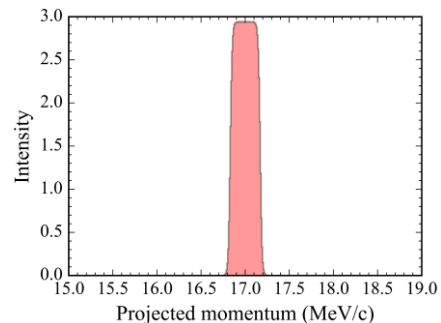
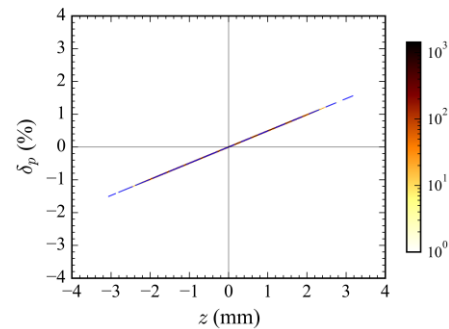
## Beam transportation

Beam momentum 17 MeV/c

Beam with **chirp**

Energy spread 0.6%

Bunch charge 250 pC

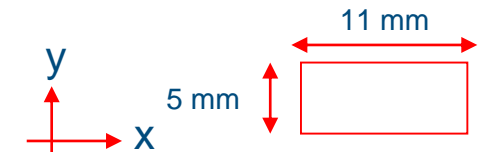


### Matching parameters (transverse phase space)

- Twiss-parameters :  $\beta_x, \beta_y, \alpha_x, \alpha_y$
- Transverse beam emittance :  $\epsilon_x, \epsilon_y$

### Challenges

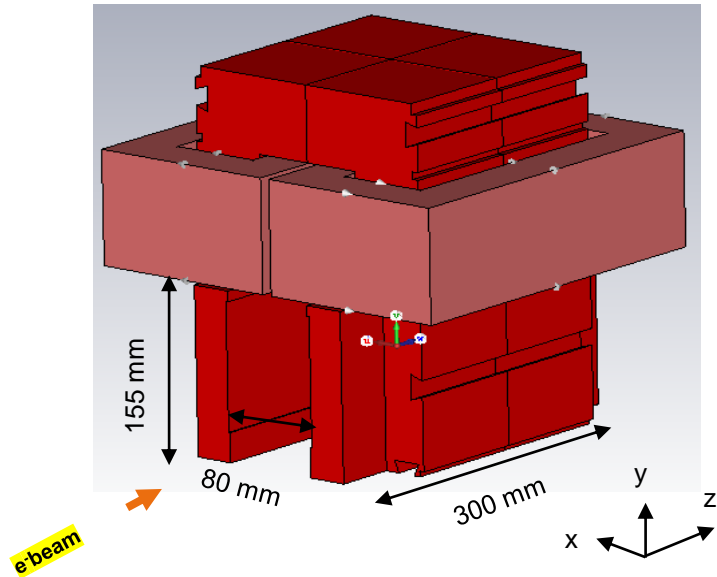
- Only one quadrupole to focus beam after BC
- Increasing of the transverse emittance (vertical) after BC
- Strong space charge force field due to low energy electron beam, compressed beam, and high bunch charge (up to 1.5 nC for SASE)
- Match beam to small vertical pipe of an undulator magnet



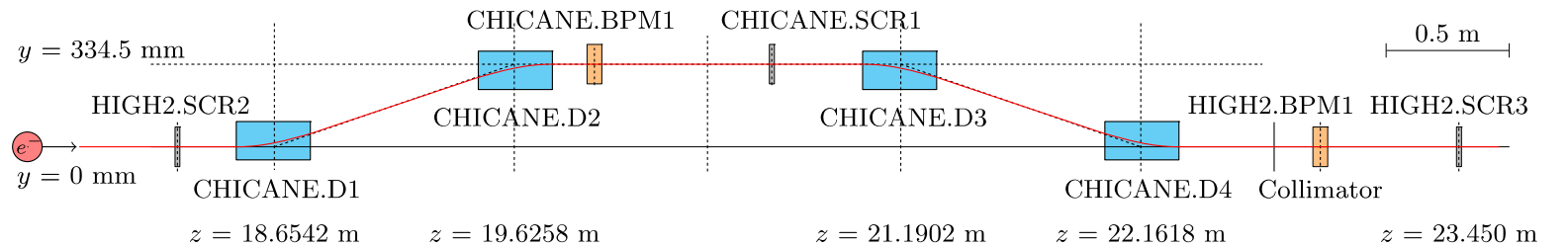
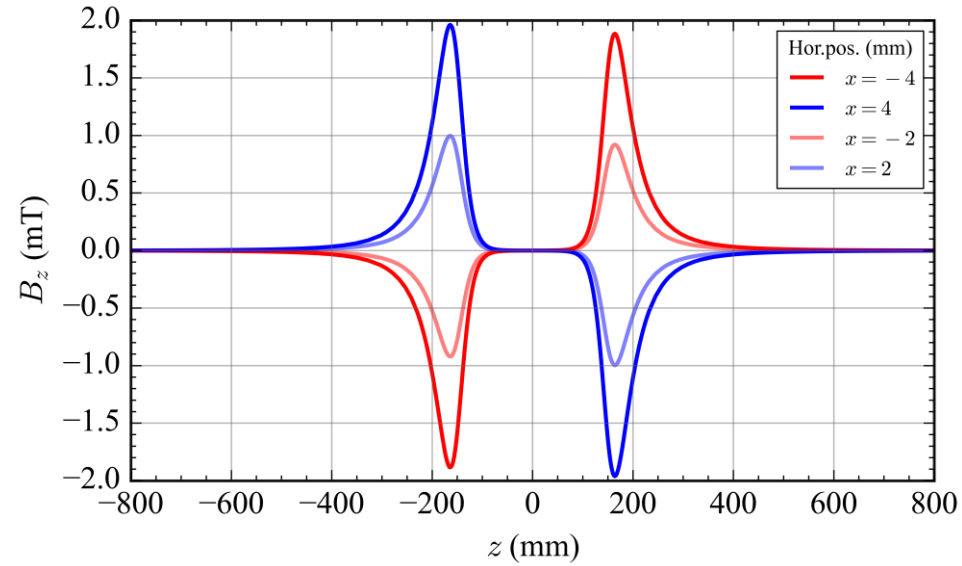
Undulator chamber cross-section

# Beam matching

## Edge focusing effect



19 degrees  
bending angle  
+  
Rectangular  
Bending magnet

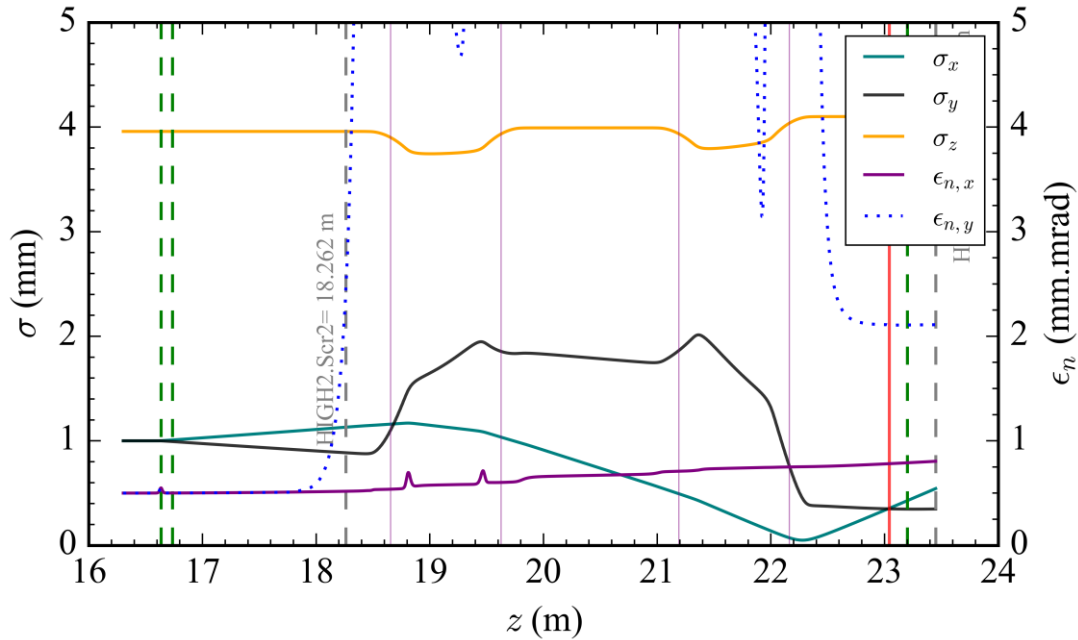


# Beam matching

## Edge focusing effect

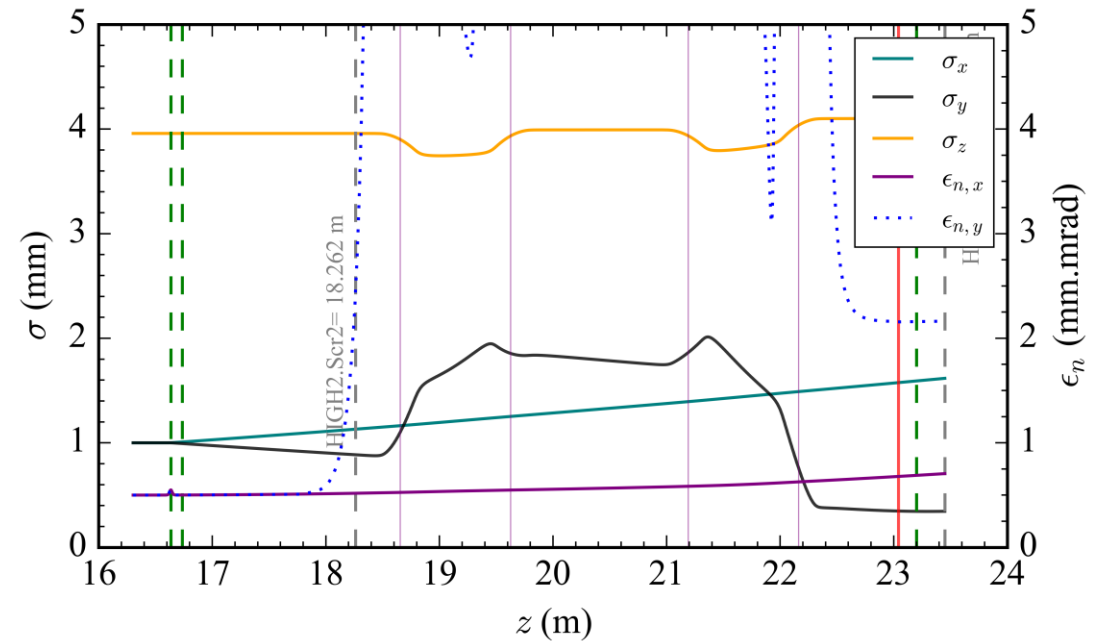
Magnetic field only Bx → '3DBNKF25X'

Before move dipole D2 and D3, h2Q1 focusing in y by 0.1 T/m



Bx, By, Bz

Before move dipole D2 and D3, h2Q1 focusing in y by 0.1 T/m

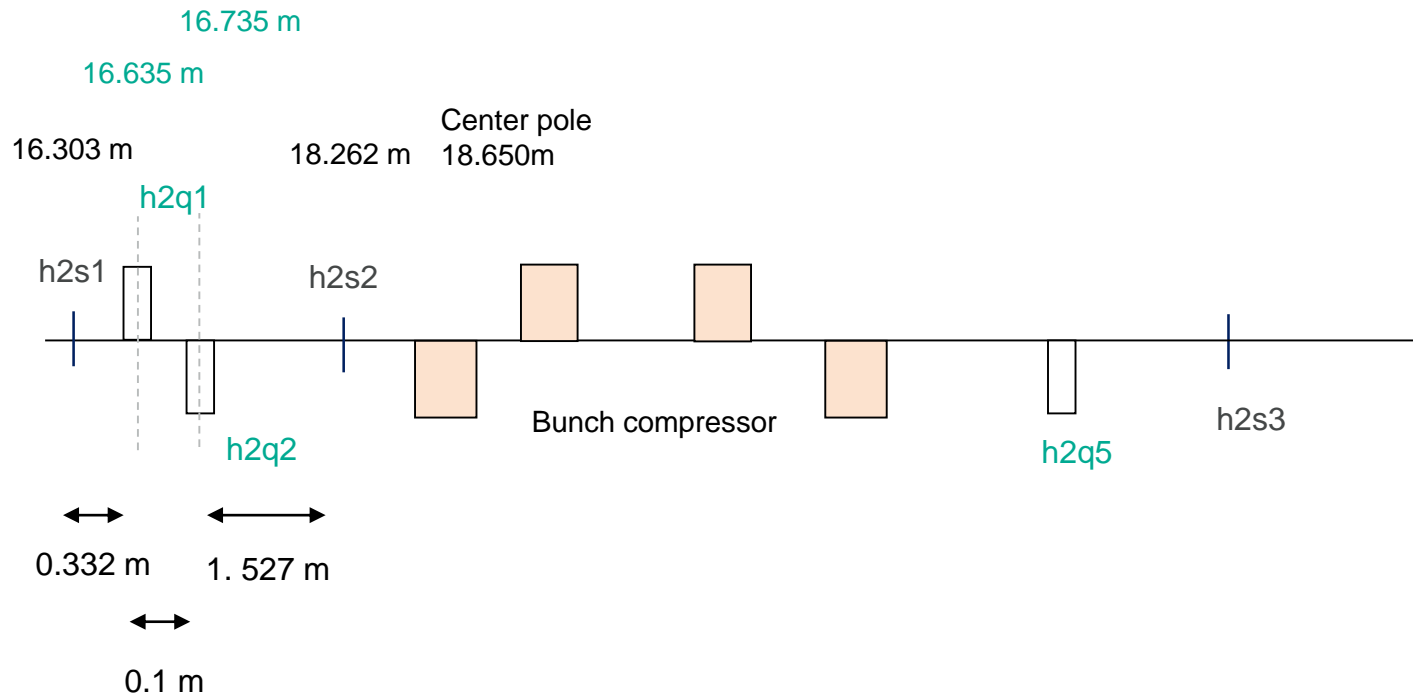


Bx only

# Beam matching

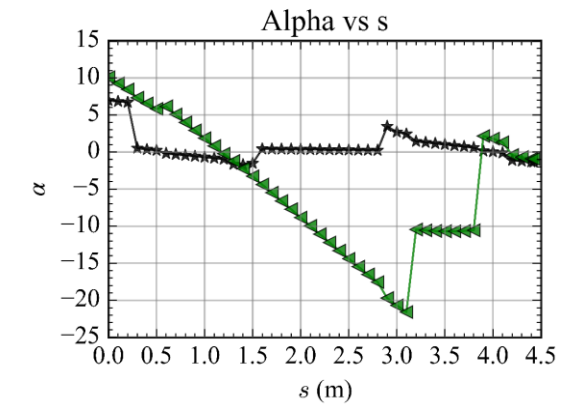
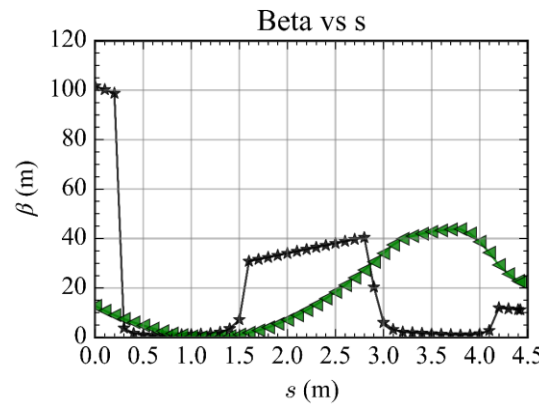
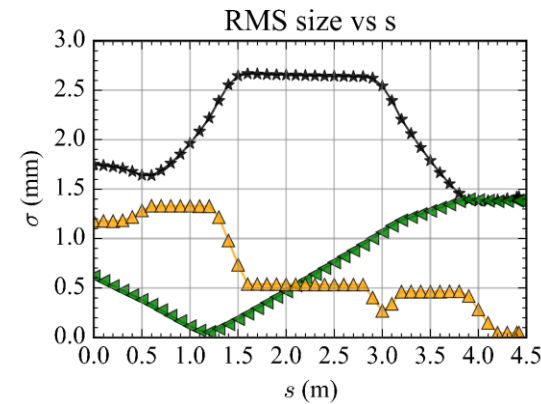
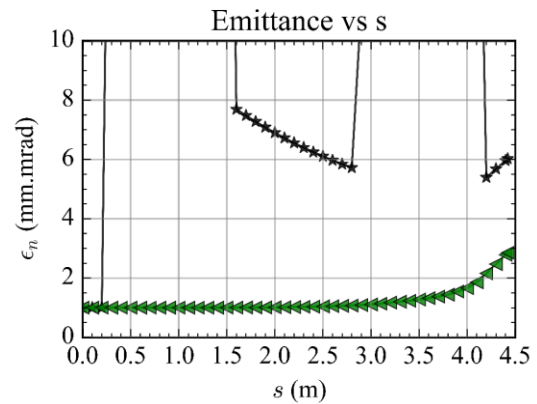
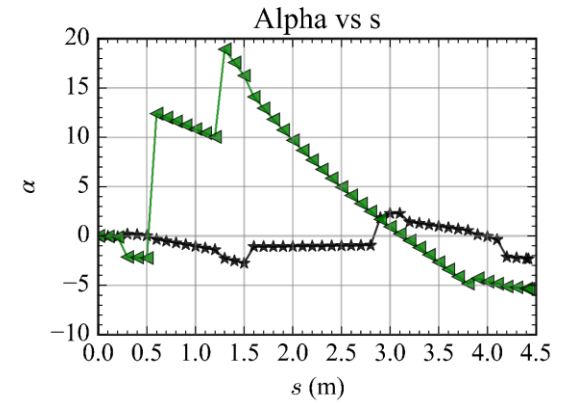
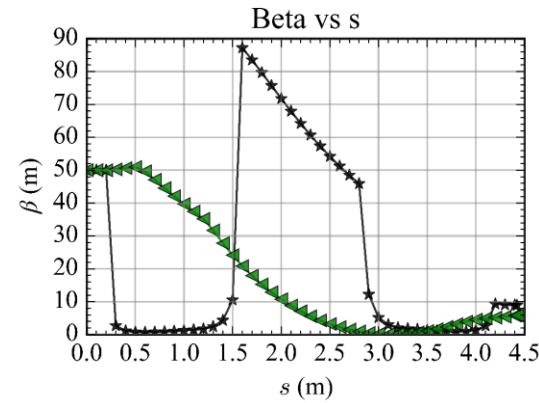
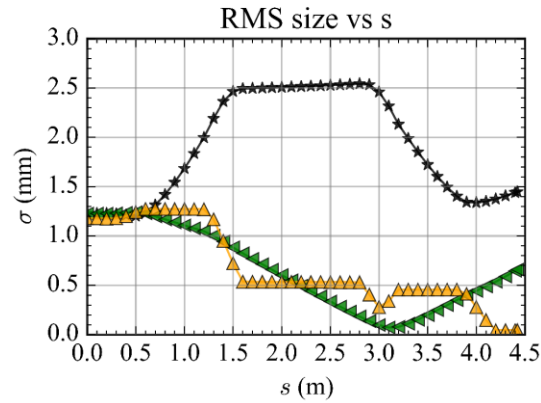
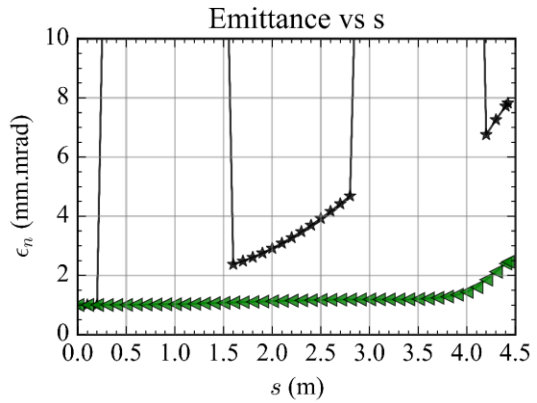
## Setup BC (Chicane) → beam dynamics

- Average beam momentum : 17 MeV/c
- Bunch charge : 50 pC, **250 pC**, 1.5 nC
- MMMG phase and ~ -20 deg. w.r.t. MMMG phase



# Beam matching

## Beam dynamics simulation using OCELOT

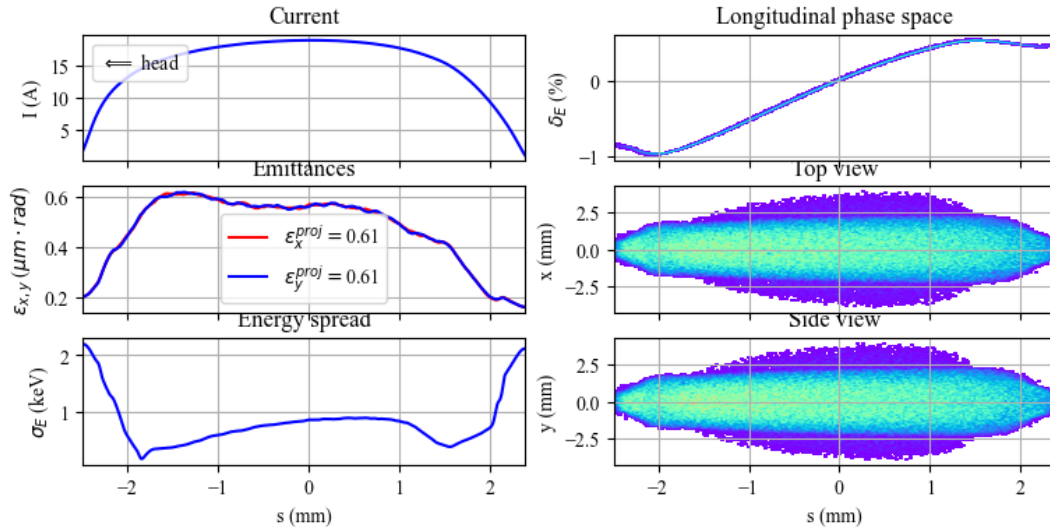




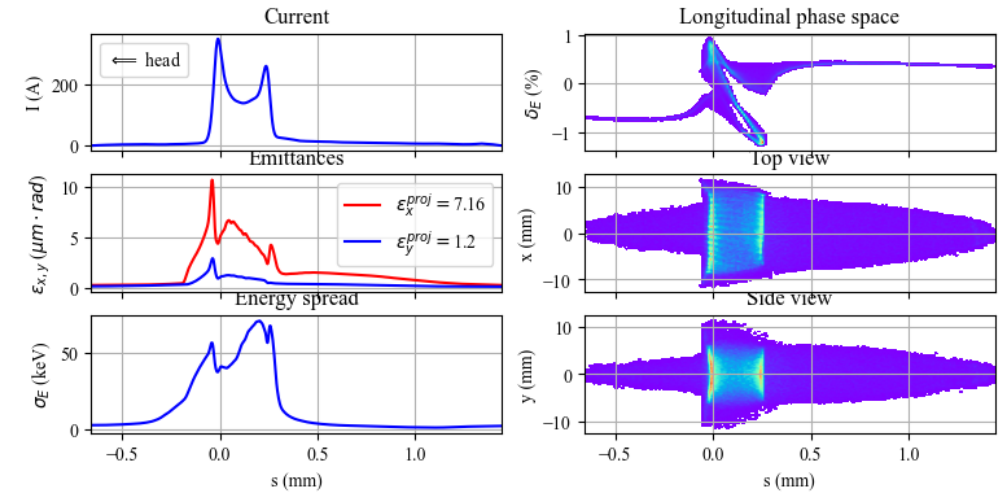
# Beam matching

## Beam from photocathode

Before BC at HIGH2.Scr2



After compression from BC



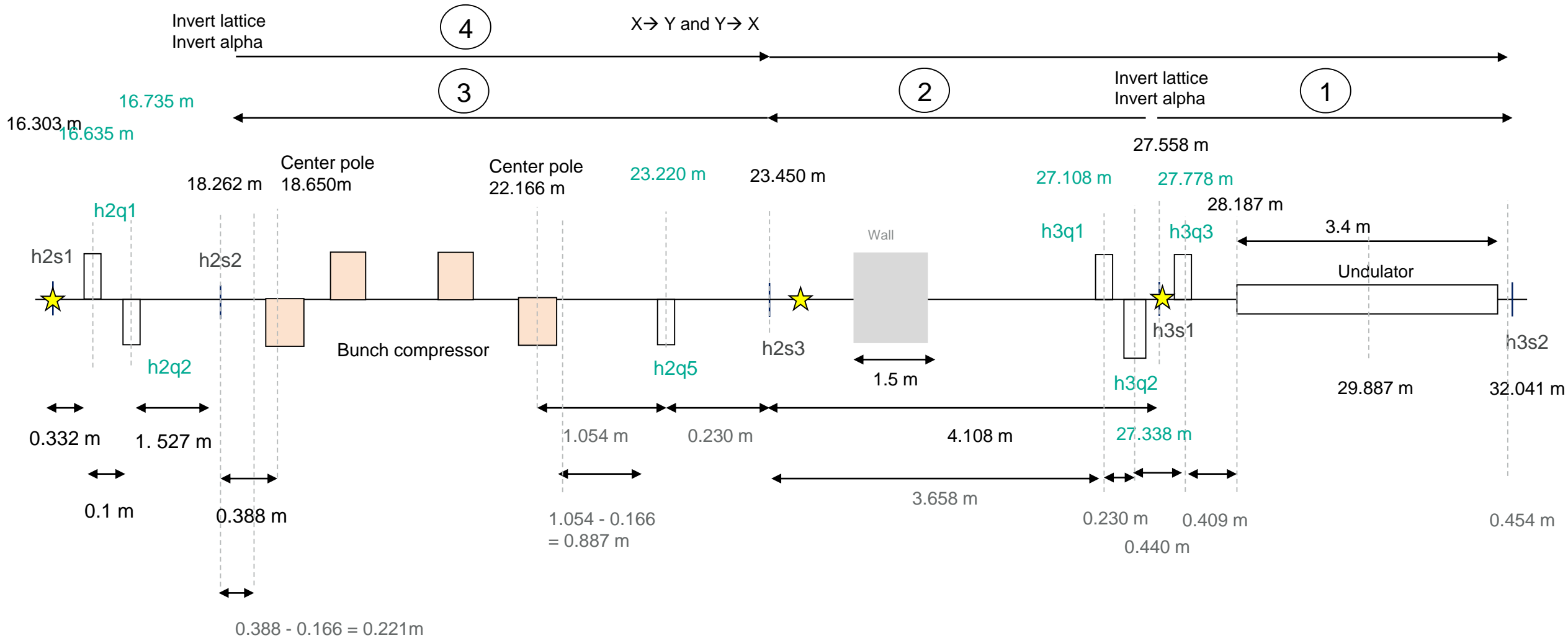
6-D transportation matrix

$$\vec{\chi} = [x, x', y, y', z, \Delta p/p_0]^T$$

- Average beam momentum : 17 MeV/c
- Bunch charge : **250 pC**
- ~ -20 deg. w.r.t. MMMG phase

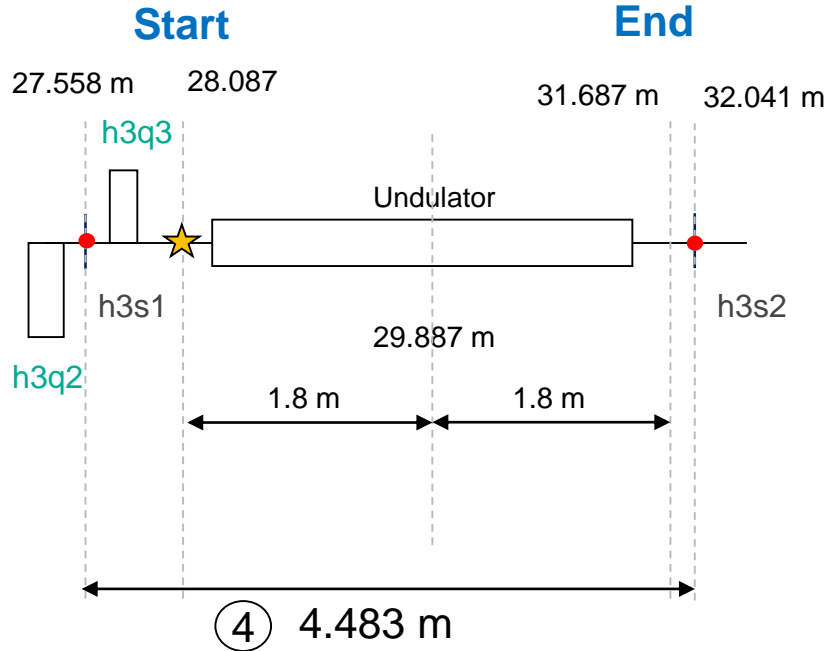
# Beam matching

## Motivation, Initial beam setup



# Beam matching

## Finding Twiss-parameters before undulator magnet



### Simulation setup

- Using ASTRA + 3D magnetic field of undulator magnet
- Optimized parameters
- Beam momentum 17 MeV/c, Bunch charge 250 pC
  - Transverse beam size  $F_x = |\sigma_{xf} - \sigma_{xi}| \rightarrow 0$   $F_y = |\sigma_{yf} - \sigma_{yi}| \rightarrow 0$
  - Correlation

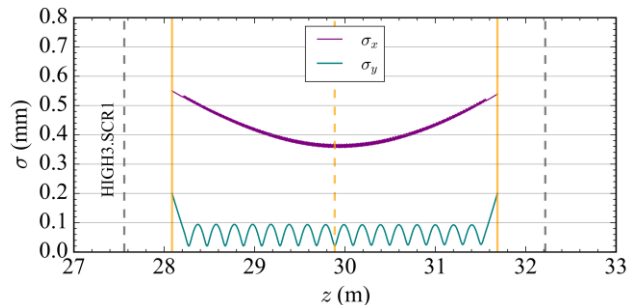
$$\sigma_x^2 = \frac{\beta_x \epsilon_{n,x}}{\beta \gamma}$$

$$cor_{px} = -\frac{\alpha_x}{\beta_x [m]} \sigma_x [mm]$$

Fixed transverse emittance !

Norm. emit\_x, Norm. emit\_y = 1, 1 mm.mrad

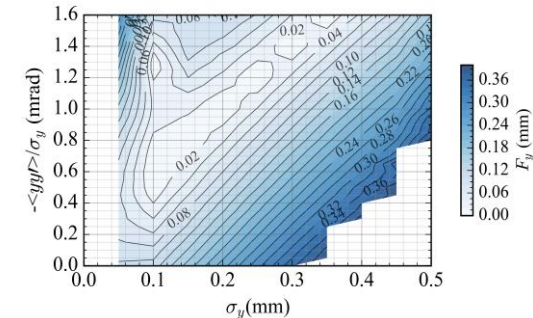
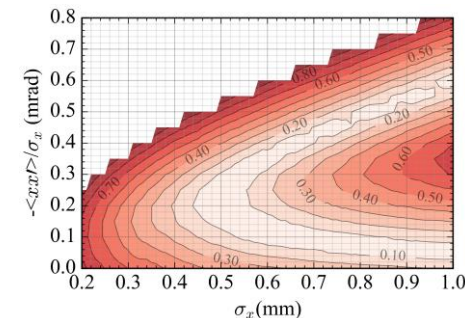
xrms, yrms, corpx, corpy = 0.55, **0.20**, 0.18, **1.0**



- Xemit = Yemit = 1 um
- Std\_x = 0.55 mm
- Std\_y = 0.15 mm
- Xx'/std\_x = 0.25 mrad
- Yy'/std\_y = 0.8 mrad

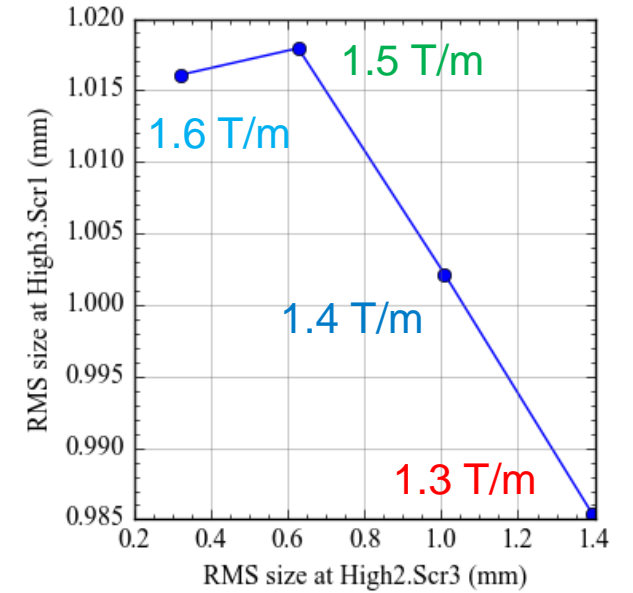
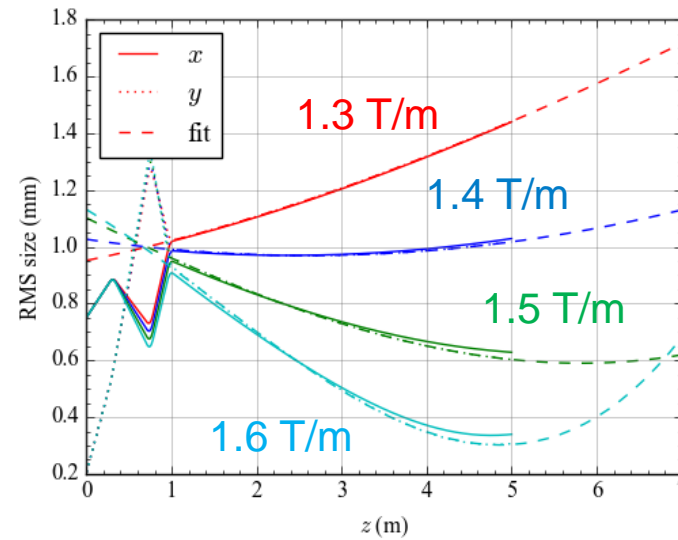
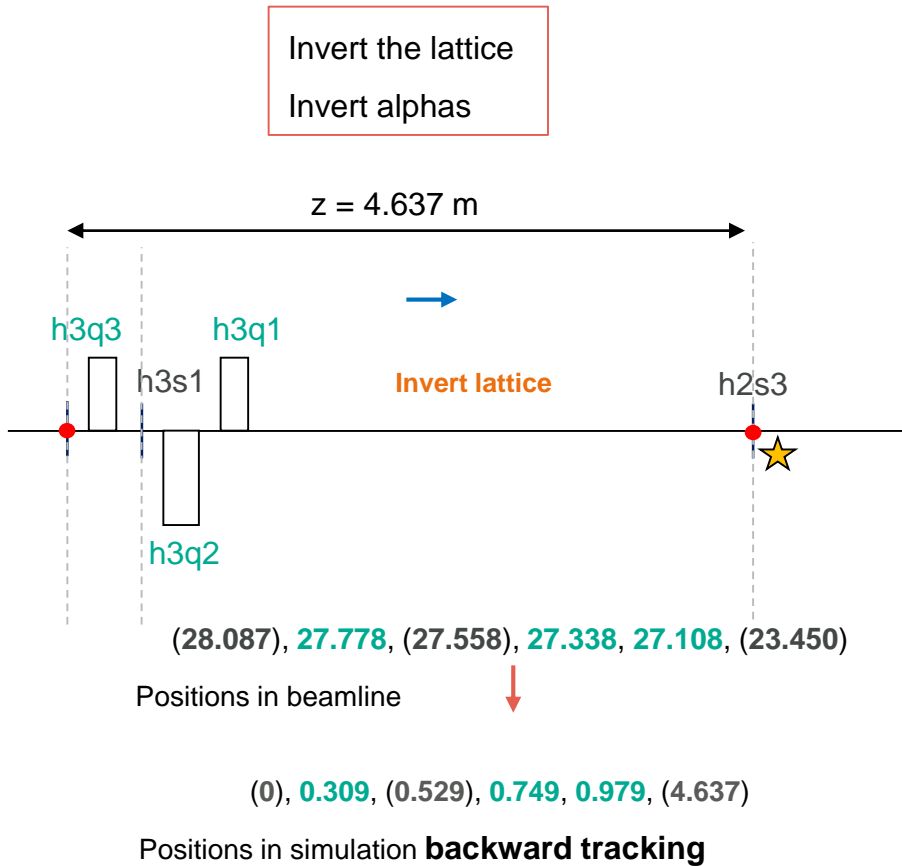


- Beta\_x = 10 m
- Beta\_y = 0.75 m
- Alpha\_x = 4.6 → 6 m
- Alpha\_y = 4 m



# Beam matching

## Edge focusing effect

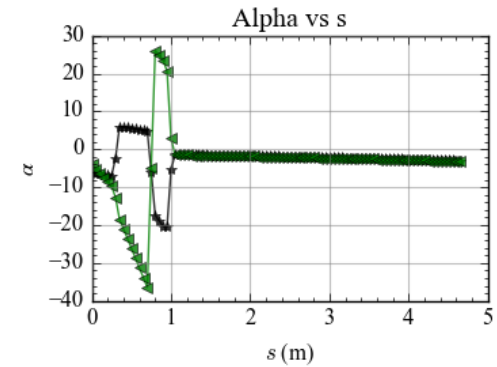
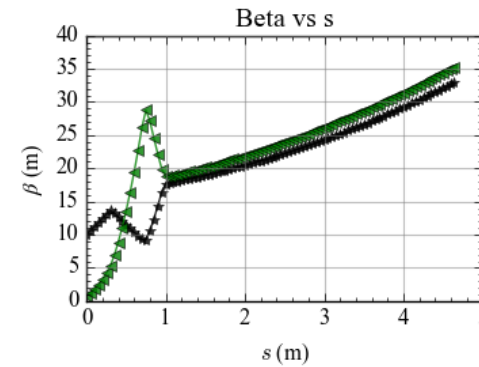
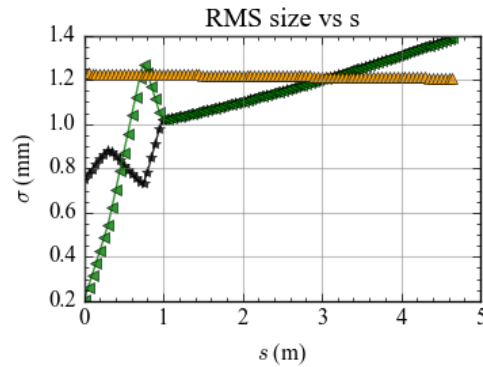
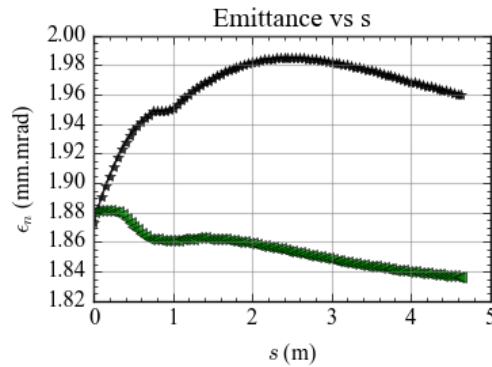


# Backward tracking using OCELOT

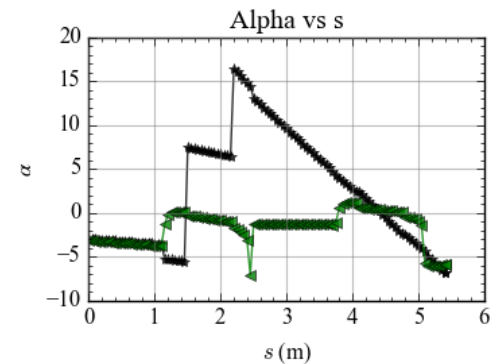
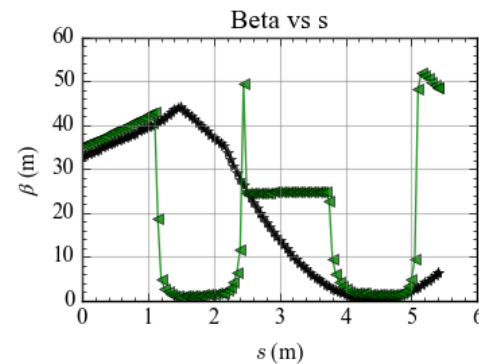
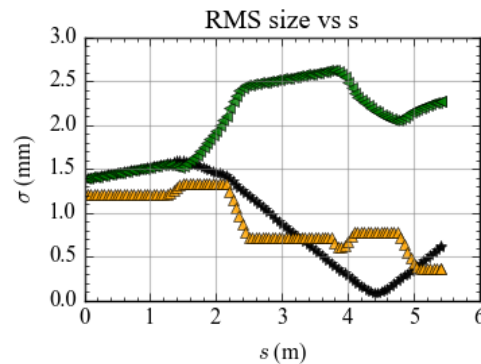
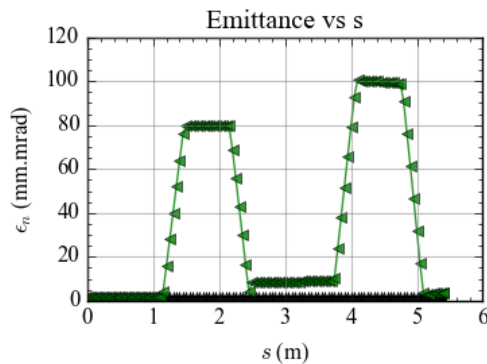
Tracking to the end off the BC, switch x and y axis and tracking further to BC entrance

1<sup>st</sup> Iteration, HIGH3.Q3 = 1.3 T/m

Green color → Vertical      Black color → Horizontal



X ← → Y

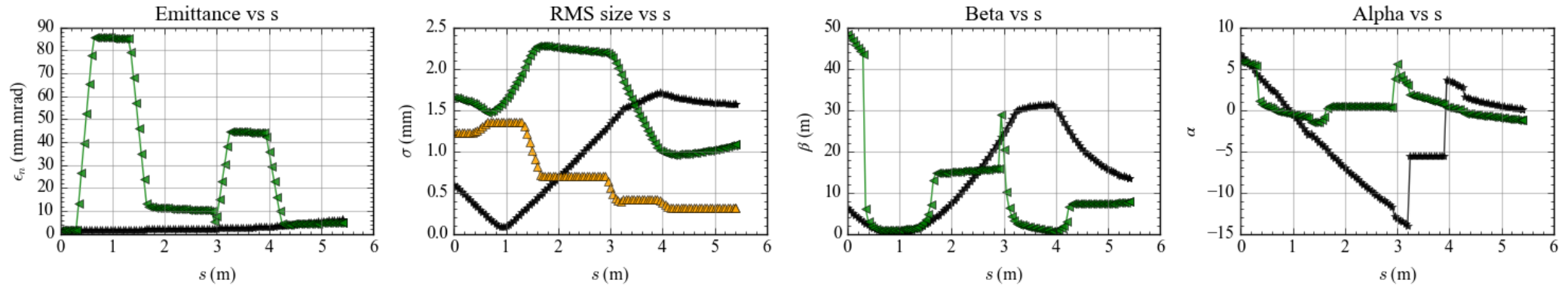


# Forward tracking using OCELOT

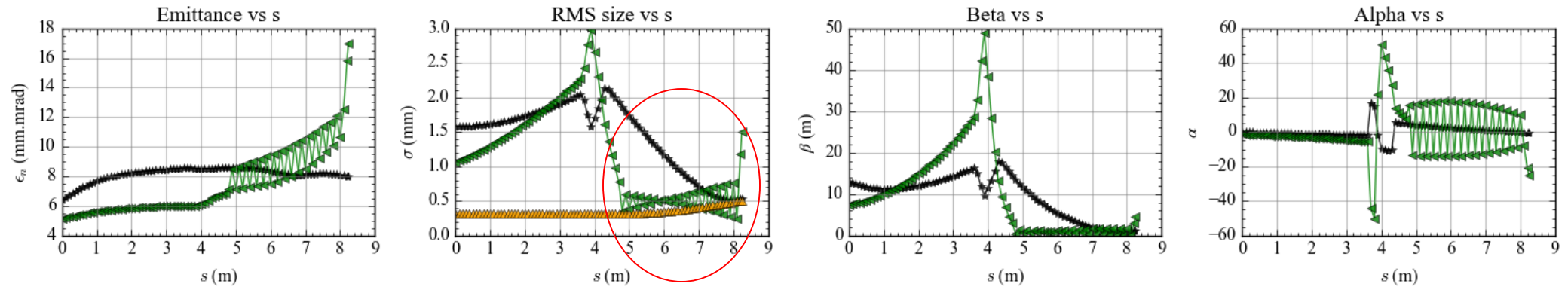
Invert alpha (twiss-parameter), tracking beam the end of the undulator magnet

1<sup>st</sup> Iteration, HIGH3.Q3 = 1.3 T/m

Green color → Vertical    Black color → Horizontal



X ↔ Y

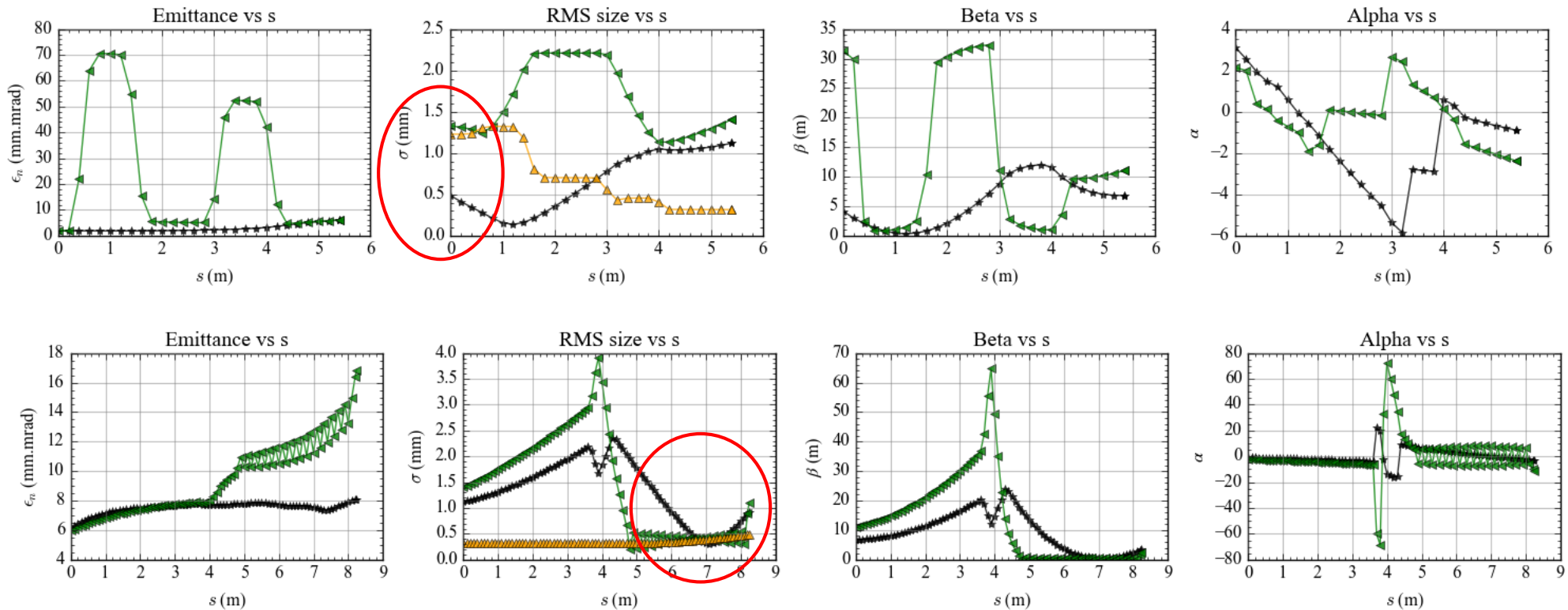


# 2<sup>nd</sup> Iteration

Forward tracking to the end of the undulator magnet (using beam from **S2E** simulation)

1<sup>st</sup> Iteration, HIGH3.Q3 = 1.3 T/m

2<sup>nd</sup> Iteration, HIGH3.Q3 = 1.5 T/m



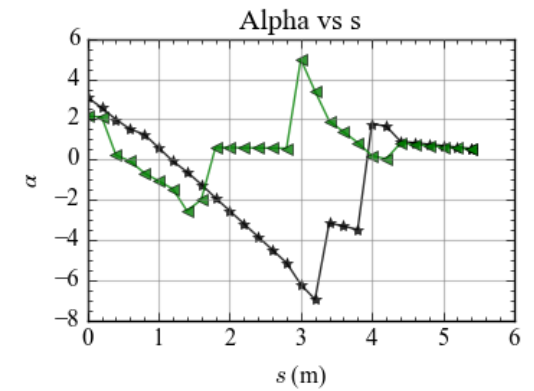
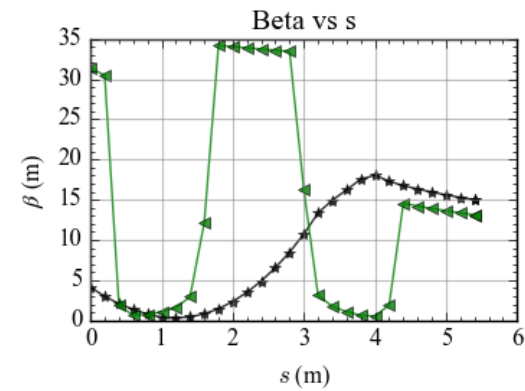
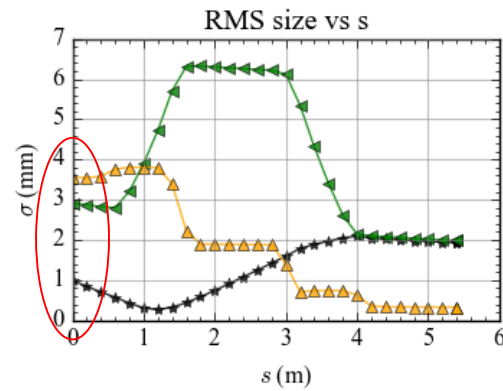
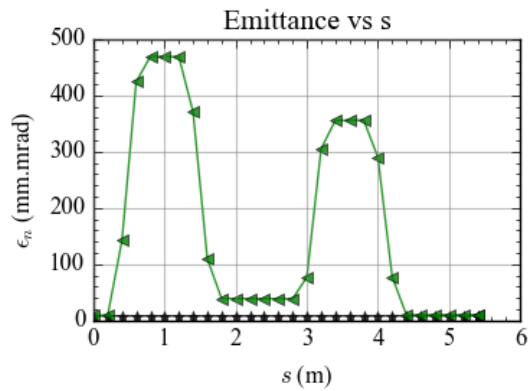
X  $\leftrightarrow$  Y

# 2<sup>nd</sup> Iteration

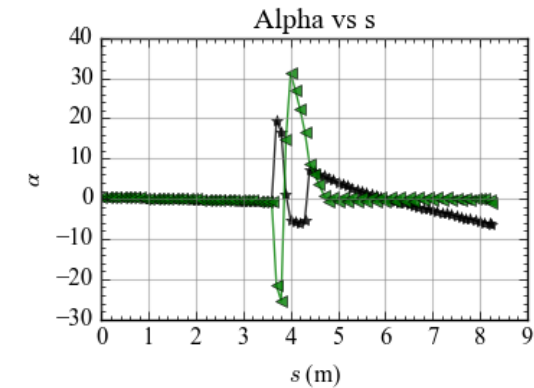
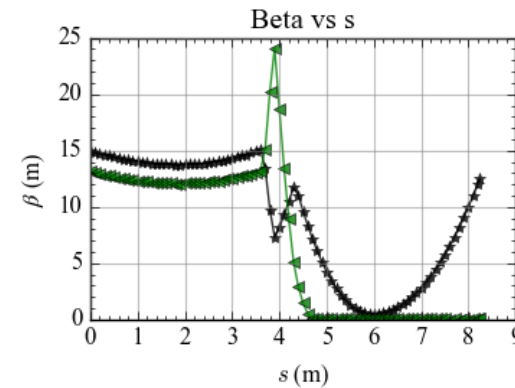
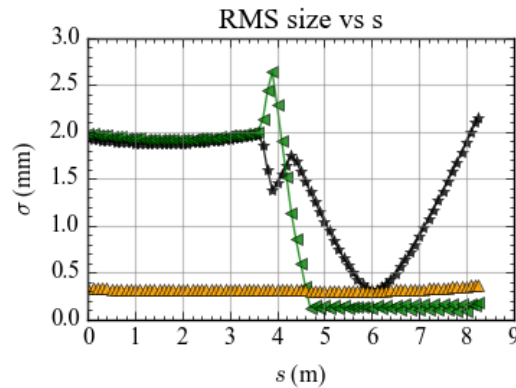
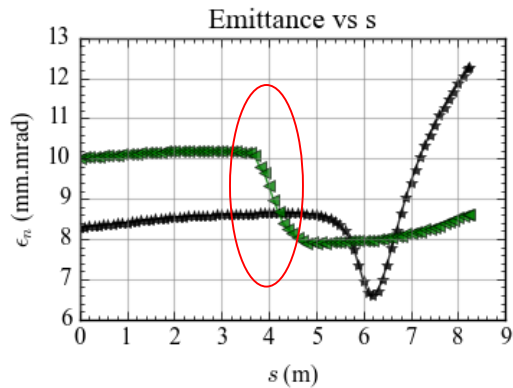
Forward tracking to the end of the undulator magnet (using beam from backward tracking)

1<sup>st</sup> Iteration, HIGH3.Q3 = 1.3 T/m

2<sup>nd</sup> Iteration, HIGH3.Q3 = 1.5 T/m



X ↔ Y





# Achievement and Outlook

## **PITZ and my self**

- Dispersion procedure
- Startup procedure for beam matching from BC to undulator magnet
- Beam dynamics in the BC
  
- Machine operation
- Simulation
- 1 LPR paper from IPAC23
- ... 1 paper from beam matching and super-radiant radiation

## **Next...**

- Python script for beam matching (in October)
- MATLAB script for beam matching (in November)

**Thank you for your attention**