

# e-CT – Computed Tomography with Electrons

Scattering / Material Budget based Imaging at Electron Accelerators

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13/01/2022

# Concept

# Multiple Scattering & Material Budget

## Coulomb Scattering, Highland Formula

- High-energy particles undergo multiple Coulomb scattering when traversing material  
→ Particle is deflected
- Scattering angle distribution:  
Gaussian-like center with tails at larger angles
- Width of Gaussian-like center well predicted by the Highland formula:

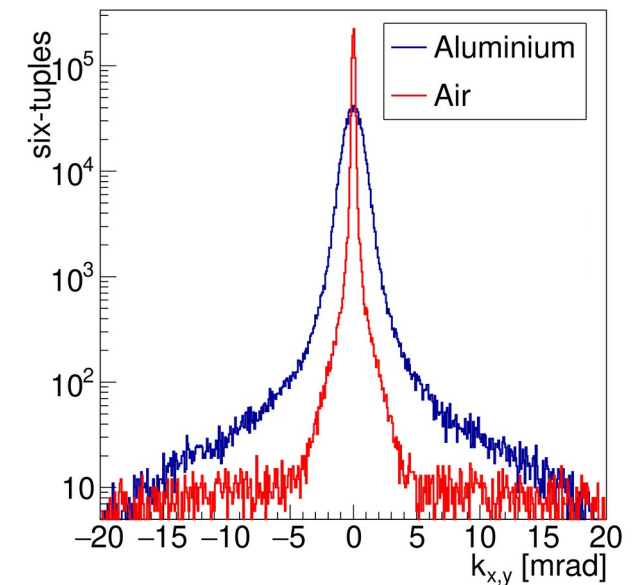
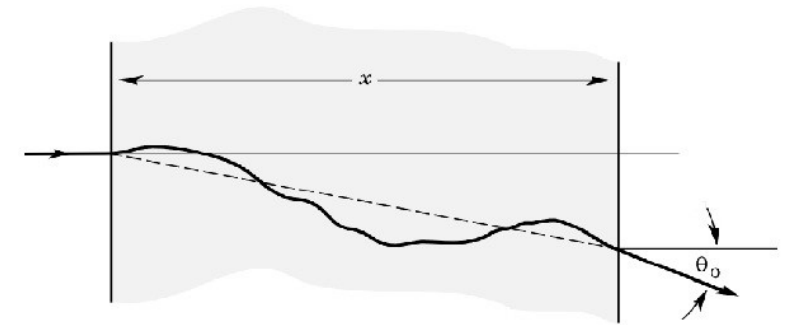
$$\theta_{x,y} = \frac{13.6 \text{ MeV}}{\beta c p} \sqrt{\frac{x}{X_0}} \left( 1 + 0.038 \ln \left( \frac{x}{X_0} \right) \right)$$

x: Path length in the material

$X_0$ : Material's radiation length

$\epsilon = x/X_0$ : Material Budget

- Measurement: Scattering angle distribution  
Characteristic quantity: Material budget



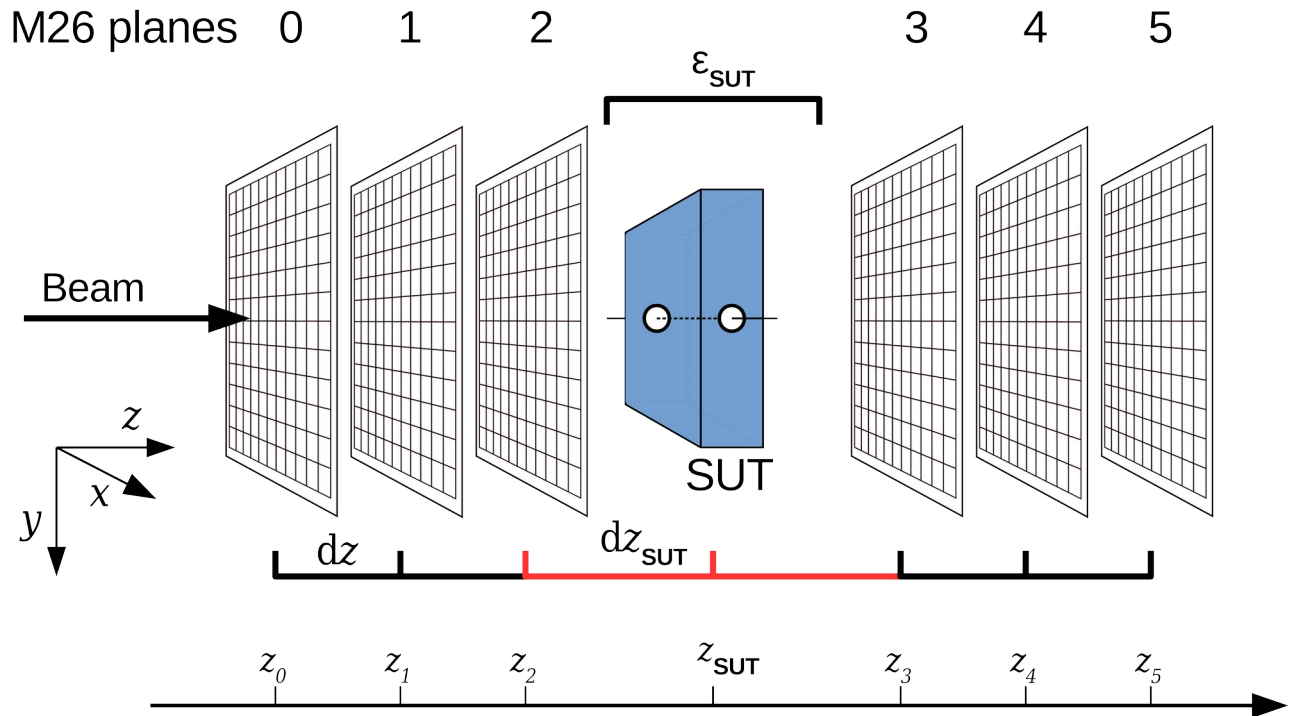
# The Work so Far

Track-based Multiple Scattering Tomography

# Track-based Multiple Scattering Tomography

## Position-resolved measurement of the material budget via the deflection angle

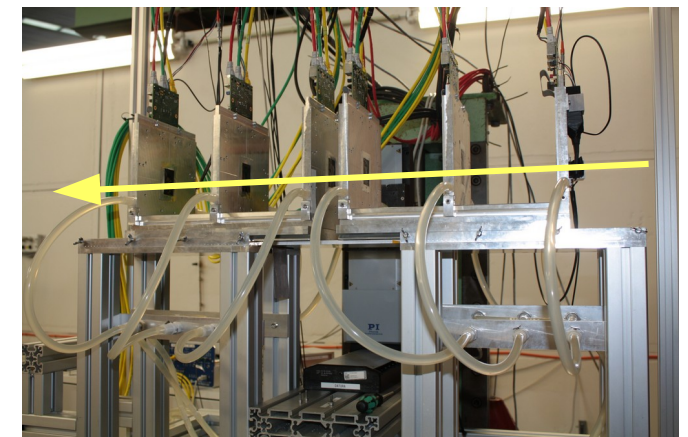
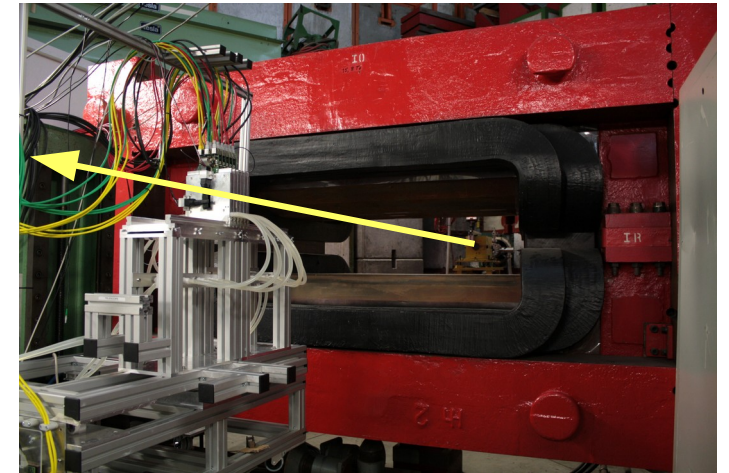
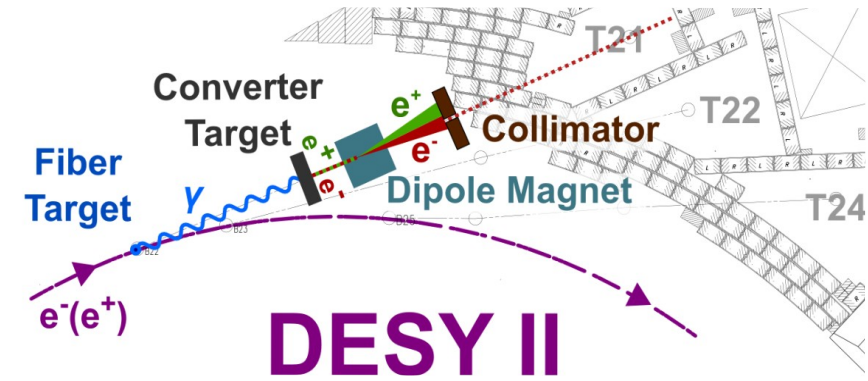
- Single-particle tracking before and after the sample under test (SUT) using so-called beam telescopes – multi-plane (silicon) tracking detectors
- Measurement of the scattering angle at the SUT
- Extrapolation of the track to the position of the sample
- Four steps:
  - Illuminate a sample with a charged particle **beam**
  - Measure the *hits* in the **pixel sensor** planes around it
  - Reconstruct the particle **trajectories** through the telescope
  - Extract the **width** of the kink angle distribution



# Measurement Setup

## Accelerator, beam line & beam telescope

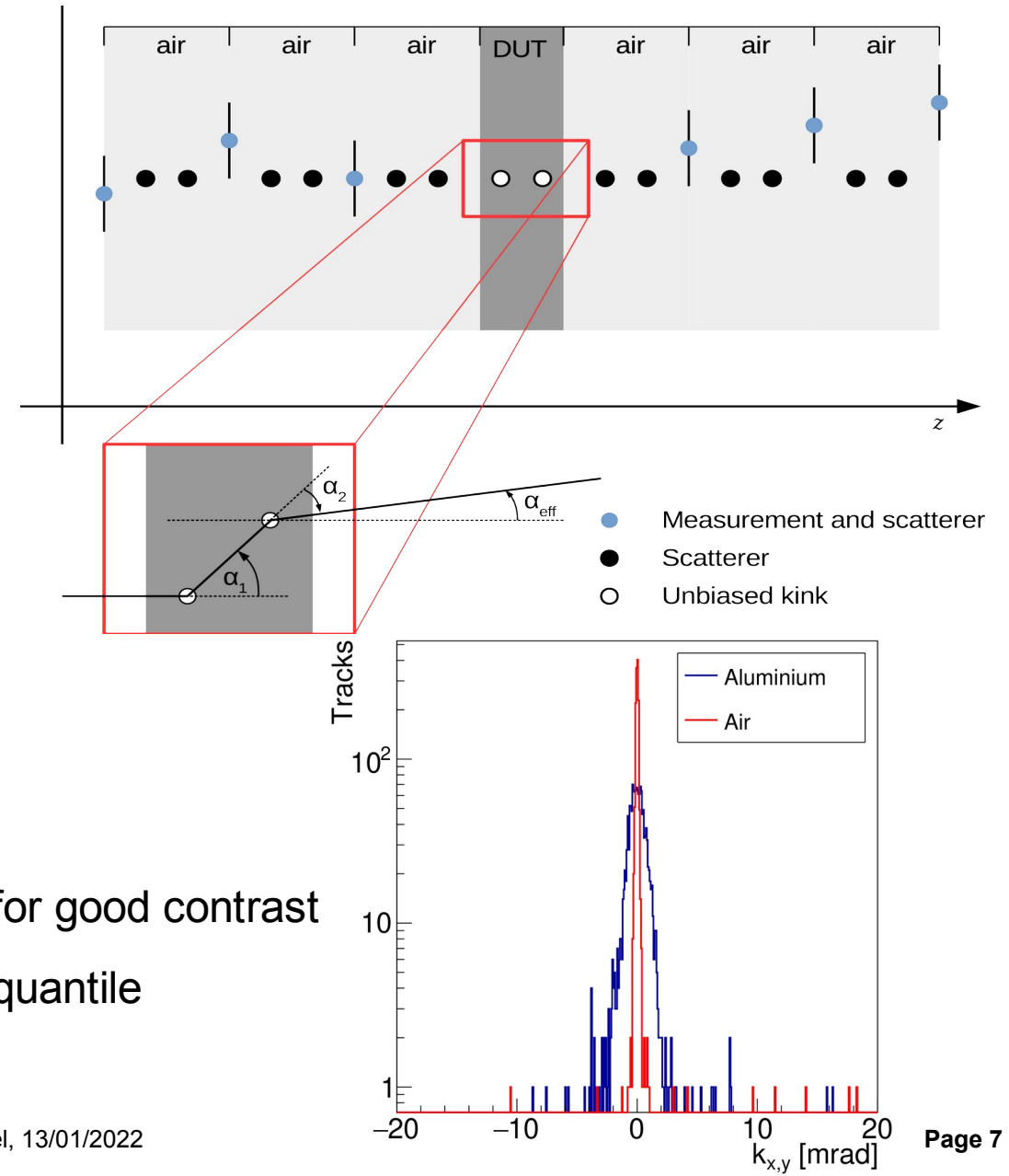
- DESY II Test Beam
  - Positron or electron beams created from primary bunch via bremsstrahlung / pair conversion target
  - Beam energy: 1 – 6 GeV
  - Particle rate: < 50 kHz (energy dependent)
  - Three beam lines available, all equipped with...
- Beam telescopes
  - Six Mimosa26 MAPS sensors
  - Pixel Pitch: 18.4  $\mu\text{m}$  x 18.4  $\mu\text{m}$
  - Active area: 10.6 mm x 21.2 mm
  - Intrinsic sensor resolution: > 3.24  $\mu\text{m}$
- Track resolution at SUT:  $\sigma \sim 2 \mu\text{m}$



# Track Reconstruction & Material Budget Estimators

## Combining robustness with contrast

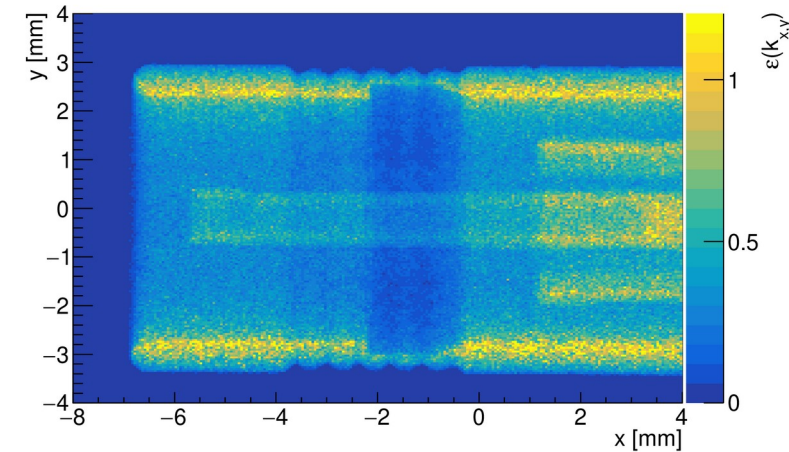
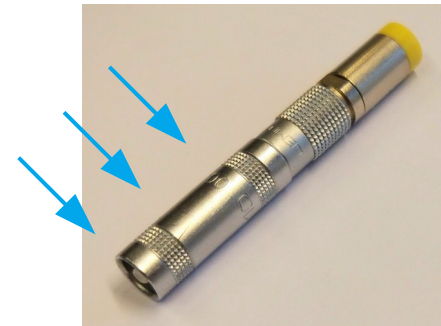
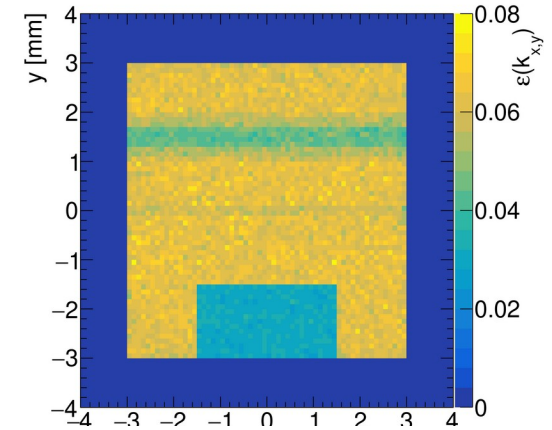
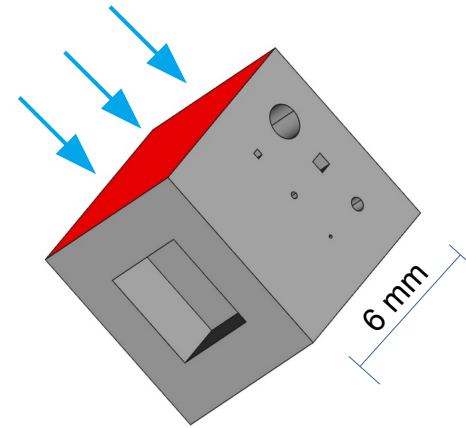
- Track model needs to allow kinks at scatterers
  - Using **General Broken Lines**
  - Find the most probable trajectory based on the measured hits
  - Uncertainties weighted with (known) detector materials to include multiple scattering in telescope
  - Kink angle at the sample:  
Local, unbiased parameter in the track model
  - Volume scatterer approximated by two thin scatterers
- Estimator for distribution width not straight forward
  - Gaussian shape only approximation
  - Need statistically robust method with high sensitivity for good contrast
  - E.g. **Average Absolute Deviation** of the inner 90% quantile
- Many more parameters: voxel size, required statistics



# Image Reconstruction

## 2D measurement of the scatterer material budget

- Illumination of the scatterer, reconstruction of individual particle tracks
- Division of the image plane (SUT) into regions (pixels)
- Calculation of scattering angle for every track, determination of scattering angle distribution width individually for each pixel
- Calibration of the scattering width to material budget using known-thickness known-material scatterers
- Result: projection of the material budget  
Data & simulation compare very well
- Material budget of LHC tracking detector layers  
(CMS & ATLAS upgrades, complex CF with glue)

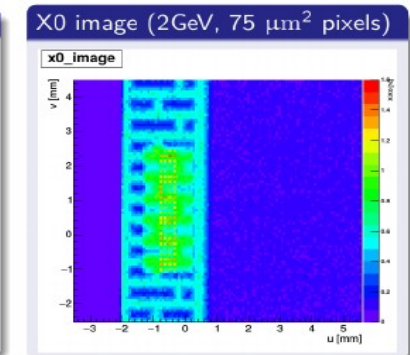
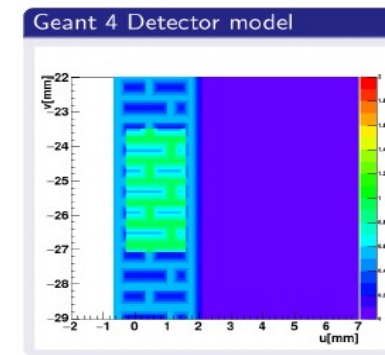
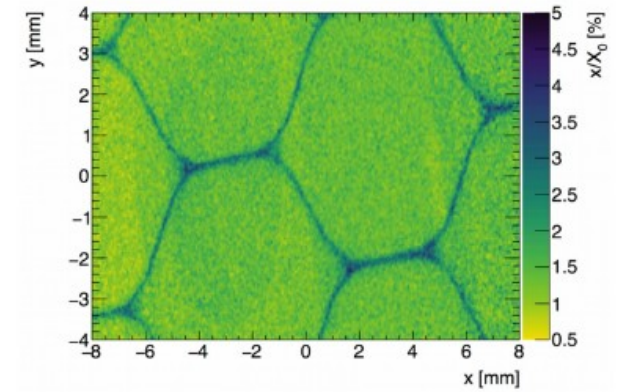
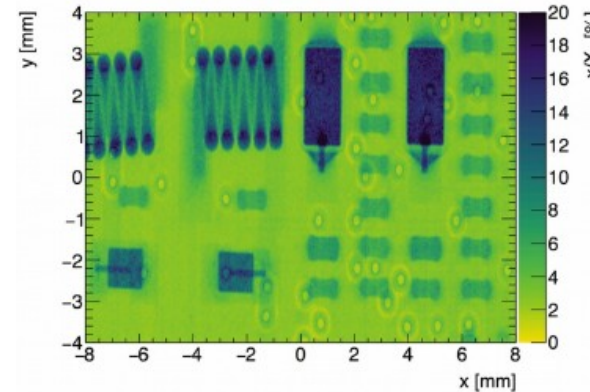
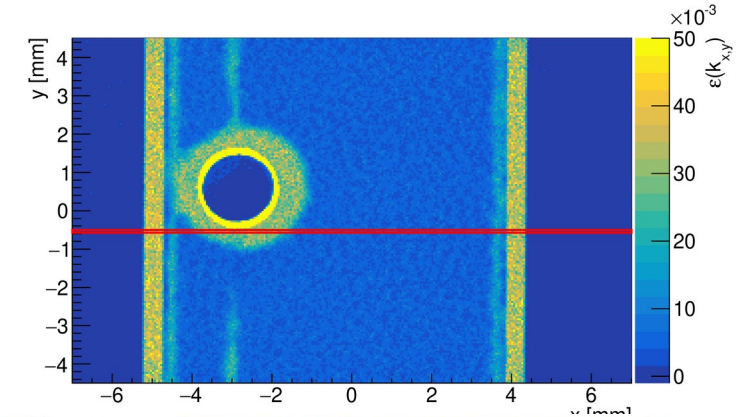
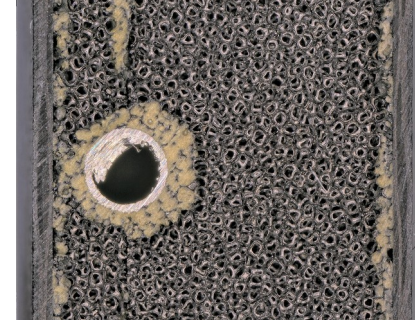




# First Applications in High-Energy Physics

## Measurement of detector structures & comparison with simulations

- CMS Phase II Tracker Upgrade
  - CF foam with cooling pipe & face sheets
  - Glue layers visible in material budget
- ATLAS ITk Upgrade
  - Measurement of endcap petal structures
  - PCBs, CF honeycomb structure
- Belle-II Silicon Vertex Detector
  - Comparison of material budget measurement with detailed simulations

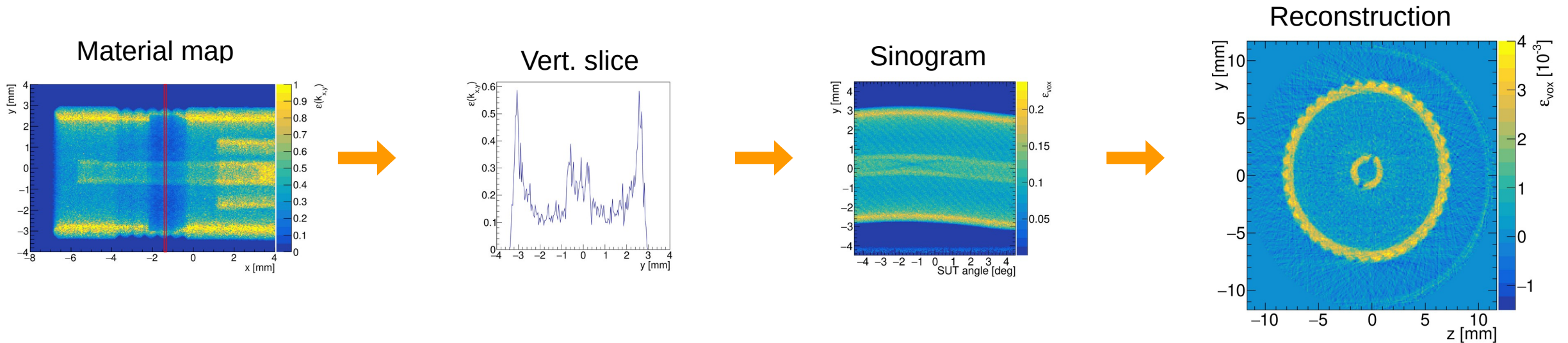
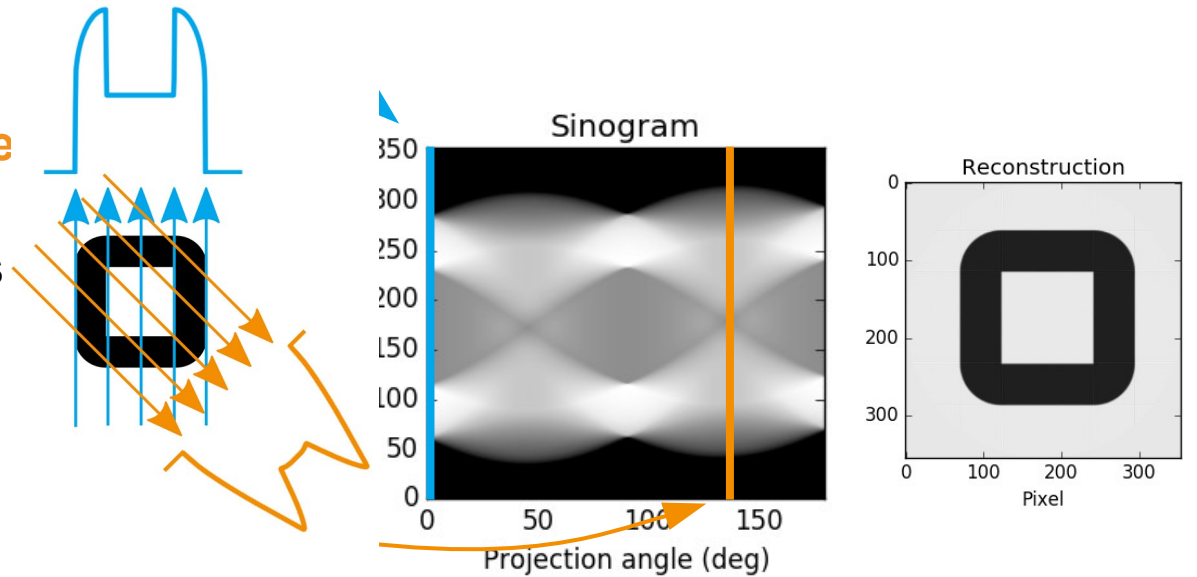


# 3D Computed Tomography

Reconstruct the 3<sup>rd</sup> dimension from repeated measure

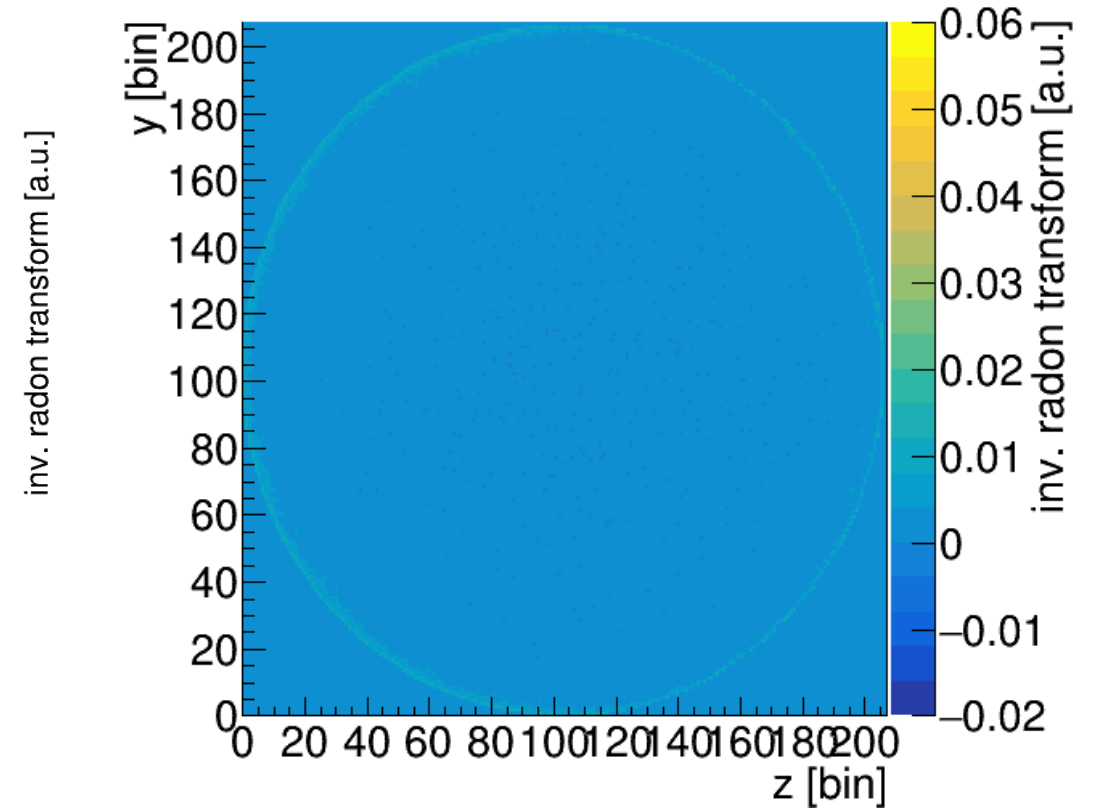
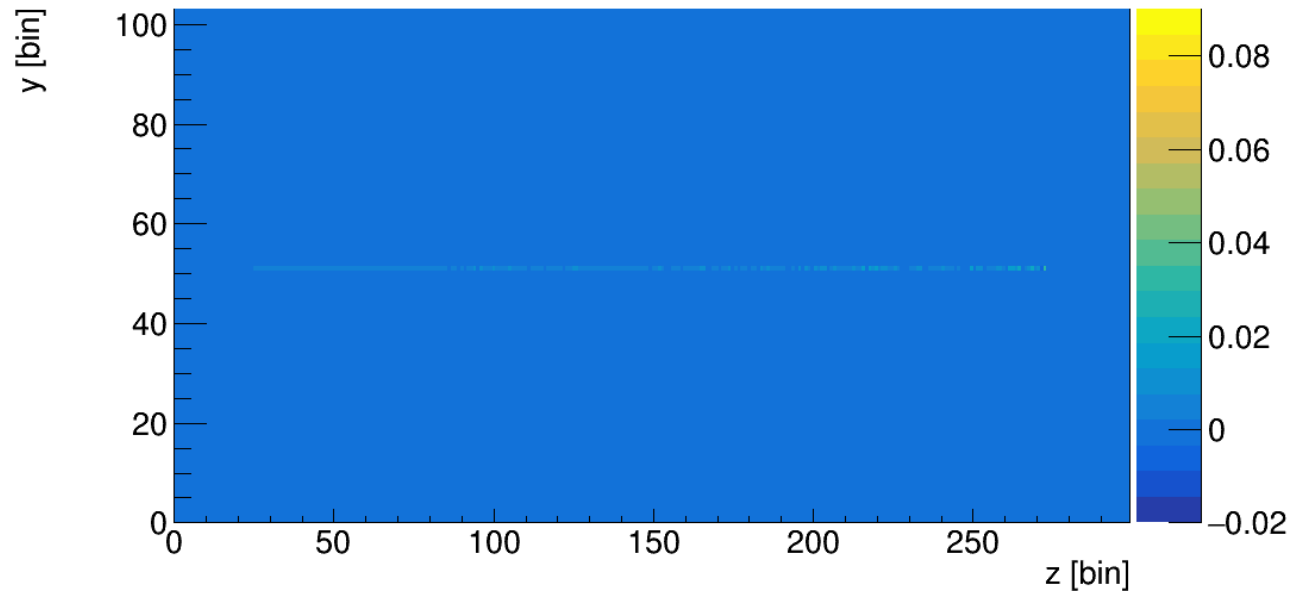
- Repeated projection measurement at different angles
- Generate sinogram from individual images
- Perform inverse radon transform to reconstruct internal material budget distribution

→ Computed tomography



# 3D Images: Animations

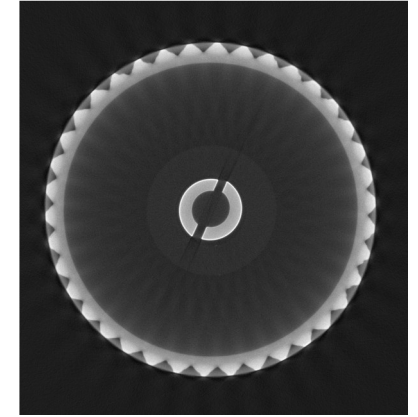
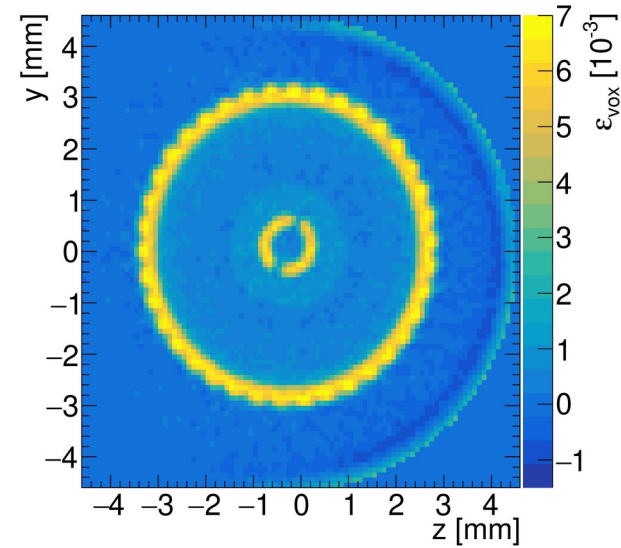
Computed tomography via scattering distribution of electrons



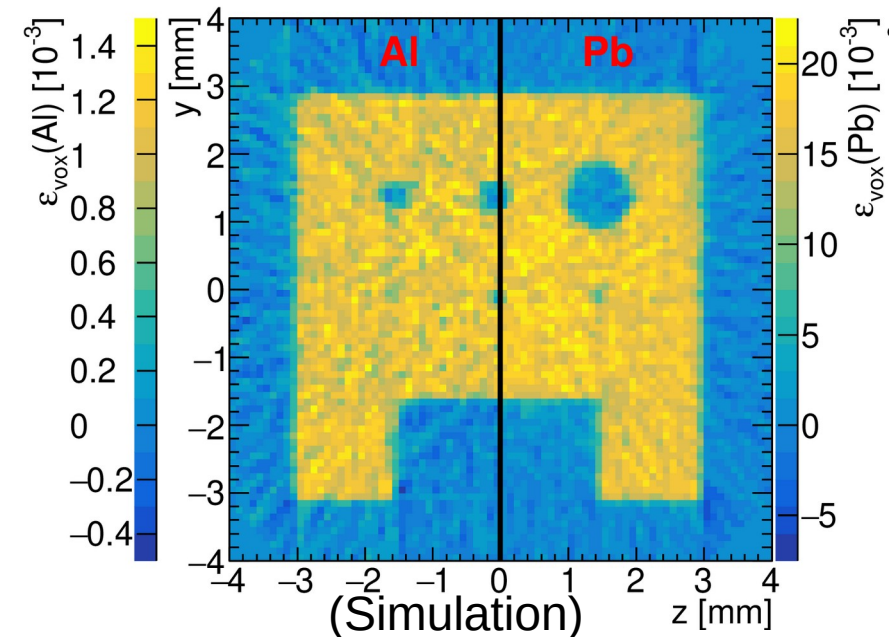
# Comparison: X-Ray CT

## Pros and cons to conventional computed tomography

- X-rays attenuation length significantly shorter than radiation length of high-energy particles – example: **Lead**
  - X-ray attenuation length:  
~0.1 mm (50 keV) / ~0.7 mm (200 keV)
  - Radiation length (GeV electrons): 5.6 mm
- GeV electrons can serve as probe for thicker materials
- High-Z materials can be probed with high precision
  - Simulation: after calibrating for material, even higher contrast achieved for lead samples than aluminum
- Strongly reduced beam hardening effects



••• Helmholtz-Zentrum  
••• Geesthacht  
Zentrum für Material- und Küstenforschung



# Status Quo

## Computed tomography via scattering distribution of electrons

- Reconstruction of 3D material structure using multiple scattering distributions achieved, both from simulation and measured data
- Computed tomography achieves good contrast, better for larger material budget
- Acceptance area limited to telescope sensors to  $\sim 1 \text{ cm} \times 2 \text{ cm}$
- Limited by statistics
  - Individual particle tracking
  - Measurement time for one sample  $\sim 3$  days
- With faster response, could this method be of broader interest?
- Industrial & clinical applications / diagnosis tool?
- Can we decrease measurement time by orders of magnitude?

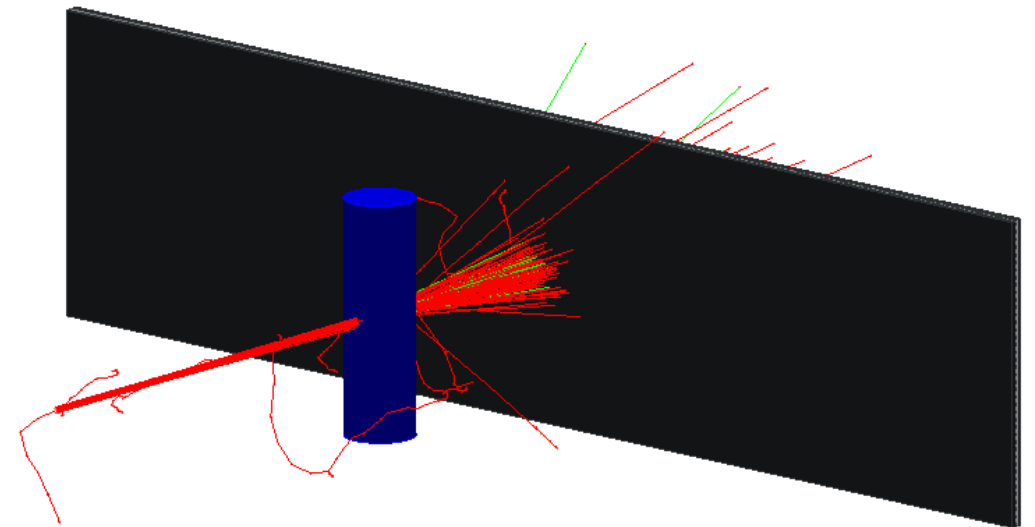
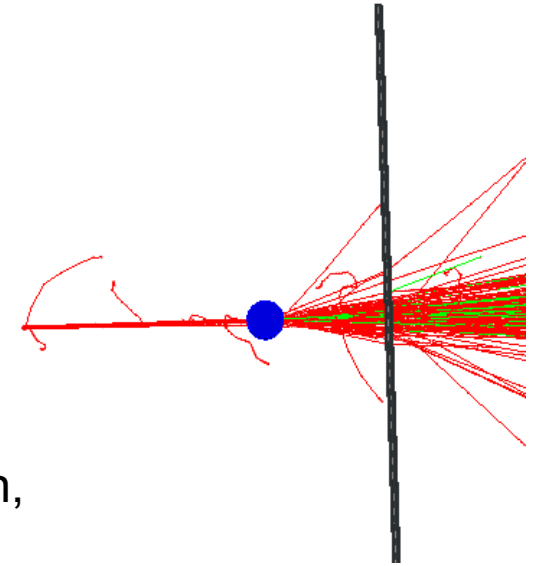
# A New Approach

Integrated-intensity-based Multiple Scattering Tomography

# Intensity-Based Measurements

## Making use of high-performance beams

- Up till now, particle track position used to identify relevant pixel / voxel of final image
- Turning things around:  
use pencil beam to raster the sample, beam position dictates voxel size & position
- Single detector records absolute beam size after scattering as function of the position,  
Single-shot many-particle measurement of scattering width
- Requirements:
  - Well-controlled, small beam spot @ sample
  - Controlled relative movement beam  $\leftrightarrow$  sample
  - High repetition rate for fast image recording
  - Fast detectors with large dynamic range



@ DESY:  
PITZ – Zeuthen  
ARES – Hamburg

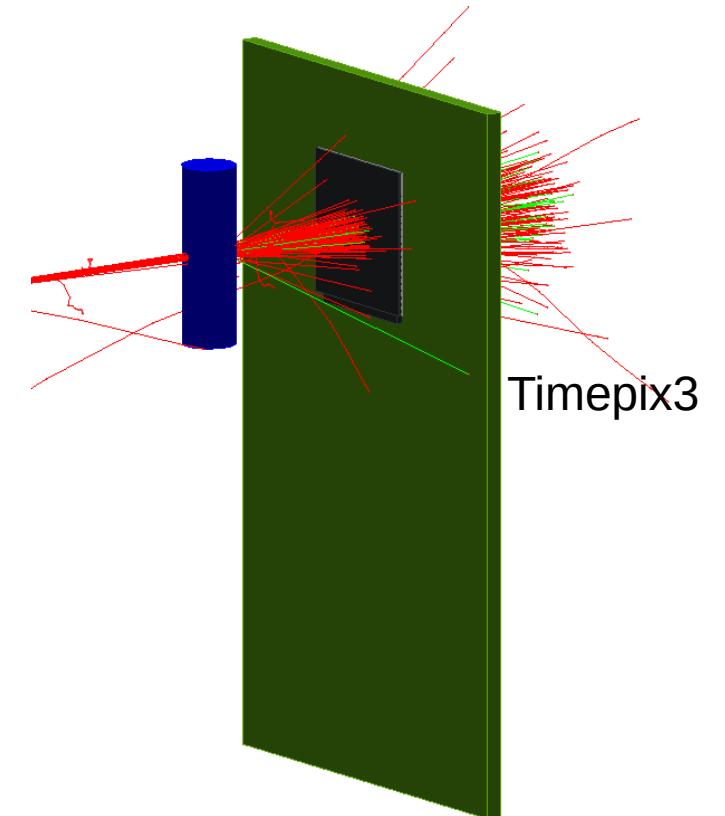
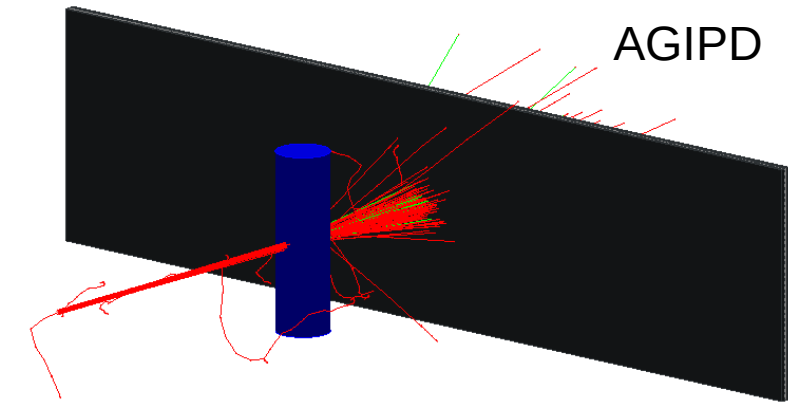
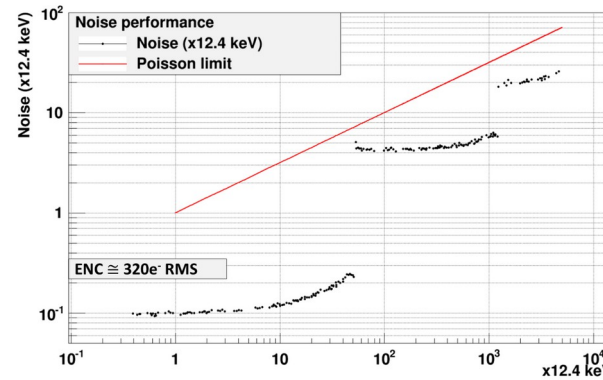
# Detector Options

- **AGIPD**

- Large area
- High dynamic range, if functioning in *adaptive gain* mode
- Available on loan by developers @ DESY FS
- Requires implementation of data acquisition

- **Timepix3**

- Smaller area
- Lower, but tolerable dynamic range
- Available at almost any time @ DESY FH
- Data acquisition ready
  - Suitable candidate for proof-of-principle measurements



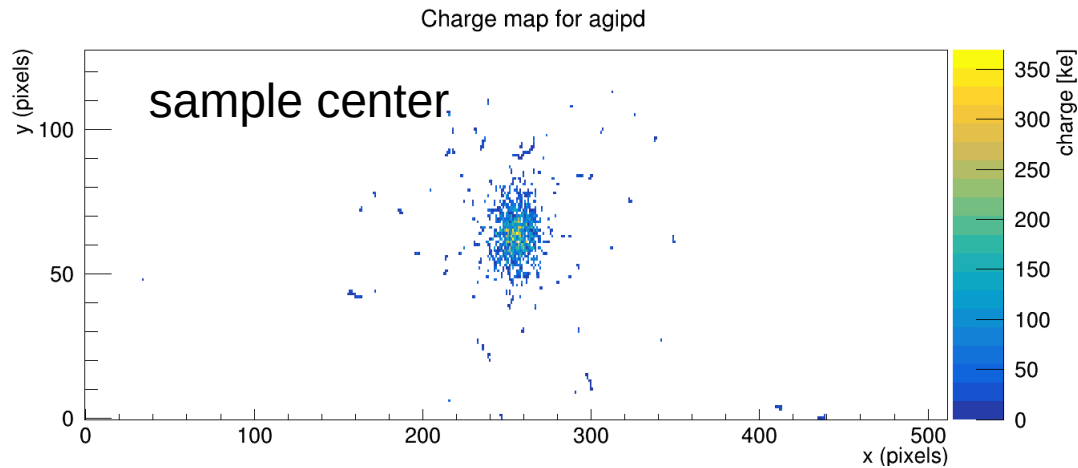


# Scattering Distribution & Sample Distance

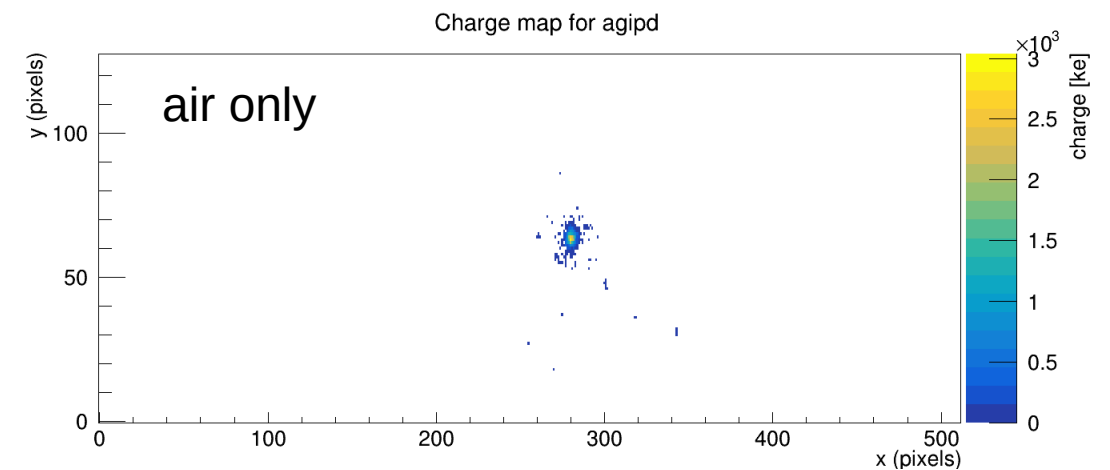
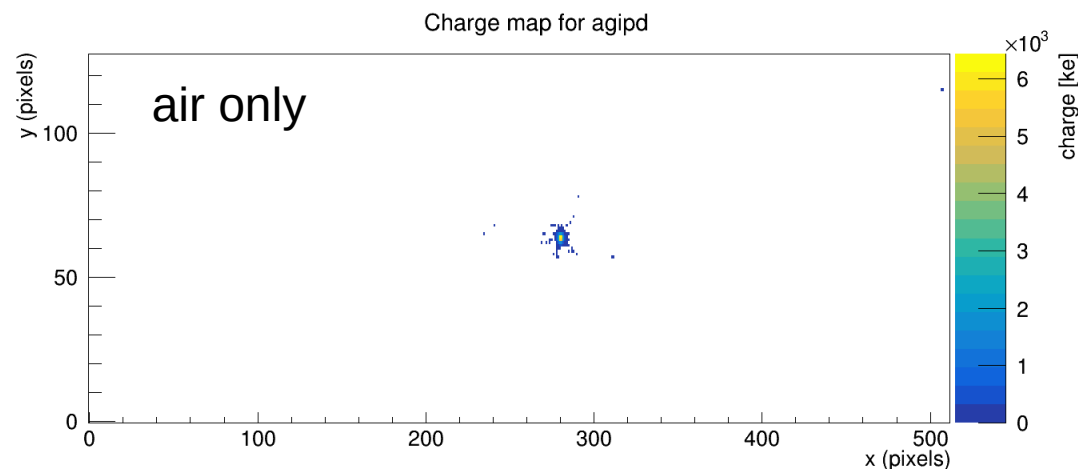
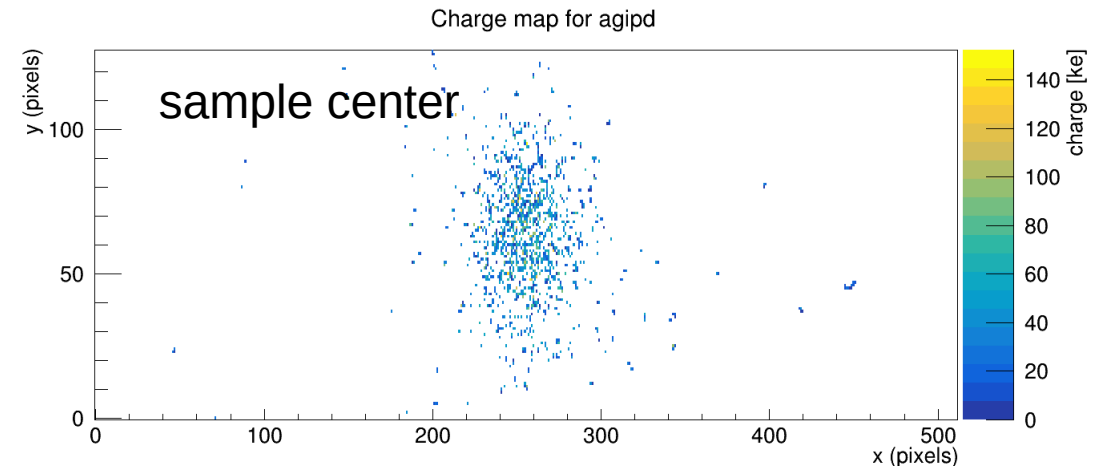
Allpix<sup>2</sup> Simulations with AGIPD Sensor Geometry

22 MeV, 1000 electrons  
100  $\mu\text{m}$  transverse size  
plexiglass cylinder, 3mm rad.

Sample  $\leftrightarrow$  AGIPD: 20 mm



Sample  $\leftrightarrow$  AGIPD: 50 mm



# Summary

# Summary & Outlook

## e-CT imaging based on material budget measurements with electrons

- Single-particle tracking e-CT shown to perform well
  - Simulation, calibration, data taking performed at DESY II synchrotron beam lines
  - Already used by high-energy physics experiments to measure detector component properties
  - Measurement time prohibitively long for wider application in industry / medical applications
- Novel approach using one-shot intensity-based scattering measurements
  - Reduces required measurement time by orders of magnitude
  - Rastering of sample either by beam or by motion stage
  - Single detector record widened beam after scattering interaction in sample
- Simulations & detector / DAQ preparations ongoing, funding application for postdoc & PhD student pending
- We are hoping for some first beam time in 2022!

# Open Questions / Beam Requirements / ...

- How can we synchronize with the accelerator?  
Bunch clock?
- Beam conditions:
  - How does rastering work? Area, stepping, ...?
  - Minimal possible bunch current?
  - Transverse bunch size at focal plane?
- Counting room, space for detector DAQ & infrastructure?
- General logistics

**Thank you**

## Contact

**DESY.** Deutsches  
Elektronen-Synchrotron

[www.desy.de](http://www.desy.de)

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