

Virtual Pepper Pot

- Algorithm review
- Simulation
- Experiment: Methodic studies

Namra Aftab
PITZ Physics Seminar
25-02-2021

VPP Algorithm

Review

- crossing of horizontal and vertical slits
- similar to pepper pot but multi-shot
- ability to perform 4D TPS measurements

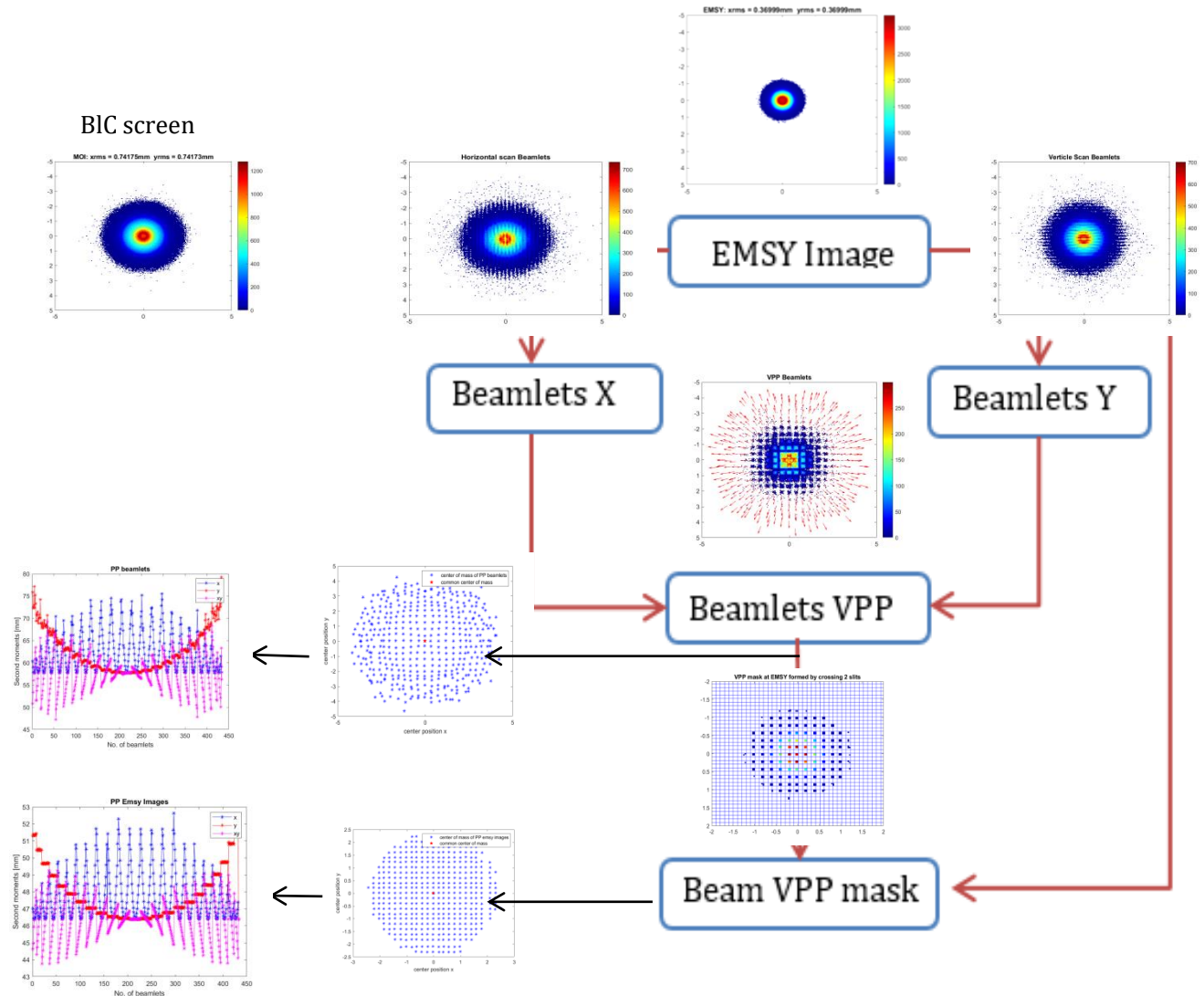
$$\sigma^{4D} = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle & \langle x'y \rangle & \langle x'y' \rangle \\ \langle xy \rangle & \langle x'y \rangle & \langle y^2 \rangle & \langle yy' \rangle \\ \langle xy' \rangle & \langle x'y' \rangle & \langle yy' \rangle & \langle y'^2 \rangle \end{pmatrix} = \begin{pmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{xy}^T & \sigma_{yy} \end{pmatrix}$$

$$\epsilon_x = \sqrt{\langle xx \rangle \langle x'x \rangle - \langle xx' \rangle^2}$$

$$\epsilon_y = \sqrt{\langle yy \rangle \langle y'y \rangle - \langle yy' \rangle^2}$$

$$C_{xy} = \sqrt{\langle xy \rangle \langle x'y' \rangle - \langle xy' \rangle \langle x'y \rangle}$$

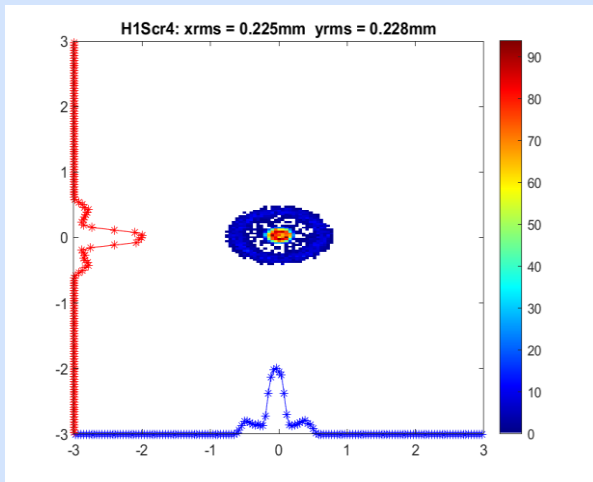
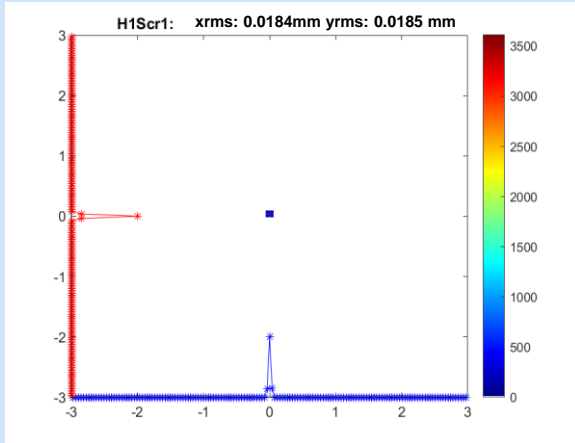
$$\epsilon_{4D}^2 = \det(\sigma^{4D}) = \epsilon_x^2 \epsilon_y^2 - C_{xy}^4$$



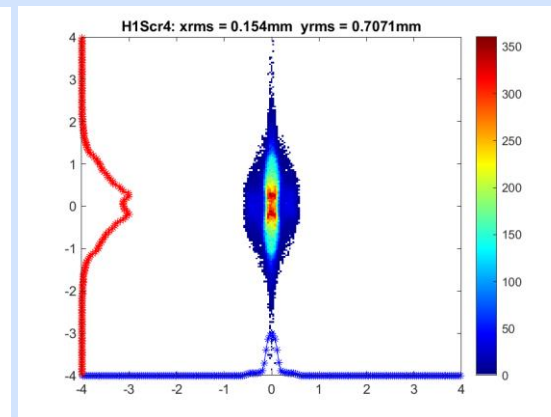
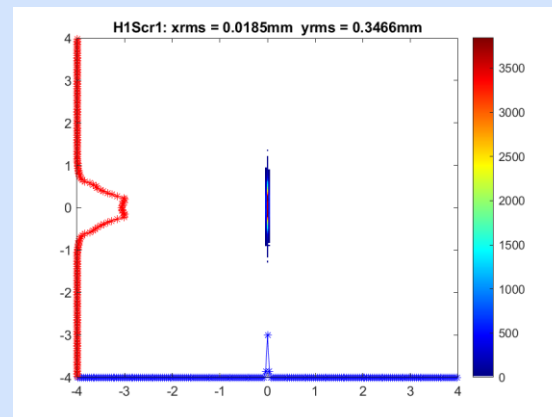
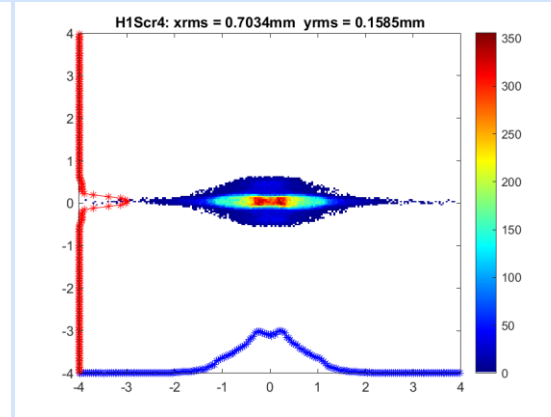
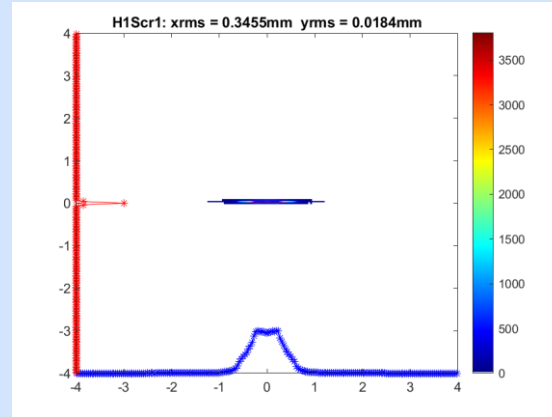
VPP Algorithm-crossing slits

Comparing PP beamlet with VPP beamlet

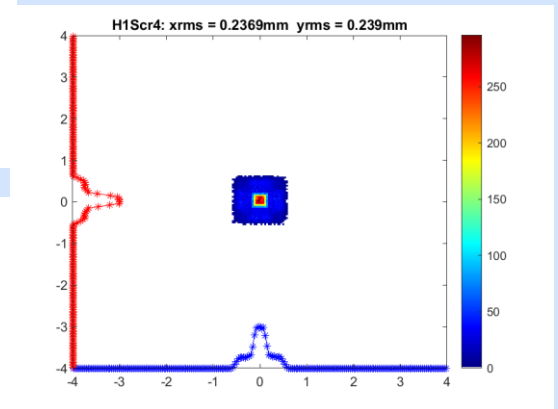
Result of passing beam through a hole



Result of crossing horizontal and vertical beamlets



Getting rid of the foreign particles →
Minimum of crossed beamlets



Astra Beam (uncoupled)

Results from Astra monitor (post-pro)

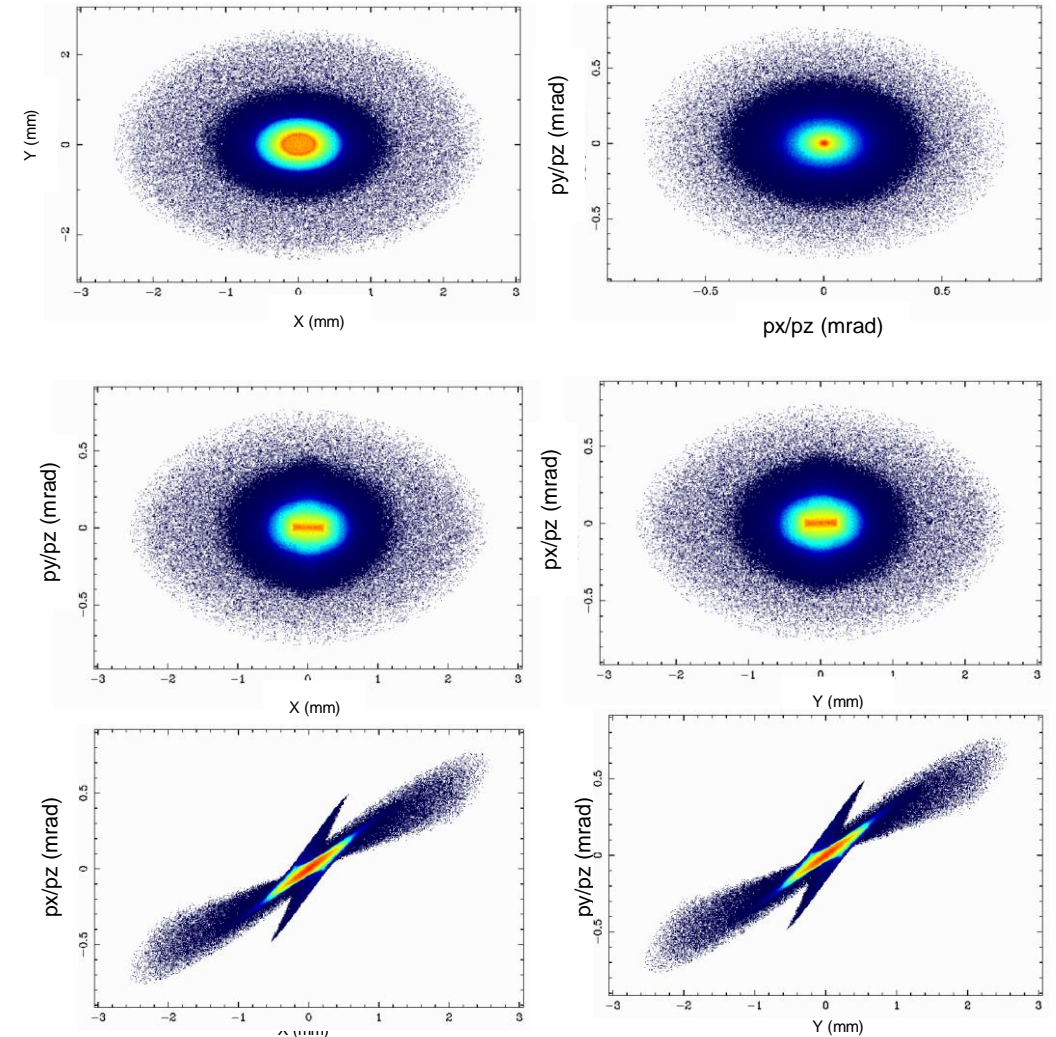
- ASTRA beam generated from 6 ps FWHM temporal gaussian laser

```
Particles taken into account   N = 2000000
total charge                   Q = -0.2500 nC
horizontal beam position       x = -9.3116E-06 mm
vertical beam position         y = -5.3608E-07 mm
longitudinal beam position     z = 5.280 m
horizontal beam size           sig x = 0.3699 mm
vertical beam size             sig y = 0.3698 mm
longitudinal beam size        sig z = 1.047 mm
average kinetic energy         E = 18.78 MeV
energy spread                  dE = 49.43 keV
average momentum               P = 19.29 MeV/c
transverse beam emittance     eps x = 0.6068 pi mrad mm
correlated divergence         cor x = 0.1146 mrad
transverse beam emittance     eps y = 0.6067 pi mrad mm
correlated divergence         cor y = 0.1146 mrad
longitudinal beam emittance   eps z = 12.62 pi keV mm
correlated energy spread      cor z = 47.94 keV
emittance ratio eps y/eps x   = 1.000
```

```
trace space emittance     eps x = 0.6069 pi mrad mm
trace space emittance     eps y = 0.6069 pi mrad mm
```

Reduced emittances:

```
hor. emittance minus z correlation: = 0.6011 pi mrad mm
hor. emittance minus z & E correlation: = 0.6063 pi mrad mm
ver. emittance minus z correlation: = 0.6010 pi mrad mm
ver. emittance minus z & E correlation: = 0.6062 pi mrad mm
long. emittance minus 2nd order corr.: = 5.513 pi keV mm
long. emittance minus 2nd & 3rd order corr.: = 4.781 pi keV mm
```



Astra Beam (uncoupled)

Results from slit scan files and VPP algorithm

❑ Astra Results

- $\epsilon_x = 0.6069$ mm mrad
- $\epsilon_y = 0.6069$ mm mrad

❑ Slit scan files

- scan step = 10um approximately (520 beamlets)
- x and y beamlets, slit positions, must have

❑ VPP beamlets

- crossing every 6th beamlets (Huge data of images!!)

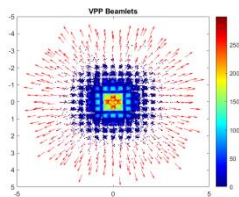
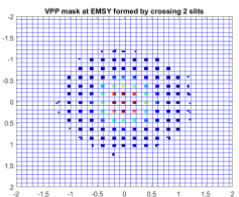
❑ Relative error = $\frac{\epsilon_{astra} - \epsilon_{slit_scan/vpp}}{\epsilon_{astra}}$

Slit width (um)	Slit scan emittance (mm mrad)				VPP emittance (mm mrad)			
	ϵ_x	ϵ_y	ϵ_x rel. err %	ϵ_y rel. err %	ϵ_x	ϵ_y	ϵ_x rel. err %	ϵ_y rel. err %
50	0.6229	0.6229	2.63	2.63	0.7236	0.7152	19	17.8
10	0.6098	0.6101	0.48	0.53	0.5541	0.5893	8.6	2.9

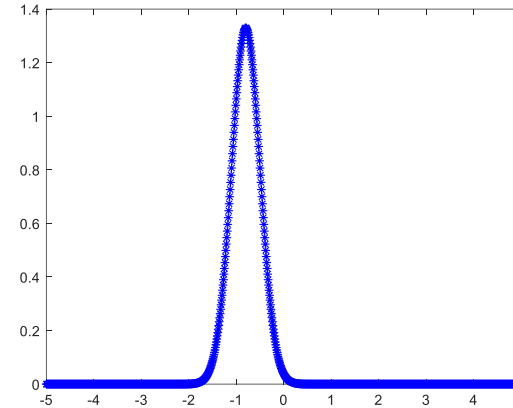
VPP Algorithm – overestimating? underestimating?

Exploring further: Estimating mean and variance

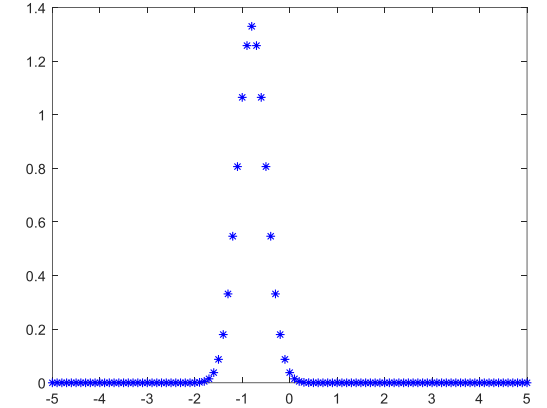
- $x = -5 : \text{step} : 5$
- $\mu = -0.8$
- $\sigma = 0.3$
- $\text{var} = 0.09$
- $G = \frac{1}{\sqrt{2\pi}} \cdot \left(\frac{1}{\sigma} \right) \cdot \left(\exp\left(-0.5 \cdot \left(\frac{x-\mu}{\sigma}\right)^2\right) \right)$
- $G1 = G / \sum(G)$
- $\text{meanG} = \sum(x \cdot G1)$
- $\text{varG} = \sum(G1 \cdot (\text{meanG} - x)^2)$
- **PP Emsy subimages case**
- **PP beamlets crossed at edges**



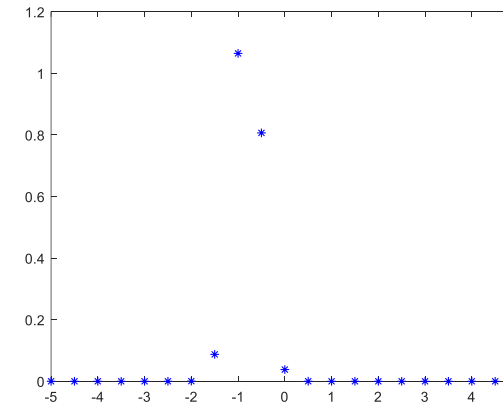
step = 0.01, $\mu = -0.8$, $\text{var} = 0.09$



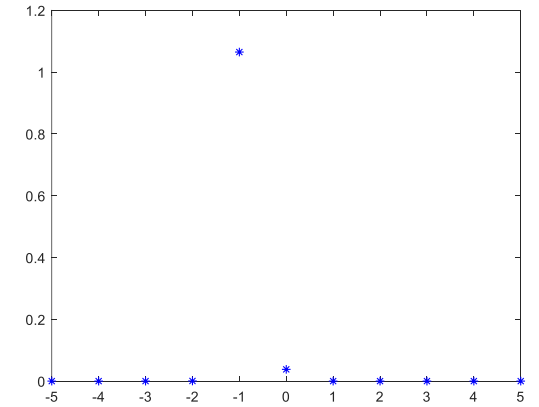
step = 0.1, $\mu = -0.8$, $\text{var} = 0.09$



step = 0.5, $\mu = -0.8011$, $\text{var} = 0.0917$



step = 1, $\mu = -0.966$, $\text{var} = 0.0337$

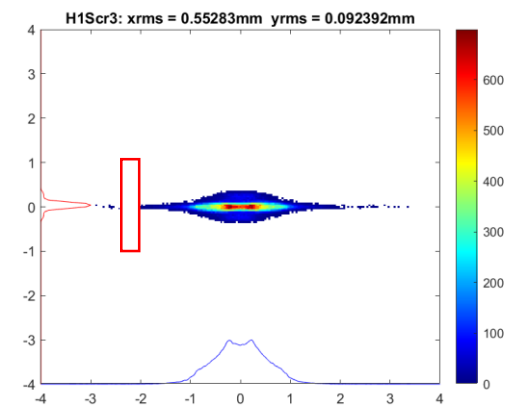
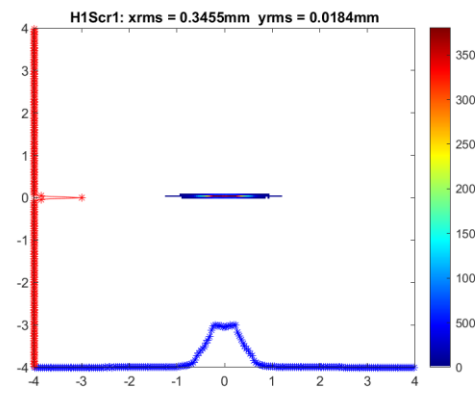
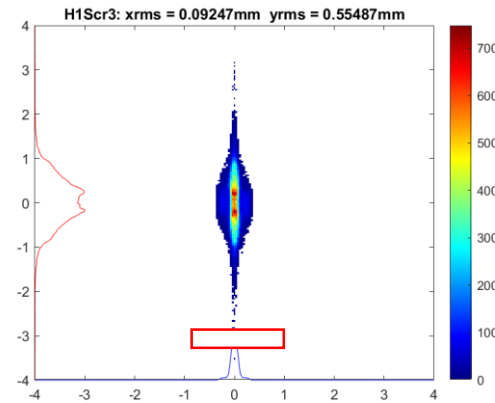
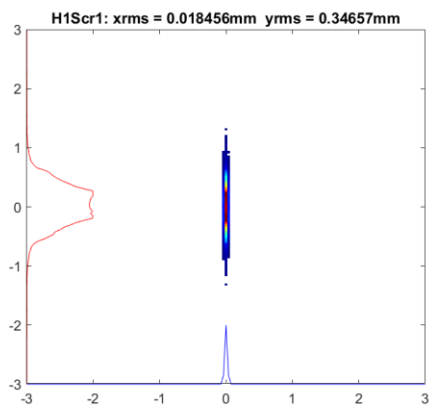


Dependent on resolution of camera!

VPP Proof of Principle simulation

Emittance Results of slit scan

- EMSY1X central beamlet + EMSY2Y scan + H1Scr4
- EMSY1Y central beamlet + EMSY2X scan + H1Scr4



EMSY1 slit width (um)	EMSY2 slit width (um)	Slit scan emittance (mm mrad)	
		ϵ_x	ϵ_y
50	50	0.8435	-
		-	0.8471
	10	0.7900	-
		-	0.7921

L1= 1848 % distance between EMSY1 and EMSY2 7125-5277
 L2= 1795 % distance between EMSY2 and H1Scr5 8920-7125
 L3= 3133 % distance between EMSY1 and H1Scr4 8410-5277
 L4= 3643 % distance between EMSY1 and H1Scr5 8920-5277
L5= 1285 % distance between EMSY2 and H1Scr4 8410-7125
 L6= 5153 % distance between EMSY2 and Pst.Scr1 12278-7125

Drift length less < 3.133

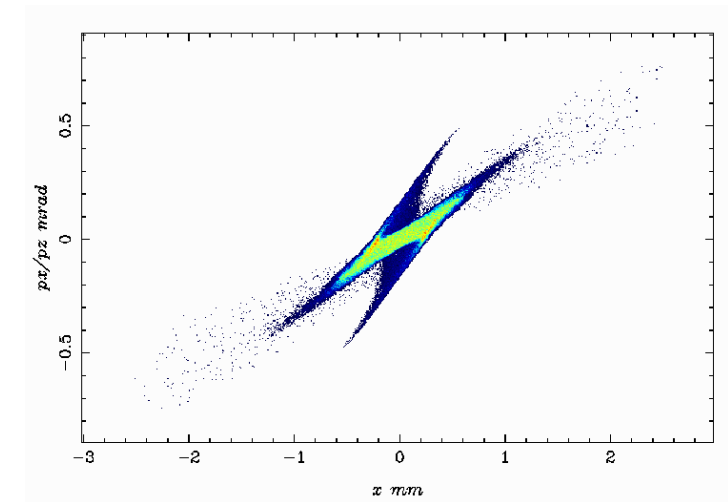
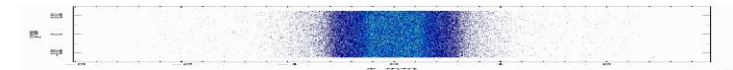
➤ Check it for greater drift length

VPP Proof of Principle simulation

Astra monitor

```
Particles taken into account      N =      116382
total charge                      Q =     -1.4548E-02 nC
horizontal beam position          x =     -7.7091E-04 mm
vertical beam position            y =      4.2133E-06 mm
longitudinal beam position        z =         5.280   m
horizontal beam size              sig x =    0.3453   mm
vertical beam size                sig y =    1.4418E-02 mm
longitudinal beam size            sig z =    0.9072   mm
average kinetic energy            E =      18.79   MeV
energy spread                     dE =     42.95   keV
average momentum                  P =      19.29   MeV/c
transverse beam emittance         eps x =    0.7669   pi mrad mm
correlated divergence             cor x =    0.1063   mrad
transverse beam emittance         eps y =    2.6209E-02 pi mrad mm
correlated divergence             cor y =    4.1692E-03 mrad
longitudinal beam emittance       eps z =    7.933   pi keV mm
correlated energy spread          cor z =    42.05   keV
emittance ratio eps y/eps x      =         29.26

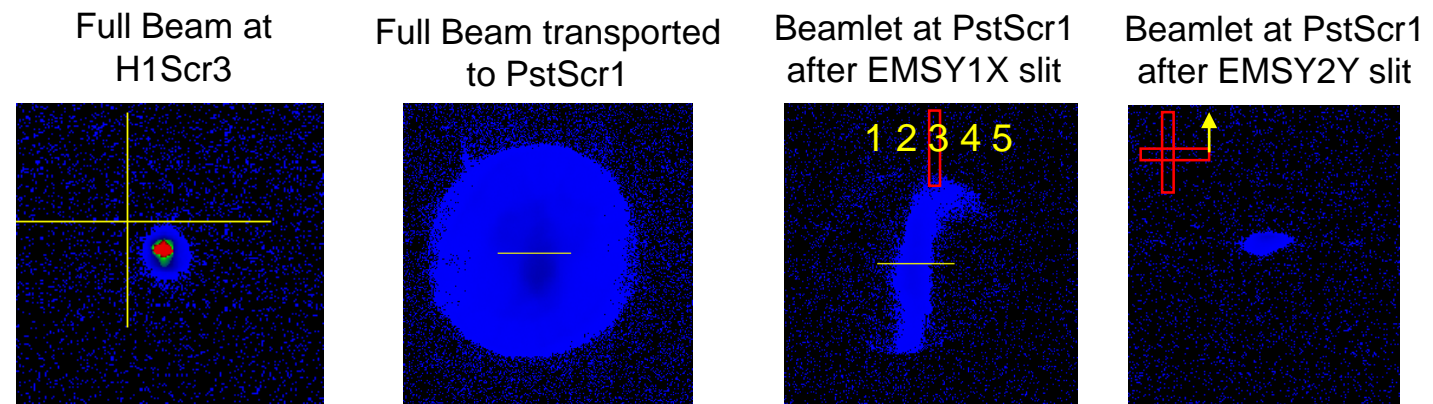
trace space emittance             eps x =    0.7668   pi mrad mm
trace space emittance             eps y =    2.6197E-02 pi mrad mm
Reduced emittances:
hor. emittance minus z correlation: =    0.7644   pi mrad mm
hor. emittance minus z & E correlation: =    0.7648   pi mrad mm
ver. emittance minus z correlation: =    2.6209E-02 pi mrad mm
ver. emittance minus z & E correlation: =    2.6209E-02 pi mrad mm
long. emittance minus 2nd order corr.: =    2.707   pi keV mm
long. emittance minus 2nd & 3rd order corr.: =    2.656   pi keV mm
```



VPP Proof of Principle experiment

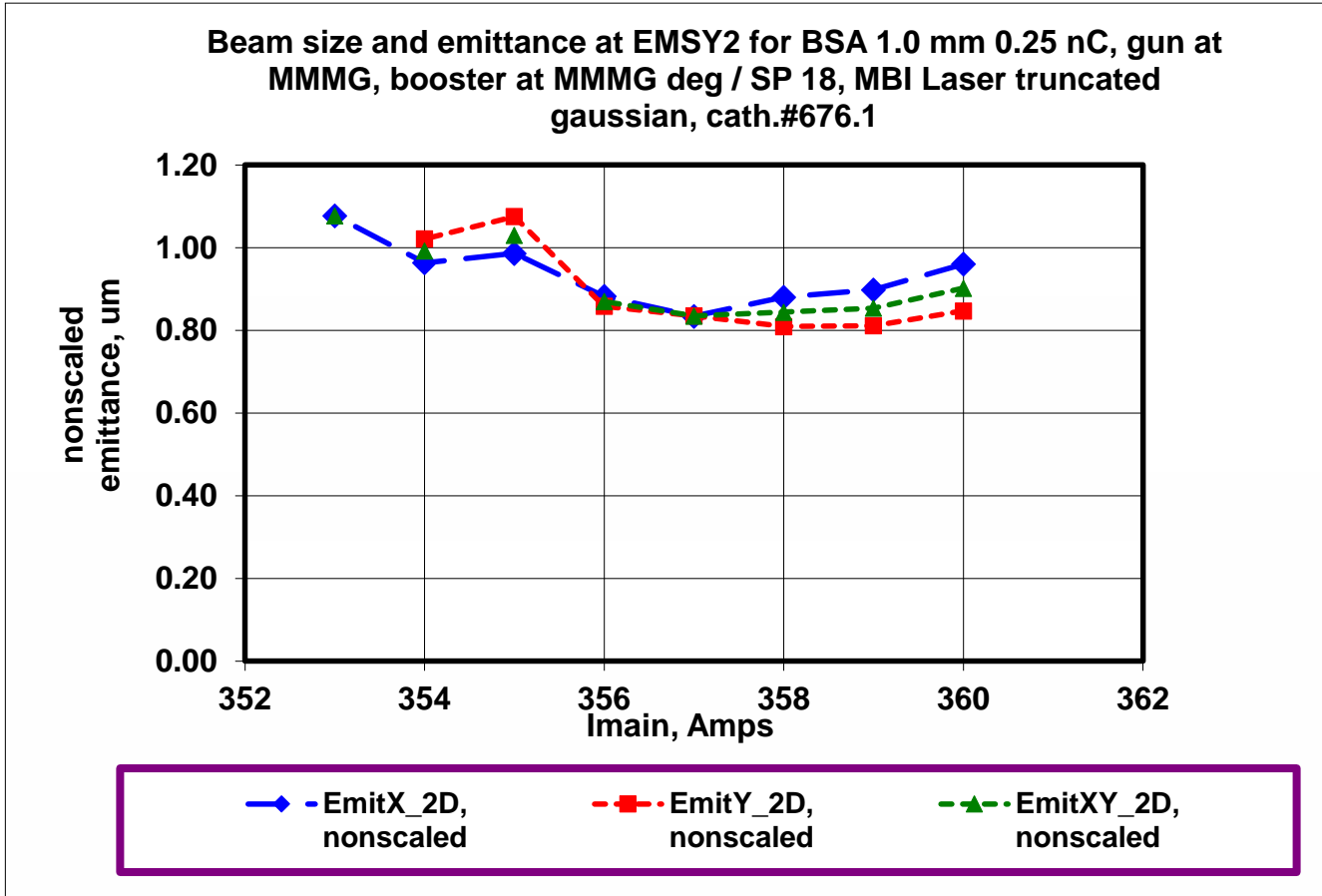
Experiment in shifts 12-14.02.2021 (~2 shifts)

- Laser : MBI
- Beam charge : 250pC
- Beam energy: 21 MeV/c
- Solenoid scan at EMSY2 using Pst.Scr1 as MOI screen
- Set I_{main} corresponding to minimum projected emittance
- EMSY2Y scan for 5 beamlets from EMSY1X at different locations
- EMSY2X scan for 5 beamlets from EMSY1Y at different locations
- Scanned without Gun Quads
- Scanned with Gun Quads 1 and 2



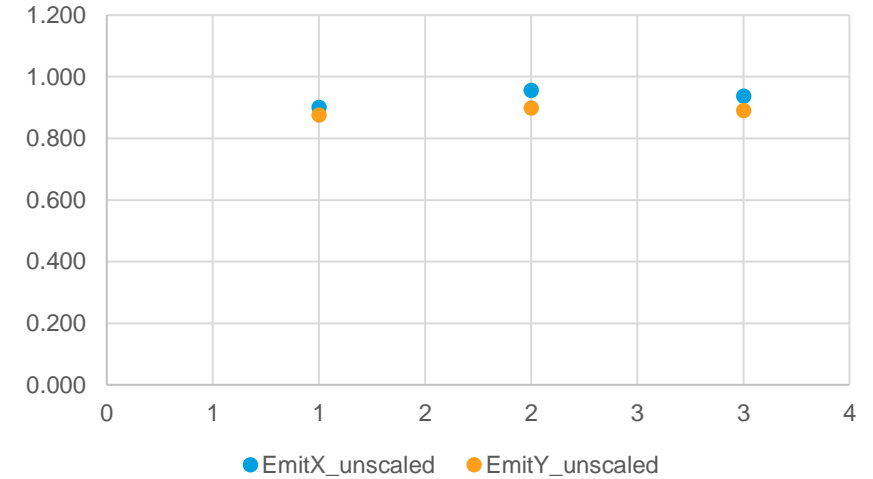
Experiment

Solenoid scan at EMSY2

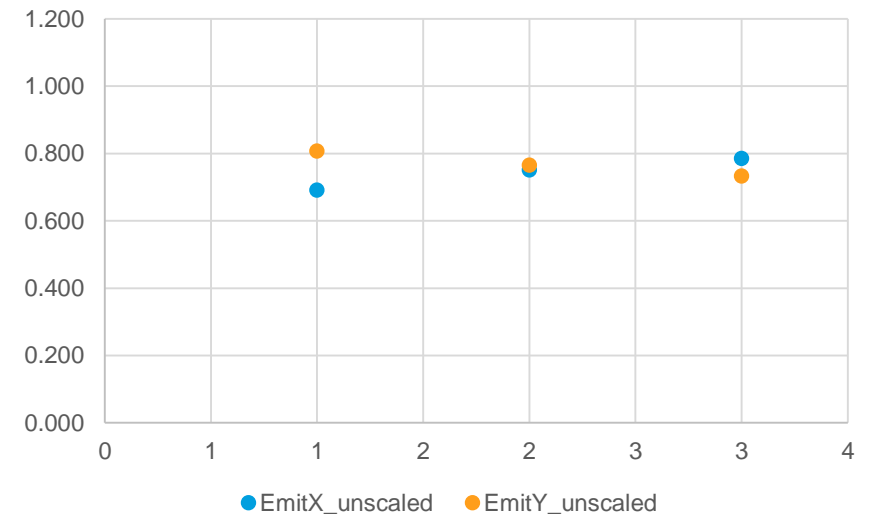


Statistics at I_{main} = 357 A

Without Gun Quads



With Gun Quads Q1+Q2

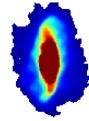


Experiment

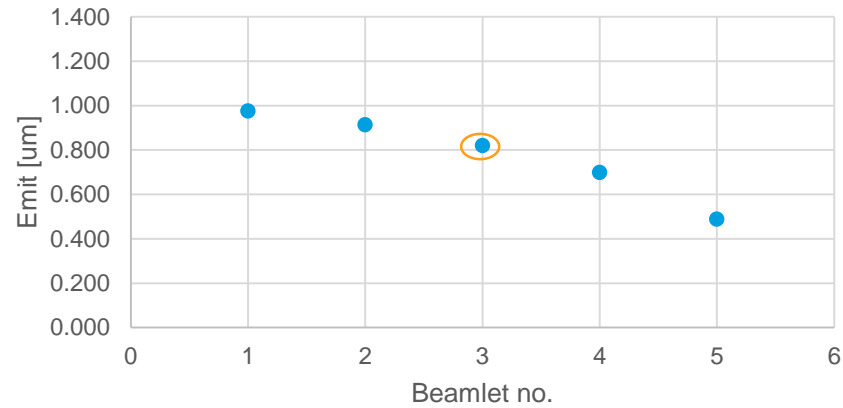
Emittance for 5 beamlets in X and 5 in Y

Without statistics!

Without Gun Quads



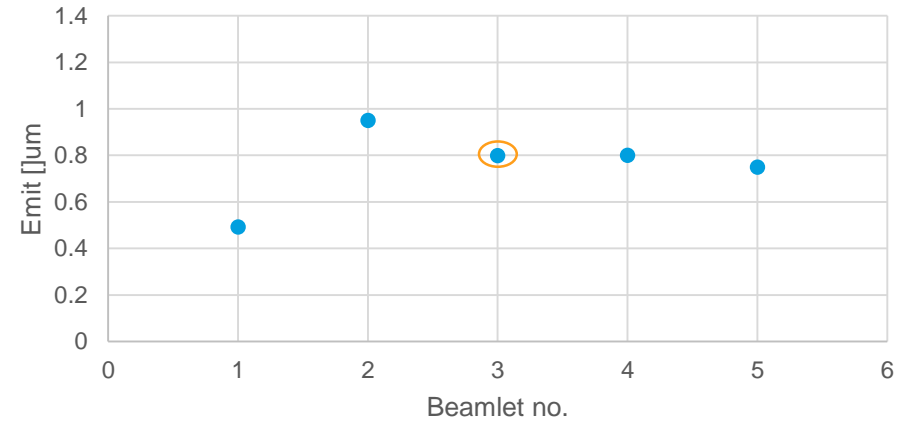
Emit_Xunscaled



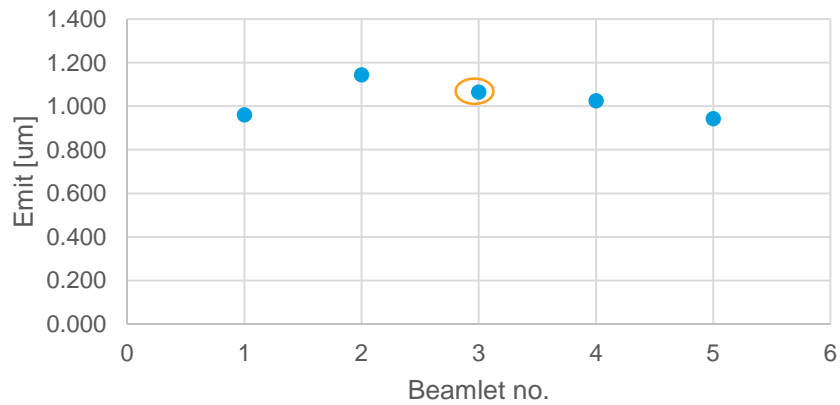
With Gun Quads Q1+Q2



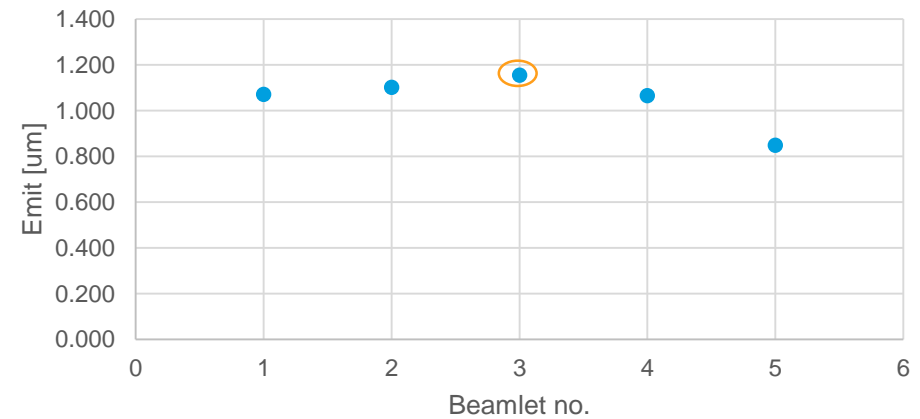
Emit_Xunscaled



Emit_Yunscaled

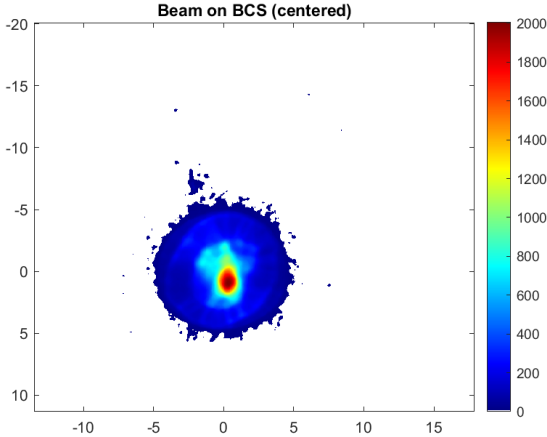
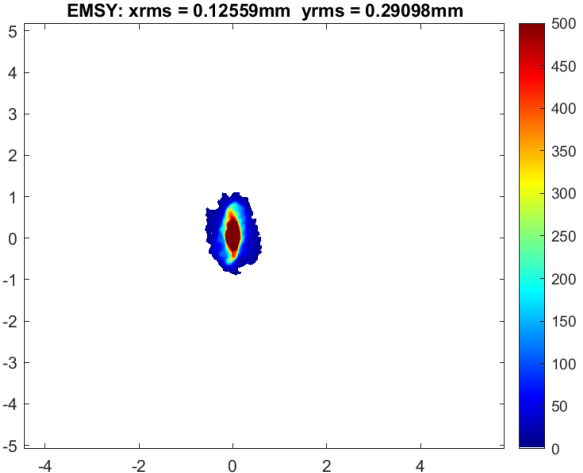


Emit_Yunscaled

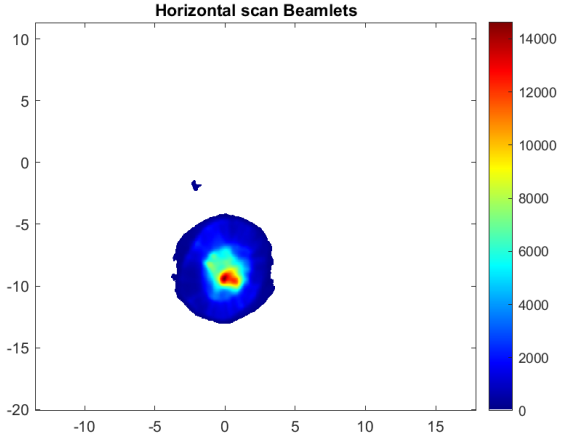


Experimental data without gun quads

Emittance at EMSY2 with Pst.Scr1 as observation screen



Summing beamlets



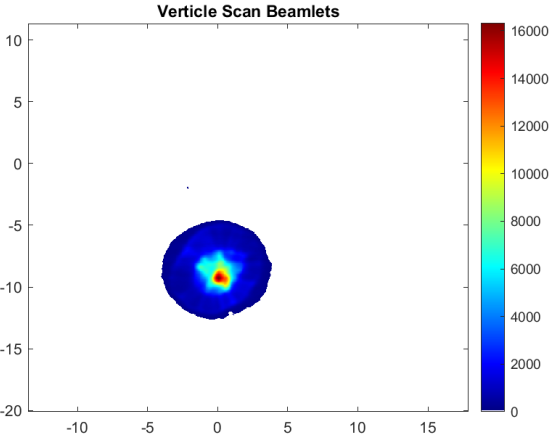
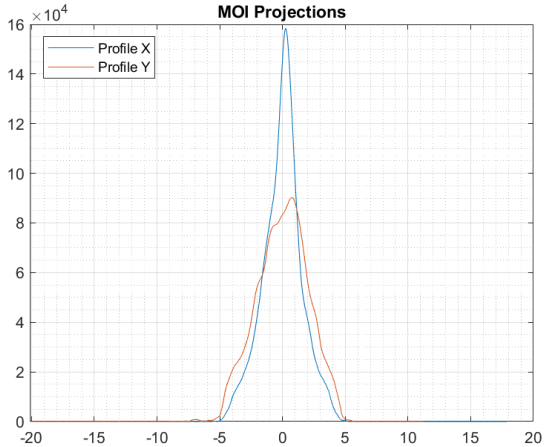
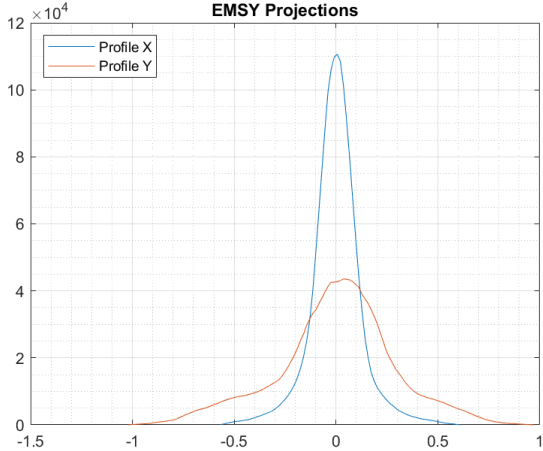
Number of beamlets X = 110

Number of beamlets Y = 125

Slit scan

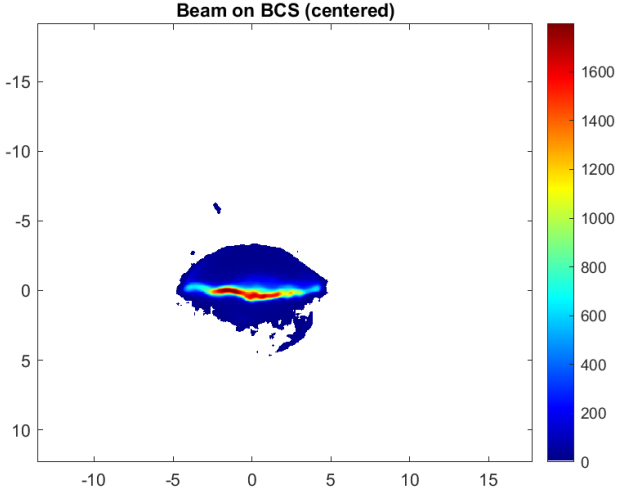
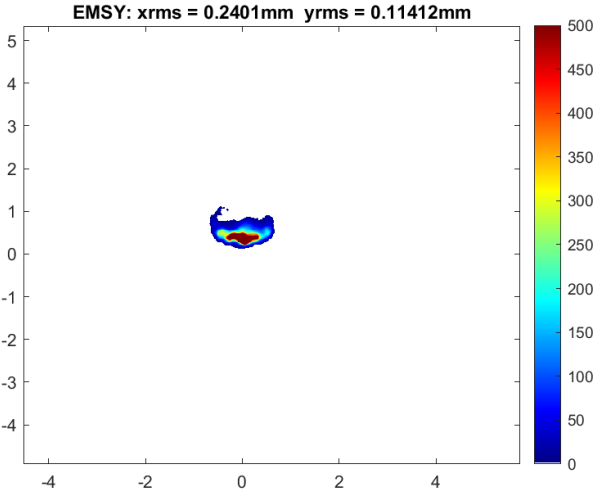
$$\epsilon_x = 0.7348$$

$$\epsilon_y = 0.8406$$

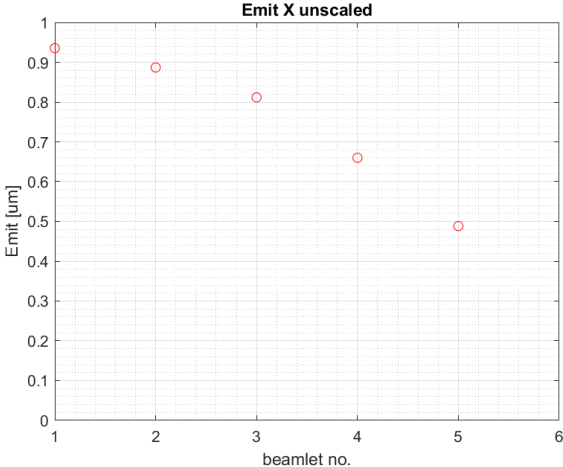
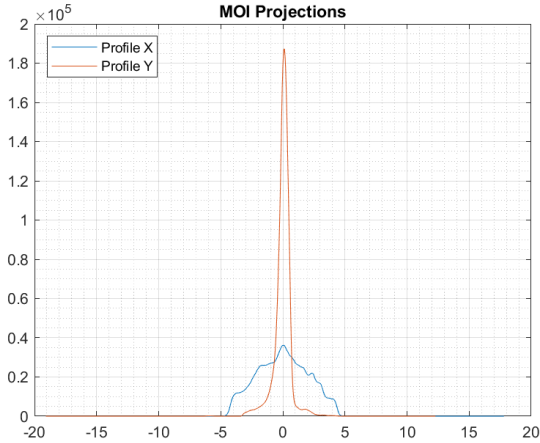
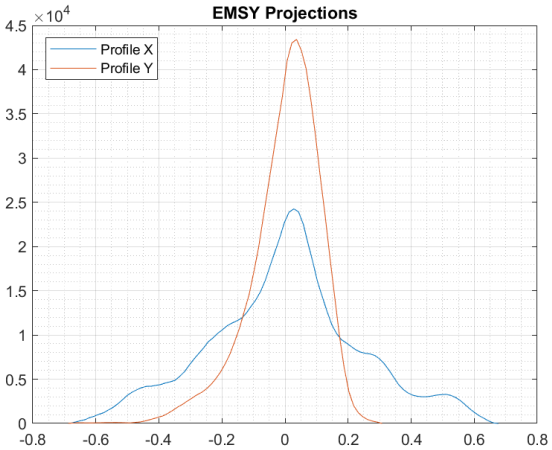
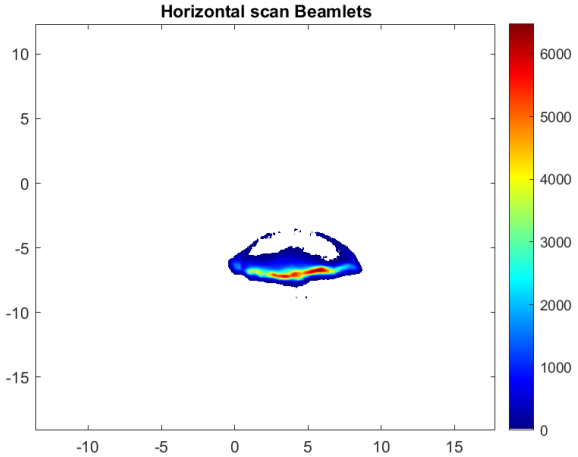


Experimental data without gun quads

EMSY1Y central beamlet +EMSY2X scan +Pst.Scr1

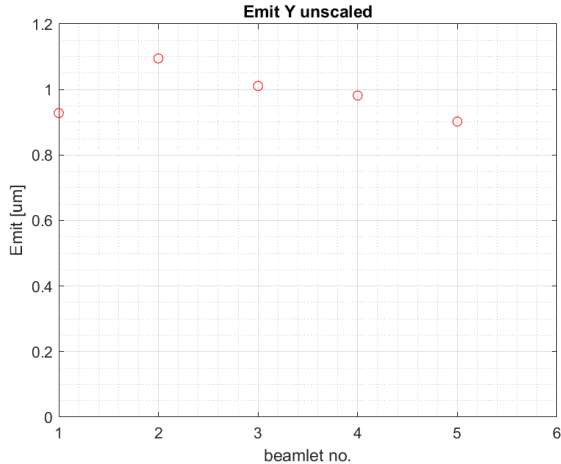
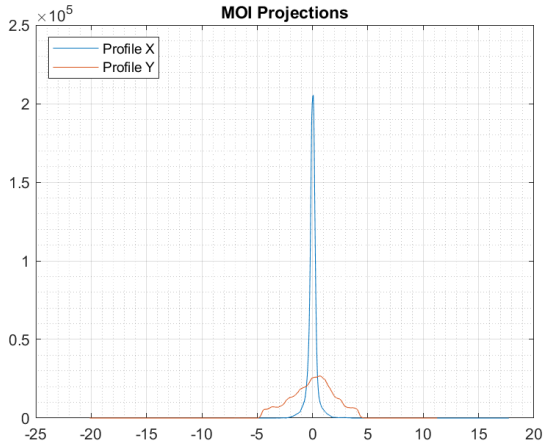
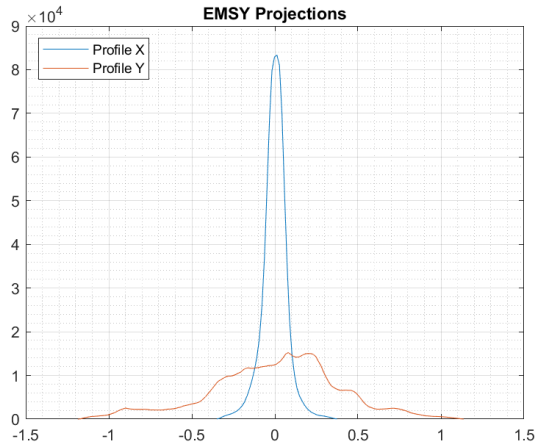
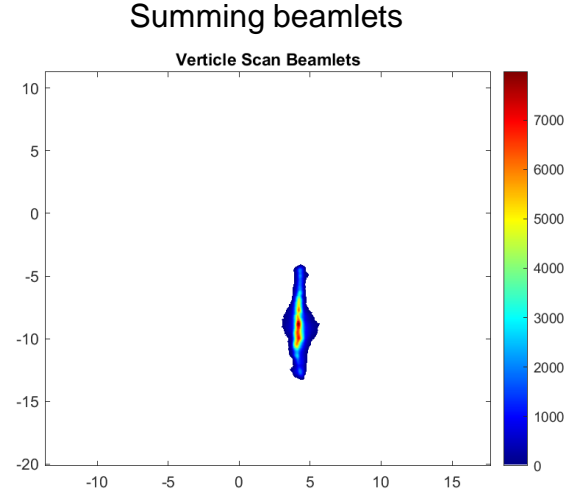
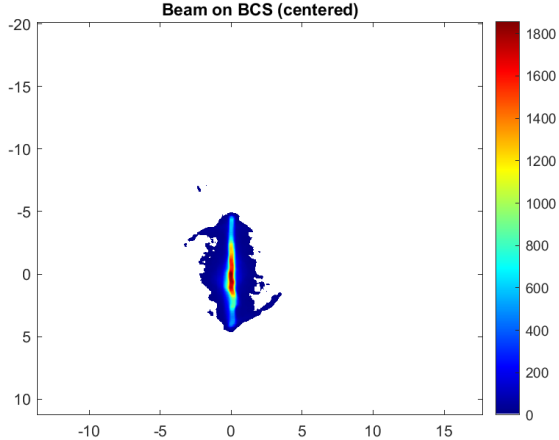
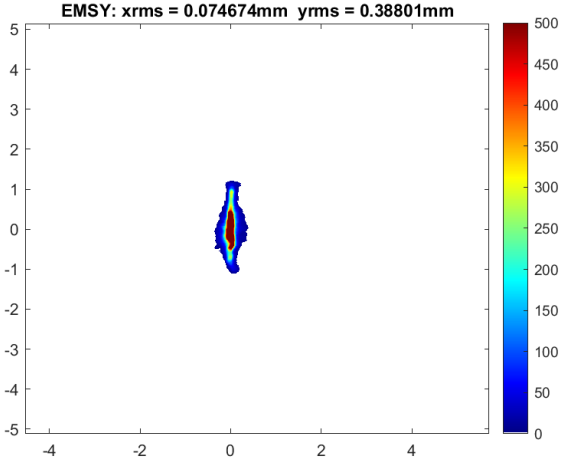


Summing beamlets



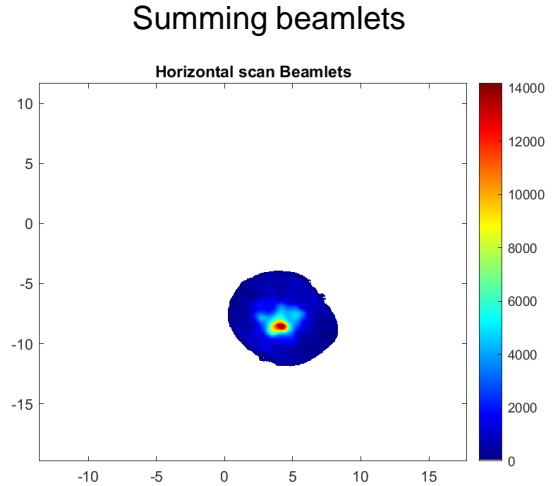
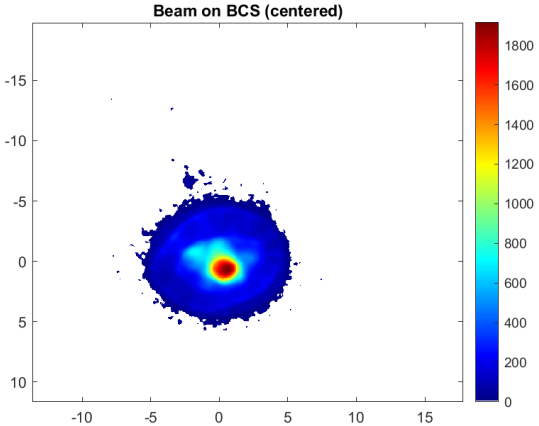
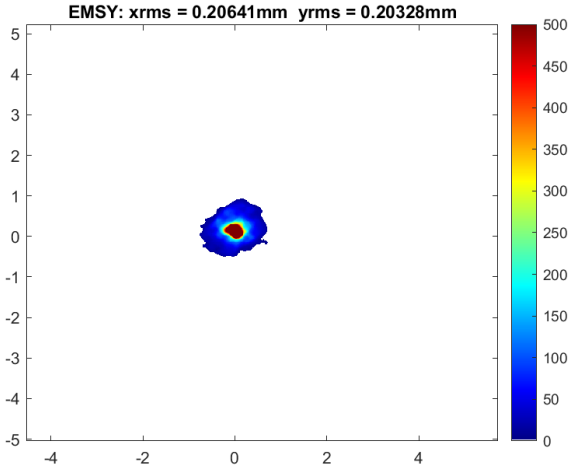
Experimental data without gun quads

EMSY1X central beamlet + EMSY2Y scan + Pst.Scr1



Experimental data with gun quads

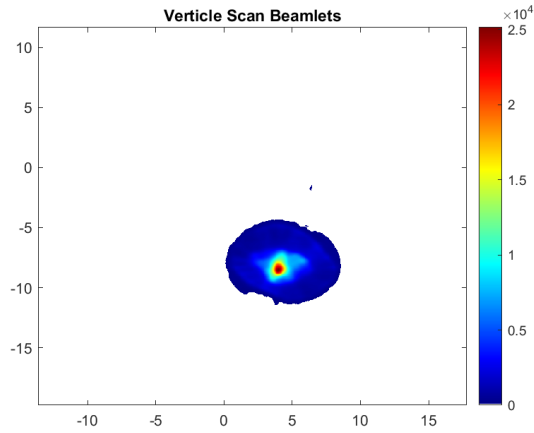
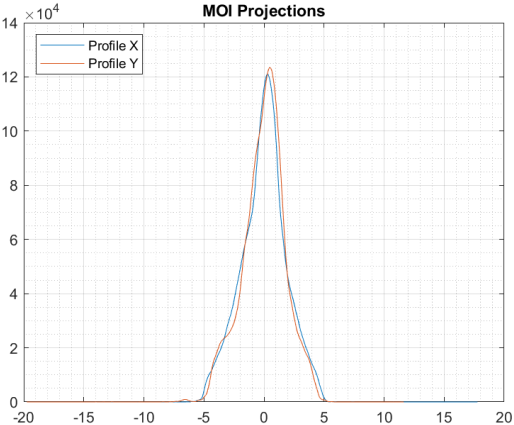
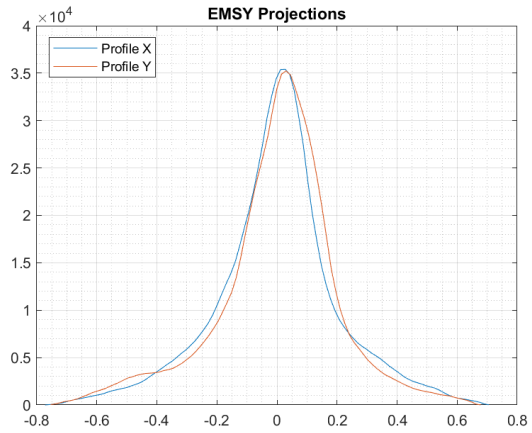
Emittance at EMSY2 with Pst.Scr1 as observation screen



Number of beamlets X = 220

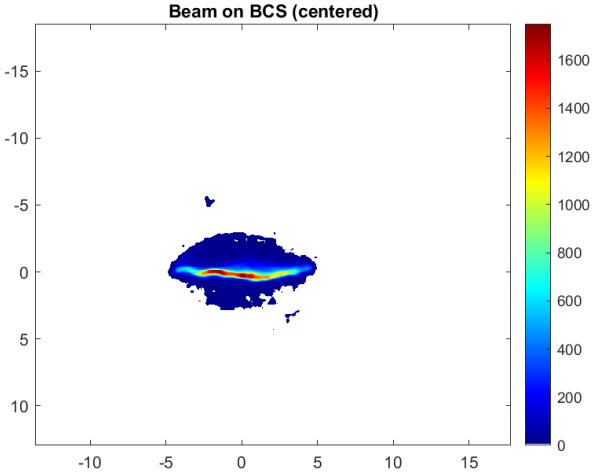
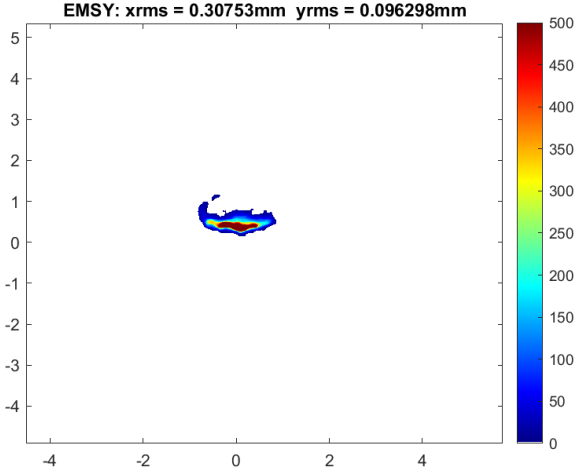
Number of beamlets Y = 250

Slit scan
 $\epsilon_x = 0.7607$
 $\epsilon_y = 0.7386$

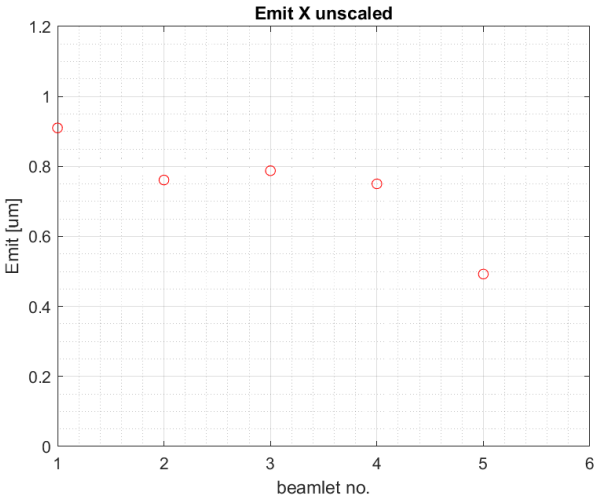
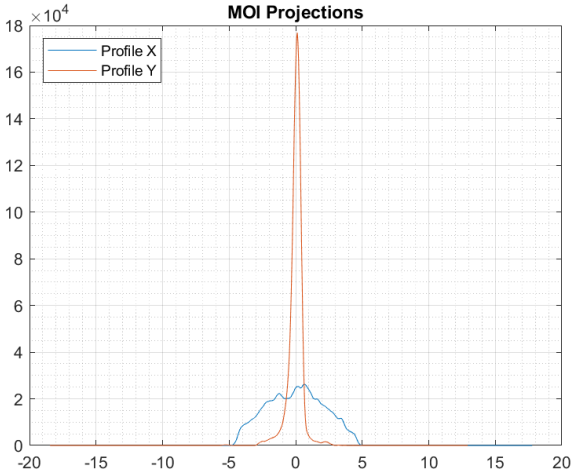
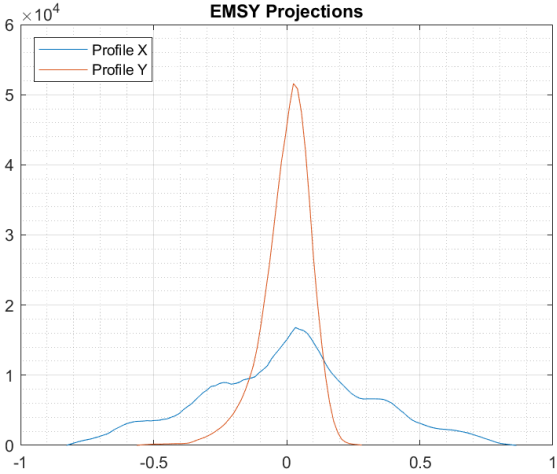
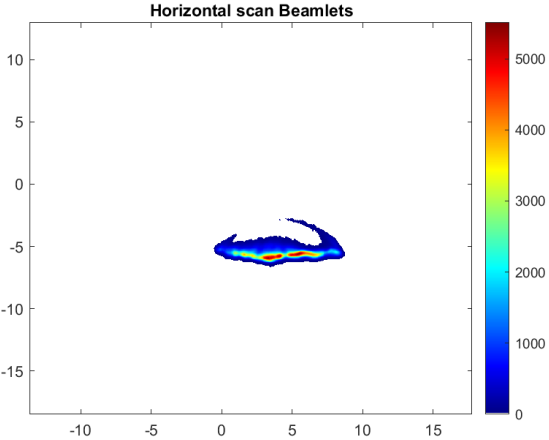


Experimental data with gun quads

EMSY1Y central beamlet +EMSY2X scan +Pst.Scr1

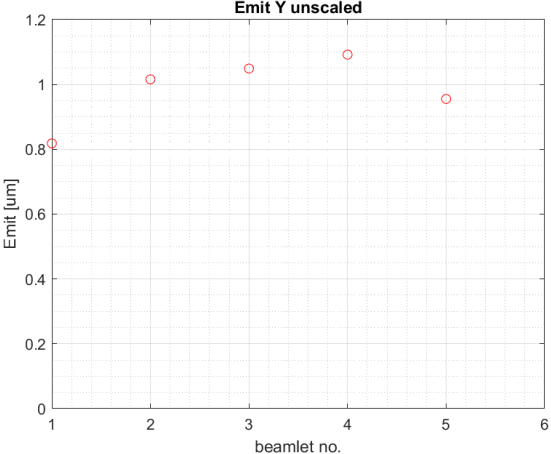
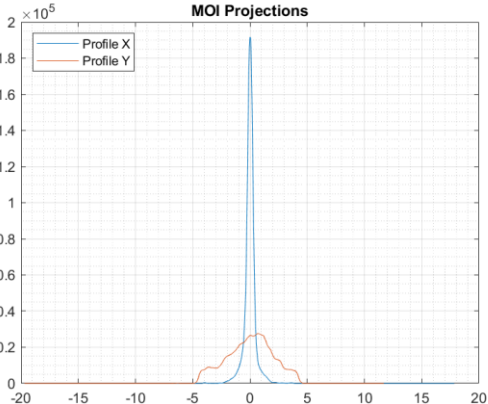
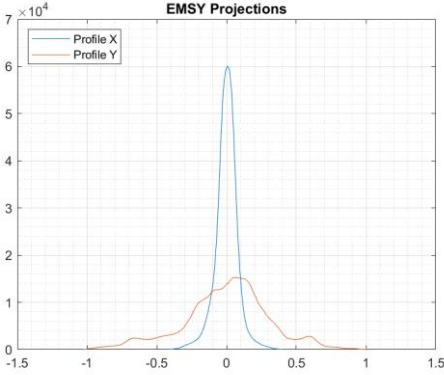
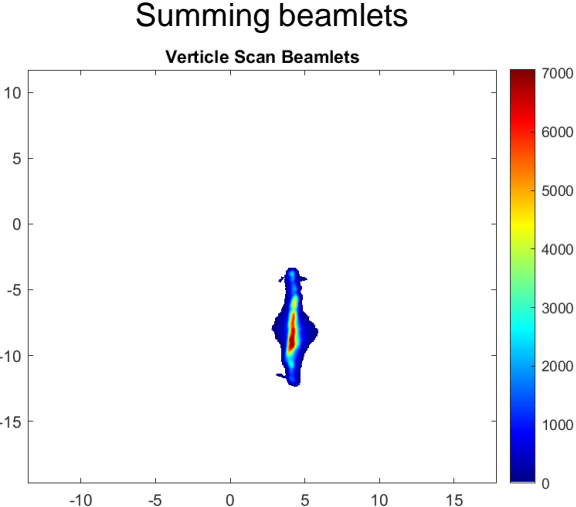
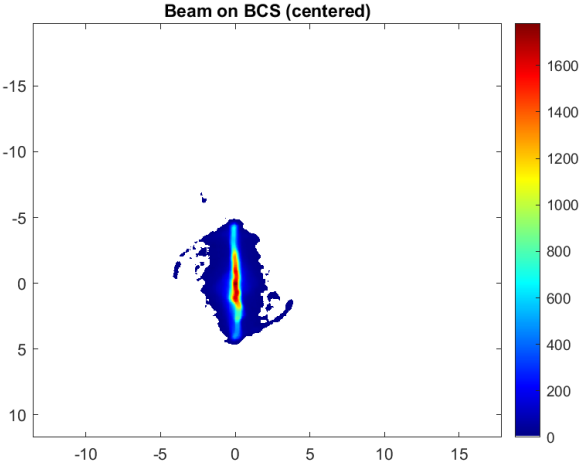
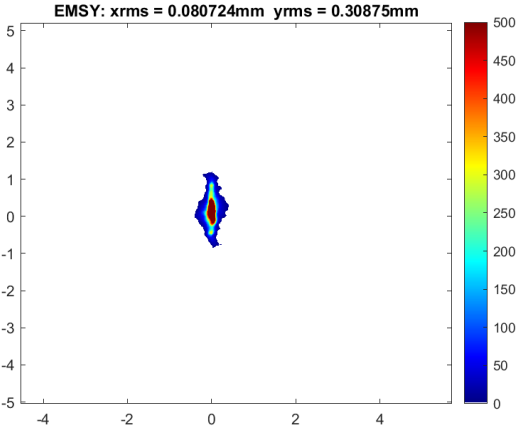


Summing beamlets



Experimental data with gun quads

EMSY1X central beamlet +EMSY2Y scan +Pst.Scr1



Analysis & Outlook

Further Analysis and Data taking

- Foreign particles effect
- Slightly higher emittance for non-central beamlets
- Simulation of non-central beamlets
- More experimental data?
- Using SlitScanner.m using a stop-n-go procedure and do Nemsy1x x Nemsy2y and Nemsy1y x Nemsy2x scans with it.