

~~Transport of the space charge dominated electron beam through the LCLS-I undulator at PITZ~~

Progress Report

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DESY Zeuthen, 08.08.2019

Outline

- Introduction
 - The LCLS-I undulator & field
 - Motivation & goals
- Single particle simulations
 - Methodology & simulation setup (ASTRA code)
 - Results
- Electron beam simulations (w/o space charge)
 - Methodology & simulation setup (ASTRA code)
 - Results
- Summary & Outlook

Introduction

The LCLS-I undulator

Properties of the LCLS-I undulator

Properties	Details
Type	fixed gap planar hybrid (NdFeB)
Nominal gap	6.8 mm
K-value	3.49
Support diameter / length	30 cm / 3.4 m
Vacuum chamber size	11 mm x 5 mm
Period length	30 mm
Poles / a module	226 poles (= 113 periods, 3.4 m)
Total weight w/o vac. chamber	1000 kg

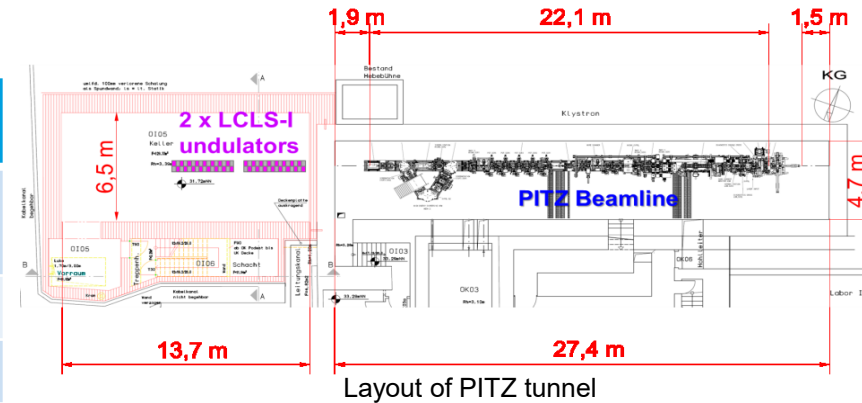


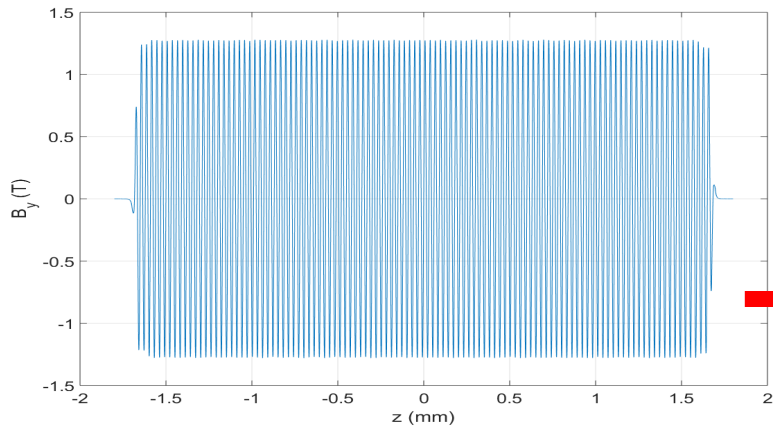
Figure of the LCLS-I undulator

Reference: LCLS conceptual design report, SLAC-0593, 2002.

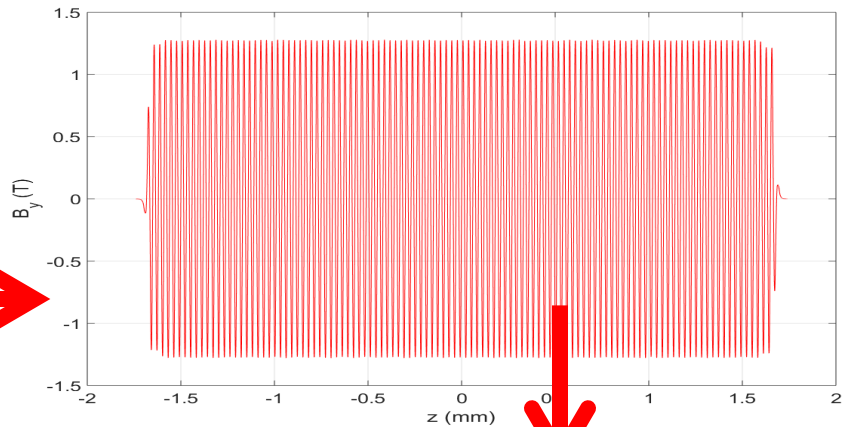
Introduction

Magnetic field of the LCLS-I undulator

Measurement field



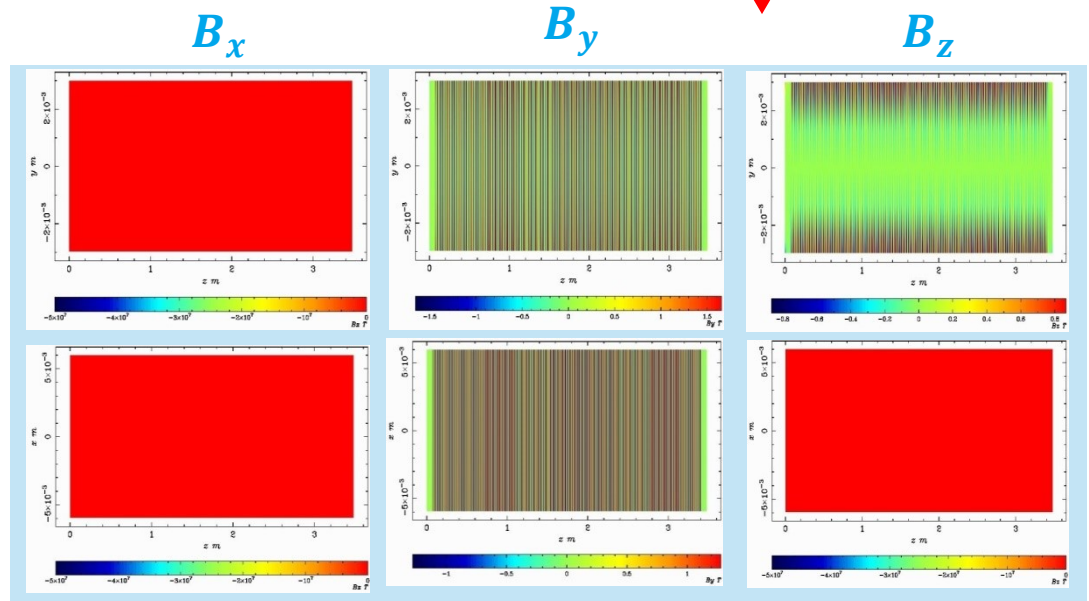
Reconstruction field



3D field

yz plane
at $x = 0$ mm

xz plane
at $y = 0$ mm



Introduction

Motivation & goals

Optimize input beam which have least beam lost when traveling through the undulator.

x_{rms}	horizontal rms beam size
y_{rms}	vertical rms beam size
cor_px	horizontal correlated divergence of bunch
cor_py	vertical correlated divergence of bunch

Goals

- Determine function of $cor_px(x_{rms})$ and $cor_py(y_{rms})$ which deliver the minimum Goal Function (GF)*.
- Determine function of $x'_0(x_0)$ and $y'_0(y_0)$ which deliver the minimum GF.

Tracking electron beam takes long simulation time. → Track single electron first.

ASTRA input file

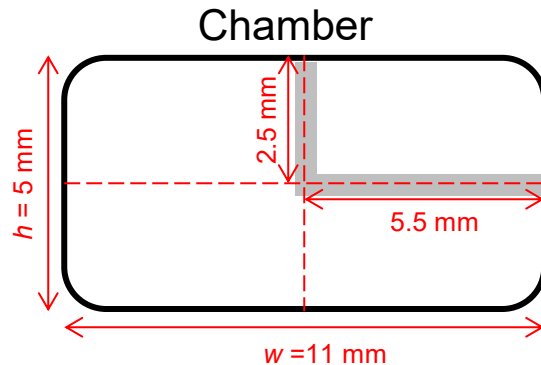
```
UBy667.in - Notepad
File Edit Format View Help
&NEWRUN
Head='LCLS-I undulator transport'
RUN=1
Distribution = 'beamLP.ini',
TRACK_ALL=.T,
TRACK_ON_AXIS=.F
CHECK_REF_PART=.F
Auto_phase=T
Zoff=0
H_max=0.0003,
H_min=0.00
Xrms=1.5
cor_px=-0.753
Yrms=0.7
cor_py=-11
/
&OUTPUT
ZSTART=0.0, ZSTOP=3.75
Zemit=4000, Zphase=5
RefS=T
```

x'_0 : horizontal trajectory angle y'_0 : vertical trajectory angle

*The GF represents the area under the electron trajectory.

Single particle simulations

Methodology & Simulation setup



Scan on x-axis

$x_0 = 0$ to 5.4 mm (0.1 mm step size)

$y_0 = 0 \text{ mm}$

$x'_0 = -2.1$ to 0.4 mrad (0.1 mrad step size)

$y'_0 = 0 \text{ mrad}$

Scan on y-axis

$x_0 = 0 \text{ mm}$

$y_0 = 0$ to 2.4 mm (0.1 mm step size)

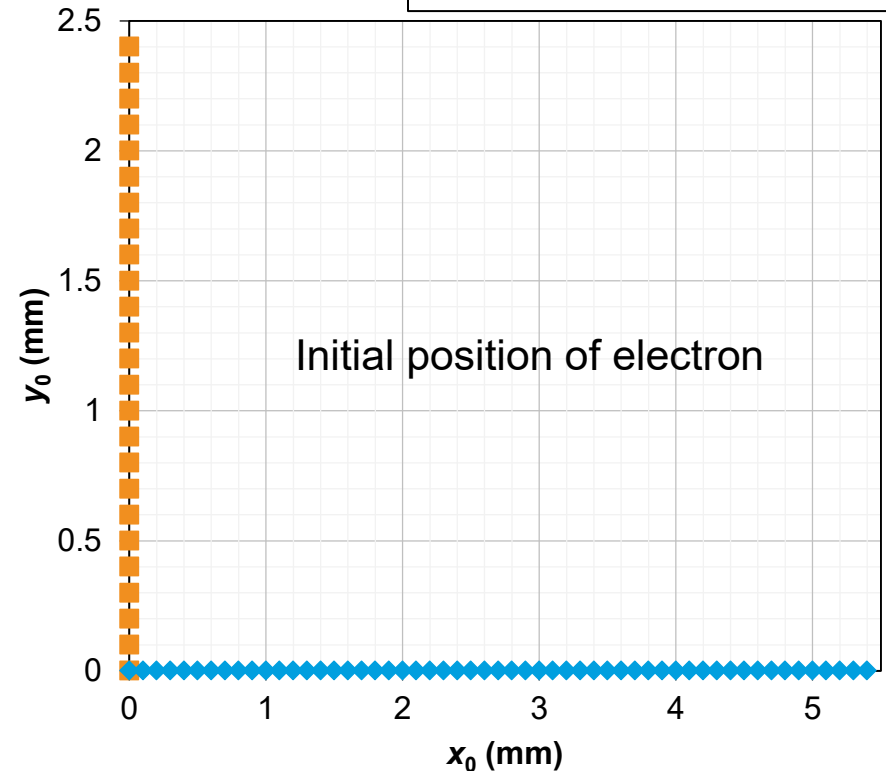
$x'_0 = 0 \text{ mrad}$

$y'_0 = -11.2$ to 0.3 mrad (0.1 mrad step size)

Then track the electron from $z = 0$ to $z = 3.4 \text{ m}$

x'_0 : horizontal trajectory angle y'_0 : vertical trajectory angle

e^- with $p_z = 17.14 \text{ MeV}/c$



Goals

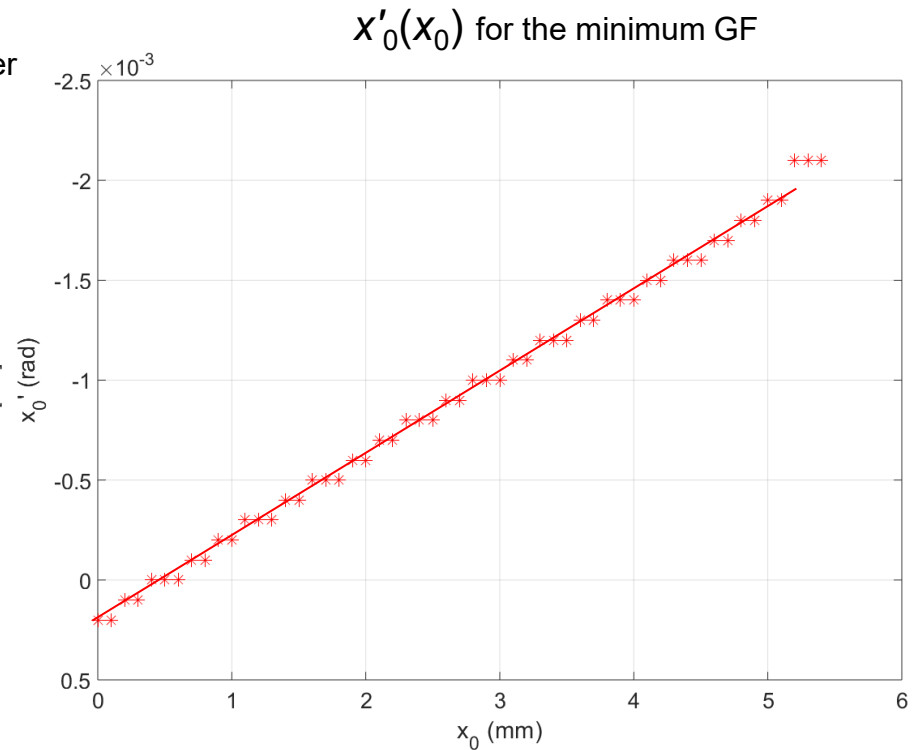
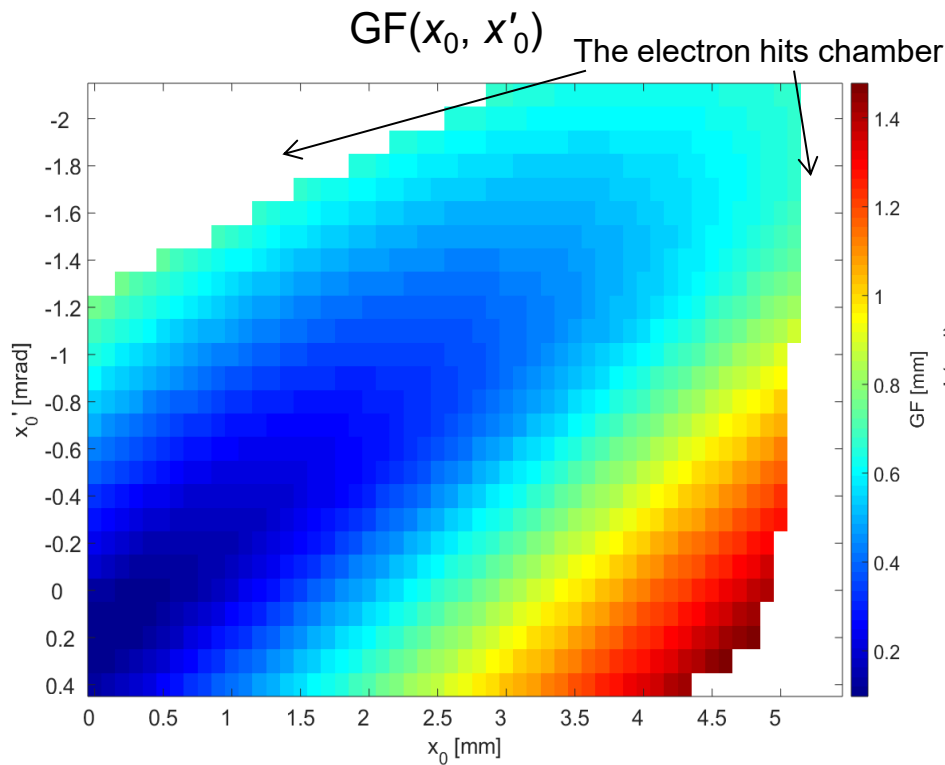
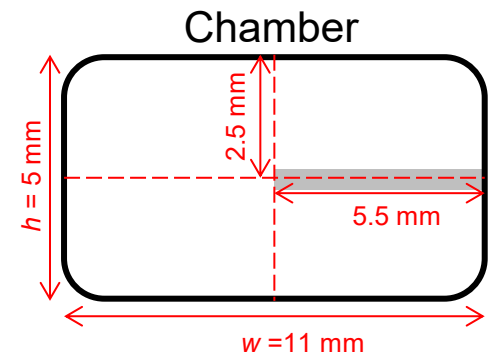
- Determine function of $x'_0(x_0)$ and $y'_0(y_0)$ which deliver the minimum GF.

$$GF = \int \frac{|x(z)| dz}{w} + \int \frac{|y(z)| dz}{h}$$

Single particle simulations

Results

Scan on x-axis



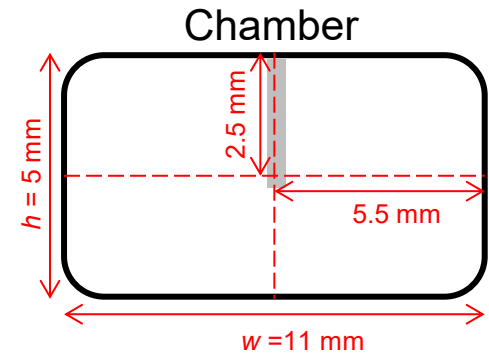
$$x'_0 [\text{mrad}] = -0.4x_0 [\text{mm}] + 0.2$$

$$R^2 = 0.9978$$

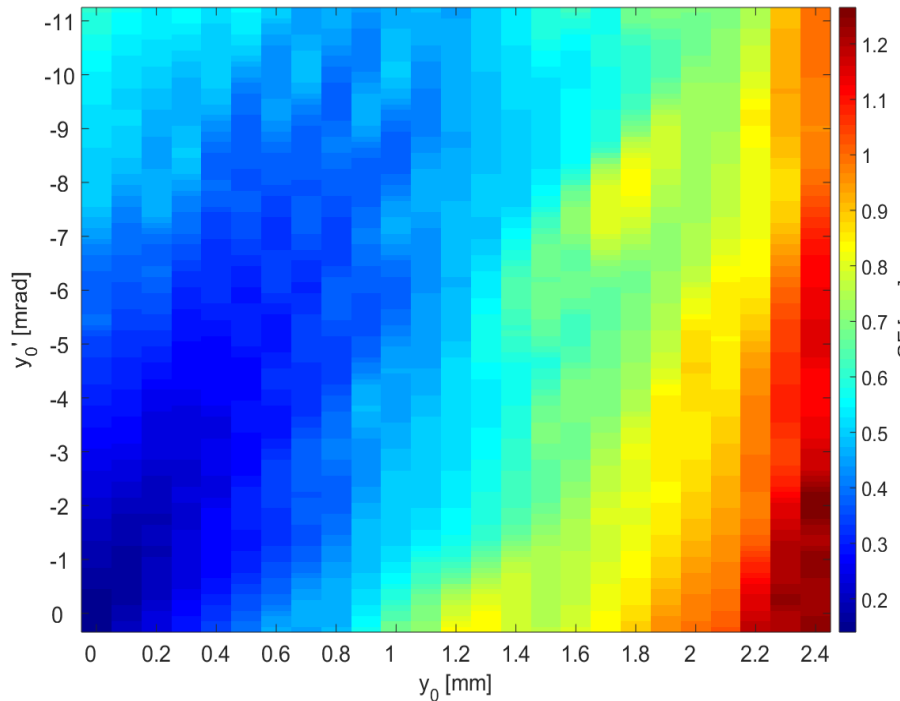
Single particle simulations

Results

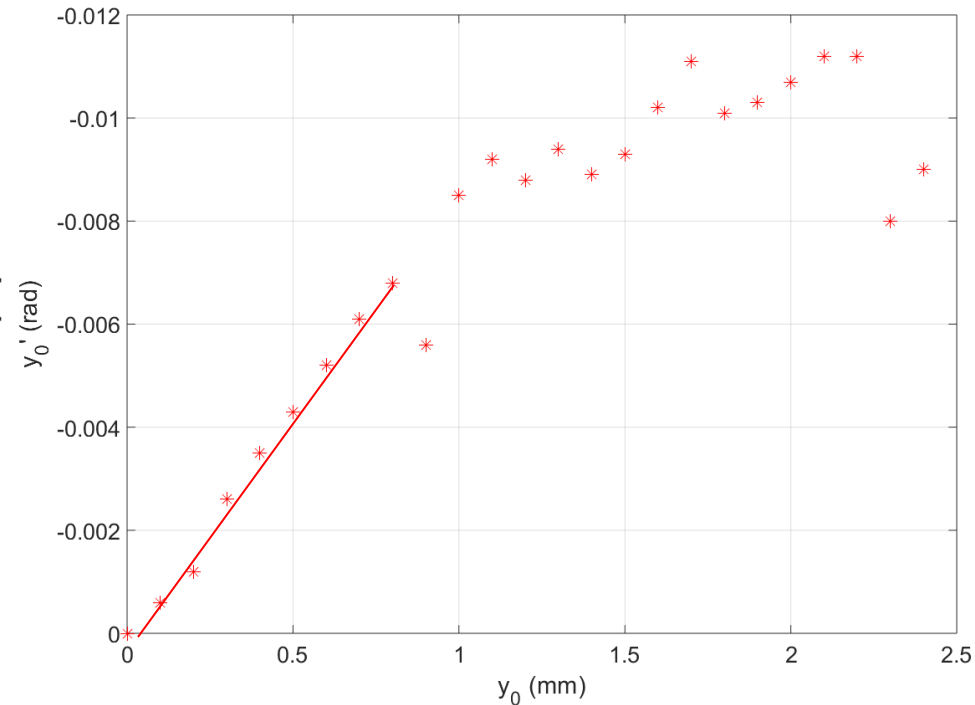
Scan on y -axis



$GF(y_0, y'_0)$



$y'_0(y_0)$ for the minimum GF



$$y'_0 [\text{mrad}] = -8.9y_0 [\text{mm}] + 0.2$$

$$R^2 = 0.9947$$

Electron beam simulations

Methodology & Simulation setup (ASTRA code)

beam with $p_z = 17.14 \text{ MeV}/c$

$$x'_0 [\text{mrad}] = -0.4x_0 [\text{mm}] + 0.2$$

\downarrow \downarrow
 cor_px x_{rms}

$$y'_0 [\text{mrad}] = -8.9y_0 [\text{mm}] + 0.2$$

\downarrow \downarrow
 cor_py y_{rms}

1st step

$x_{rms} = 0.5$ to 2.5 mm (0.1 mm step size)
 $y_{rms} = 0.5 \text{ mm}$
 $cor_px = -2.1$ to 0.4 mrad (0.1 mrad step size)
 $cor_py = 0 \text{ mrad}$

2nd step

$x_{rms} = 1.5 \text{ mm}$
 $y_{rms} = 0.1$ to 1.2 mm (0.1 mm step size)
 $cor_px = -0.753 \text{ mrad}$ ($cor_px(x_{rms})$ 1st)
 $cor_py = -11$ to 0 mrad (0.1 mrad step size)

3rd step

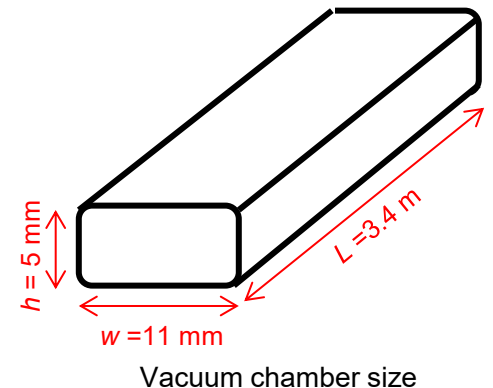
$x_{rms} = 0.1$ to 2.5 mm (0.1 mm step size)
 $y_{rms} = 0.1$ to 1.2 mm (0.1 mm step size)
 $cor_px = cor_px(x_{rms})$ 1st
 $cor_py = cor_py(y_{rms})$ 2nd

Then track the electron beam from $z = 0$ to $z = 3.4 \text{ m}$ (w/o space charge)

Goals

- Determine function of $cor_px(x_{rms})$ and $cor_py(y_{rms})$.
- Minimum Goal Function (GF).

$$GF = \int \frac{x_{rms}(z) dz}{w \cdot L} + \int \frac{y_{rms}(z) dz}{h \cdot L}$$

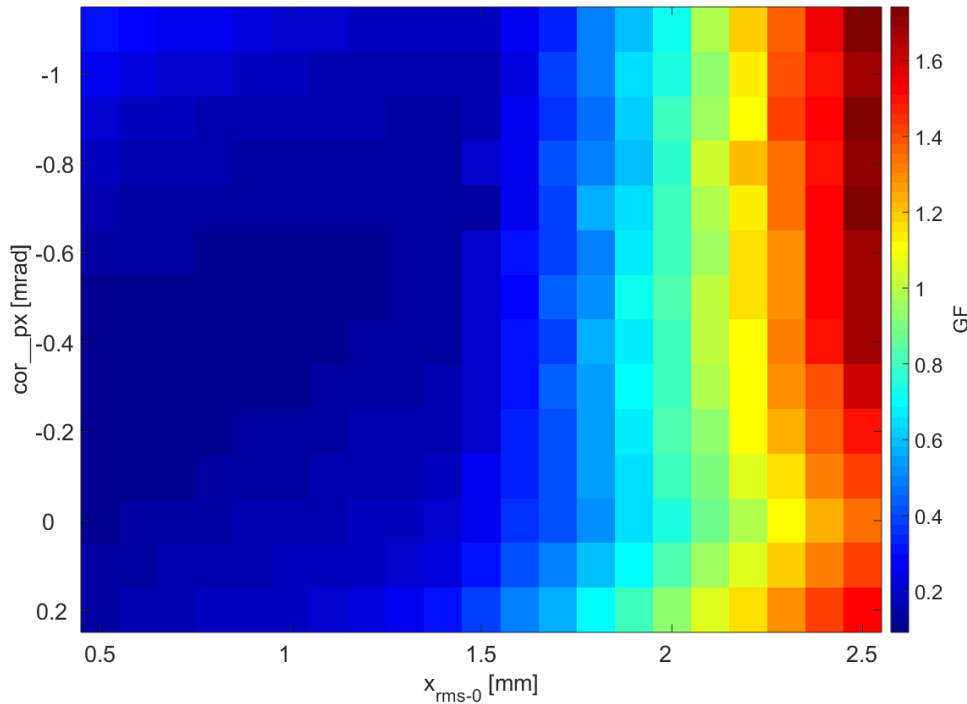


Electron beam simulations

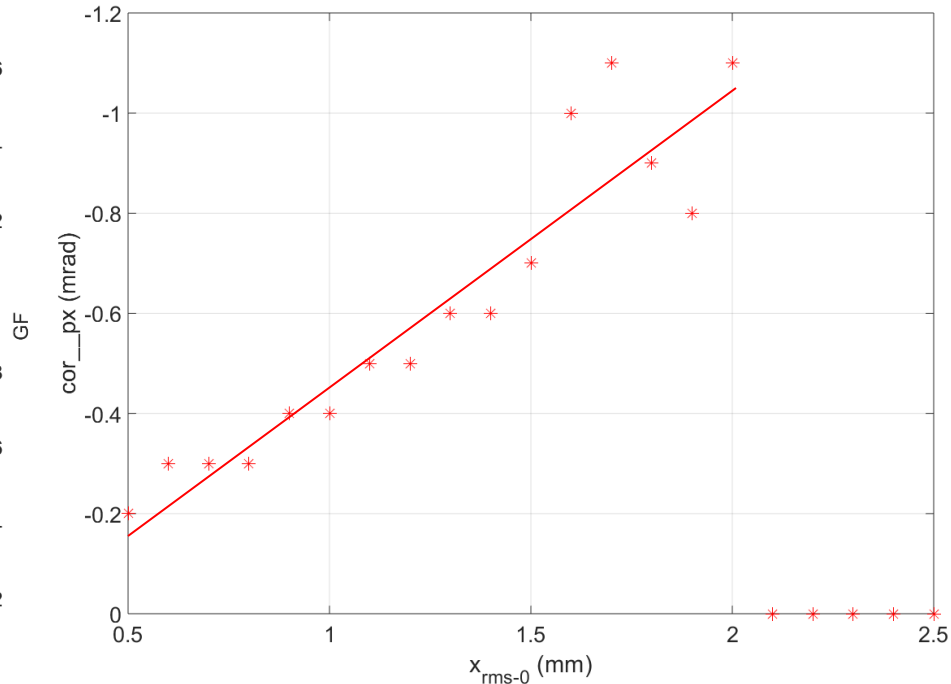
Without space charge

1st step

$GF(x_{rms-0}, cor_px)$



$cor_px(x_{rms-0})$ for the minimum GF



$$cor_px[mrad] = -0.59x_{rms-0}[mm] + 0.13$$

$$R^2 = 0.88$$

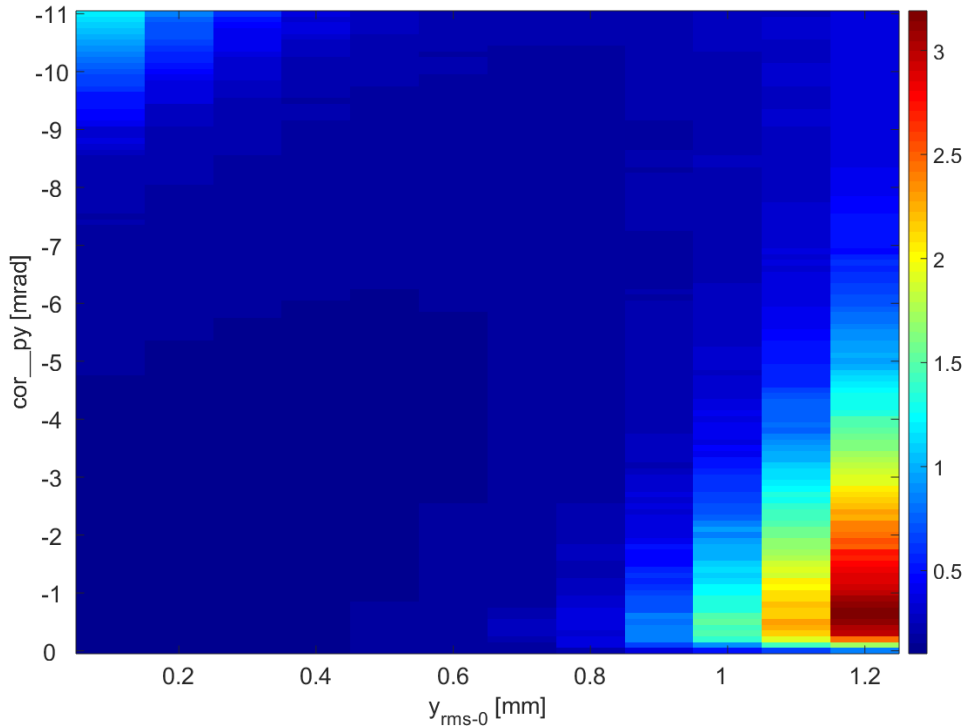
Electron beam simulations

Without space charge

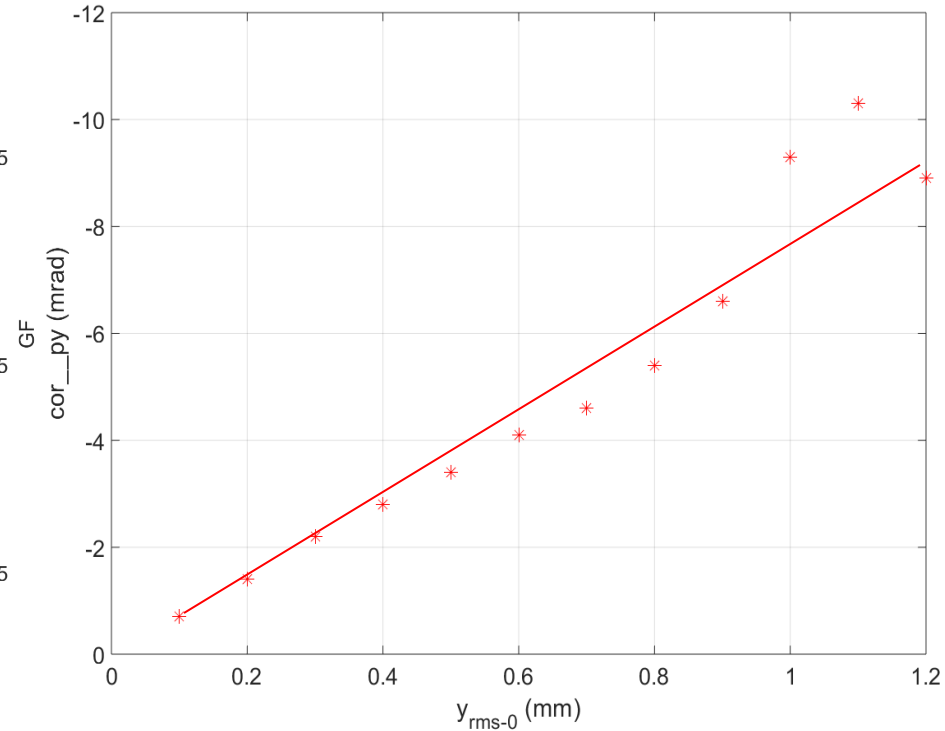
2nd step

from 1st step: $x_{\text{rms}} = 1.5 \text{ mm}$
 $cor_px = -0.753$

$GF(y_{\text{rms-0}}, cor_py)$



$cor_py(y_{\text{rms-0}})$ for the minimum GF



$$cor_py[mrad] = -8.58y_{\text{rms-0}}[mm] + 0.60$$

$$R^2 = 0.94$$

Electron beam simulations

Without space charge

3rd step

from 1st step:

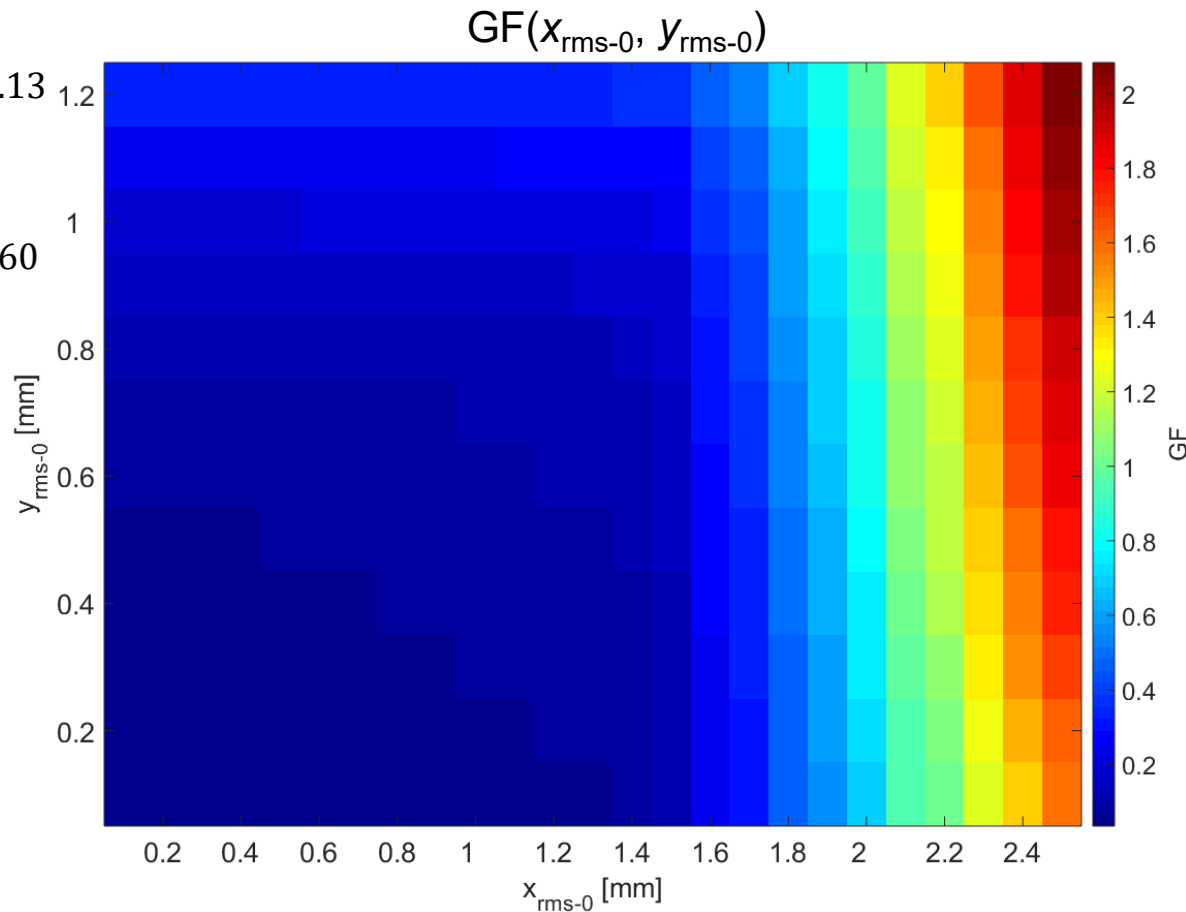
$$cor_px[mrad] = -0.59x_{rms-0}[mm] + 0.13$$

from 2nd step:

$$cor_py[mrad] = -8.58y_{rms-0}[mm] + 0.60$$

Small rms beam size → small GF

**Simulations with space charge
may get a different conclusion!**



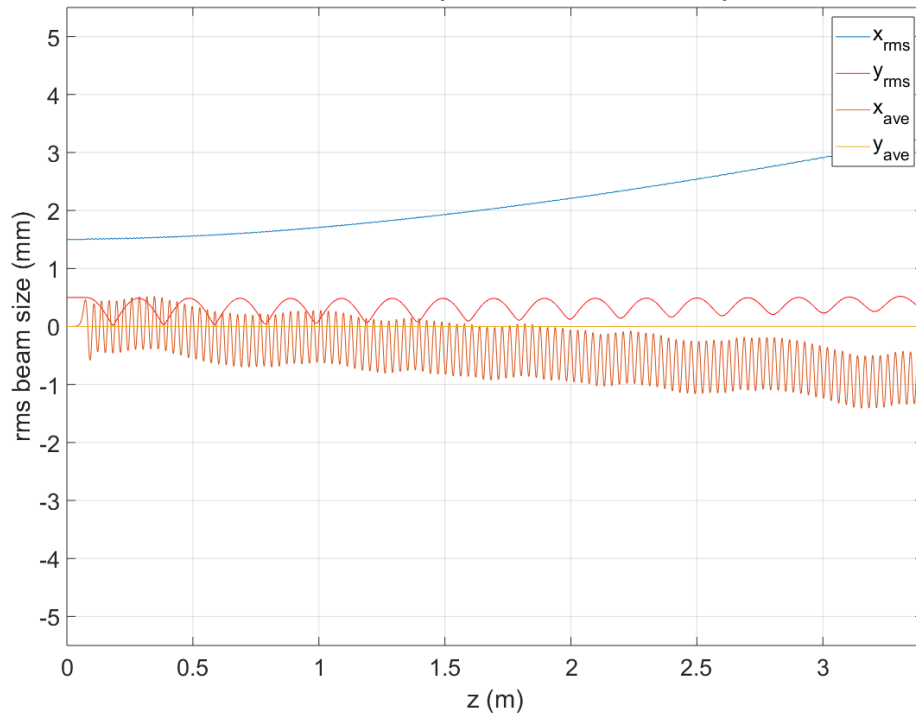
Electron beam simulations

Without space charge

beam with $p_z = 17.14$ MeV/c

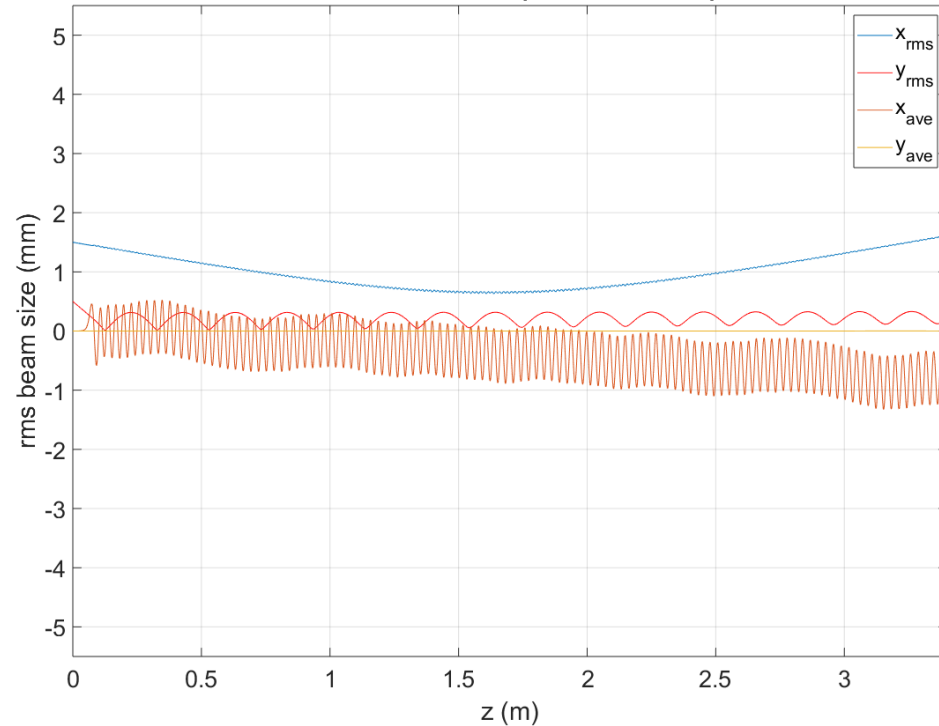
Compare rms beam size along the undulator

0th step (non-optimize)



$x_{rms} = 1.5$ mm
 $y_{rms} = 0.5$ mm
 $cor_{px} = 0$
 $cor_{py} = 0$

3rd step (optimize)



$x_{rms} = 1.5$ mm
 $y_{rms} = 0.5$ mm
 $cor_{px} = -0.753$ mrad ($cor_{px}(x_{rms})$ from 1st step)
 $cor_{py} = -3.687$ mrad ($cor_{py}(y_{rms})$ from 2nd step)

Summary

Single particle simulations

- x'_0 as a function of x_0 which delivers the minimum GF is $x'_0[mrad] = -0.4x_0[mm] + 0.2$
- y'_0 as a function of y_0 which delivers the minimum GF is $y'_0[mrad] = -8.9y_0[mm] + 0.2$

Electron beam simulations

- cor_px as a function of x_{rms-0} which delivers the minimum GF is
$$cor_px[mrad] = -0.59x_{rms-0}[mm] + 0.13$$
- cor_py as a function of y_{rms-0} which delivers the minimum GF is
$$cor_py[mrad] = -8.58y_{rms-0}[mm] + 0.60$$

Outlook

- Perform electron beam simulations with space charge.
- Determine the tolerants of x_{rms-0} , y_{rms-0} , cor_px and cor_py

Thank you

Backup

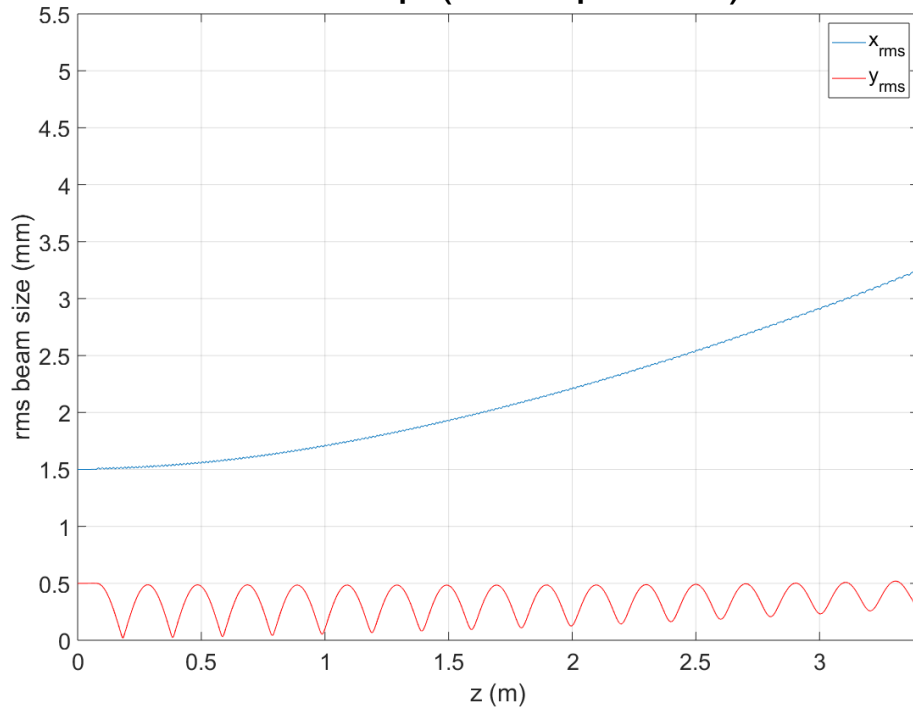
Electron beam simulations

Without space charge

beam with $p_z = 17.14$ MeV/c

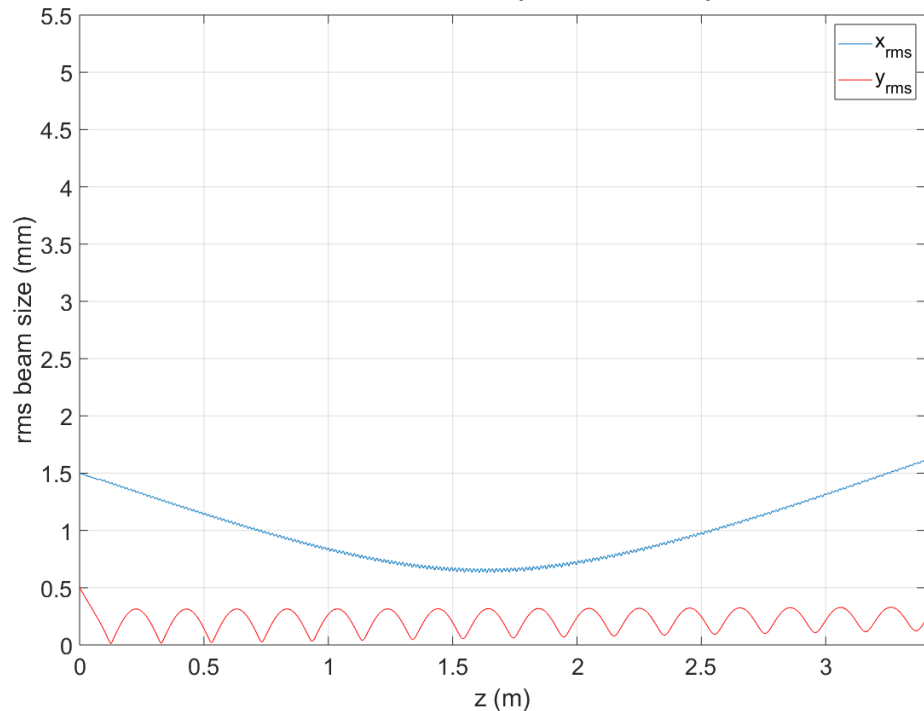
Compare rms beam size along the undulator

0th step (non-optimize)



$x_{rms} = 1.5$ mm
 $y_{rms} = 0.5$ mm
 $cor_{px} = 0$
 $cor_{py} = 0$

3rd step (optimize)



$x_{rms} = 1.5$ mm
 $y_{rms} = 0.5$ mm
 $cor_{px} = -0.753$ mrad ($cor_{px}(x_{rms})$ from 1st step)
 $cor_{py} = -3.687$ mrad ($cor_{py}(y_{rms})$ from 2nd step)

Outlook

- Simulation electron beam with space charge.
- Optimize parameters number of harmonics and number of magnetic field period. Then follow the steps of single particle simulations and electron beam simulations.
- Fine the tolerant of x_{rms0} and y_{rms0}

Introduction

Magnetic field of the LCLS-I undulator

Undulator Magnetic Field in 3 Dimensions

B_x

B_y

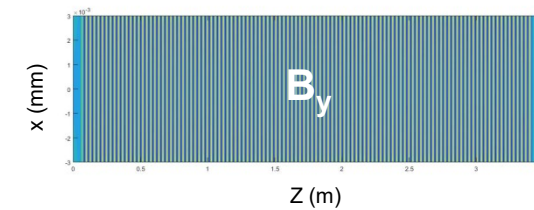
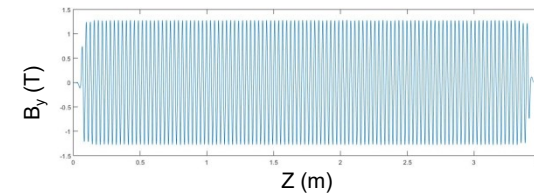
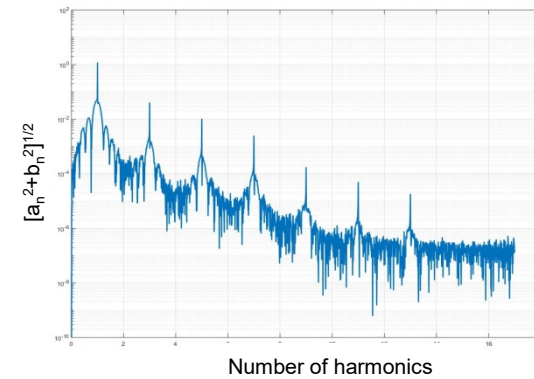
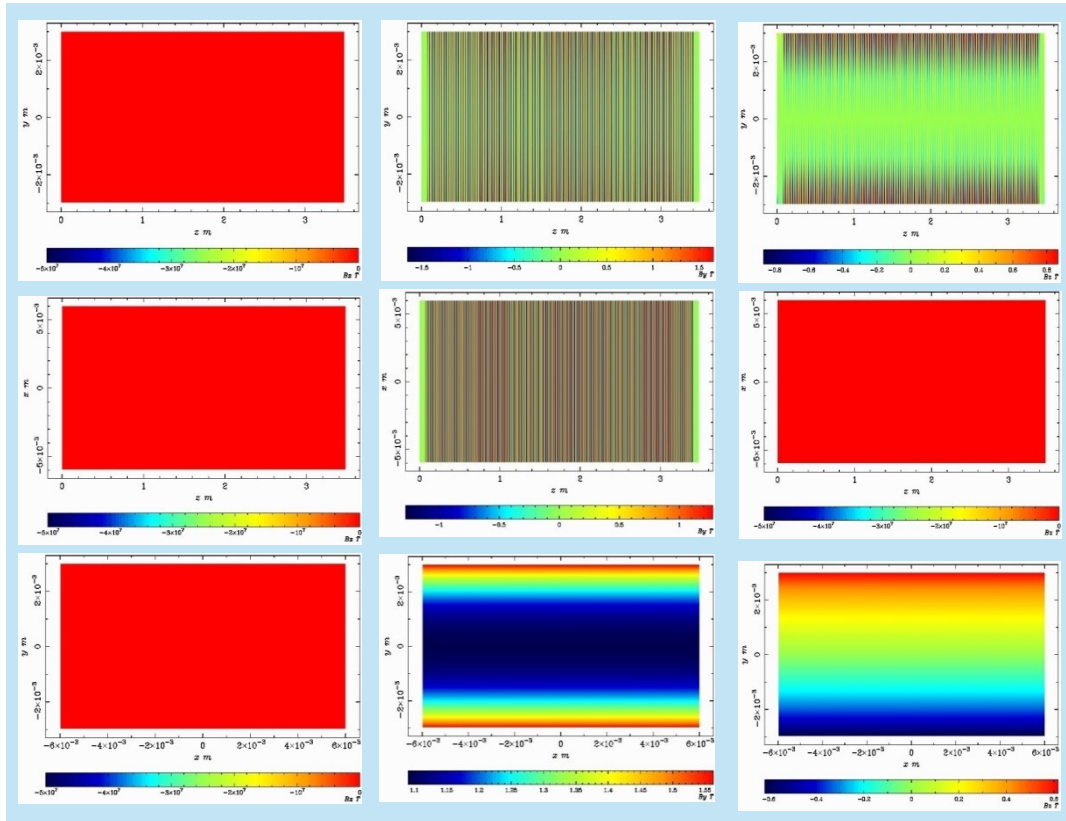
B_z

of harmonics = 17
of undulator field period = 116

along z-axis
and y-axis
at $x = 0$ mm

along z-axis
and x-axis
at $y = 0$ mm

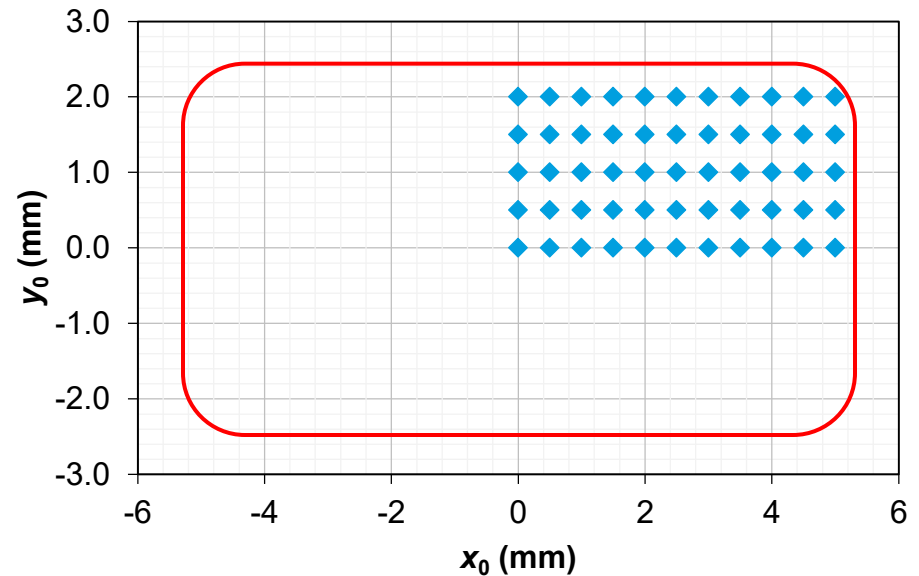
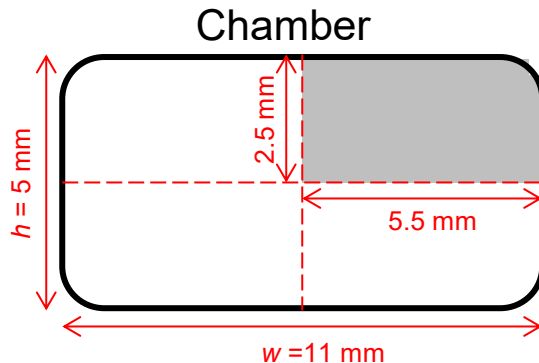
along x-axis
and y-axis
at $z = 2$ m



Single particle simulations

Methodology & Simulation setup

Rough scan



Goals

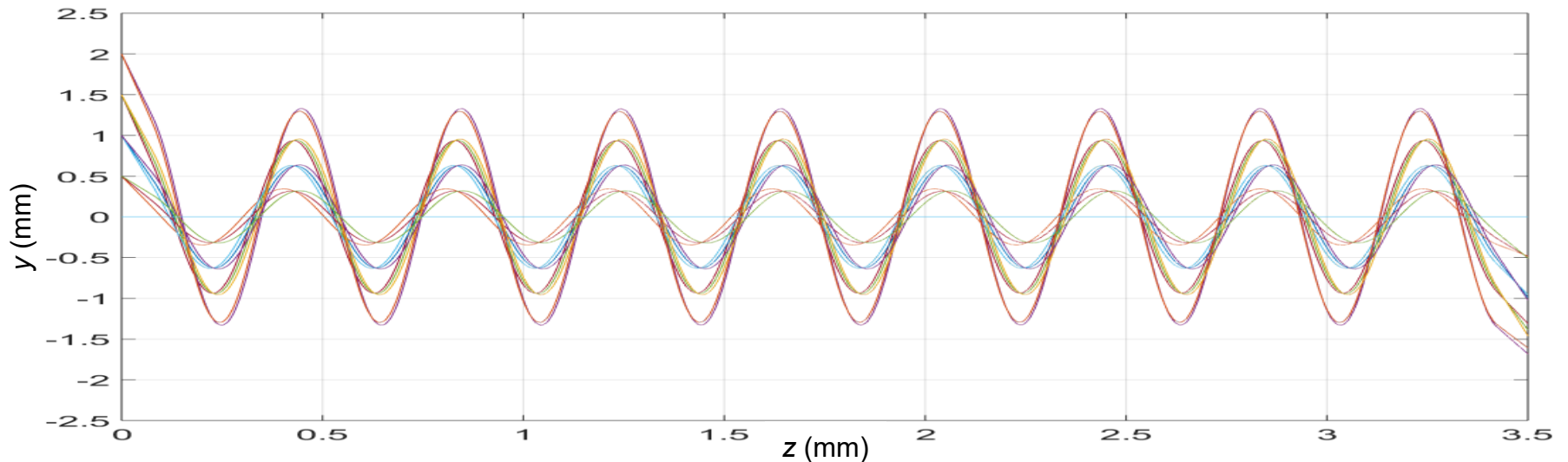
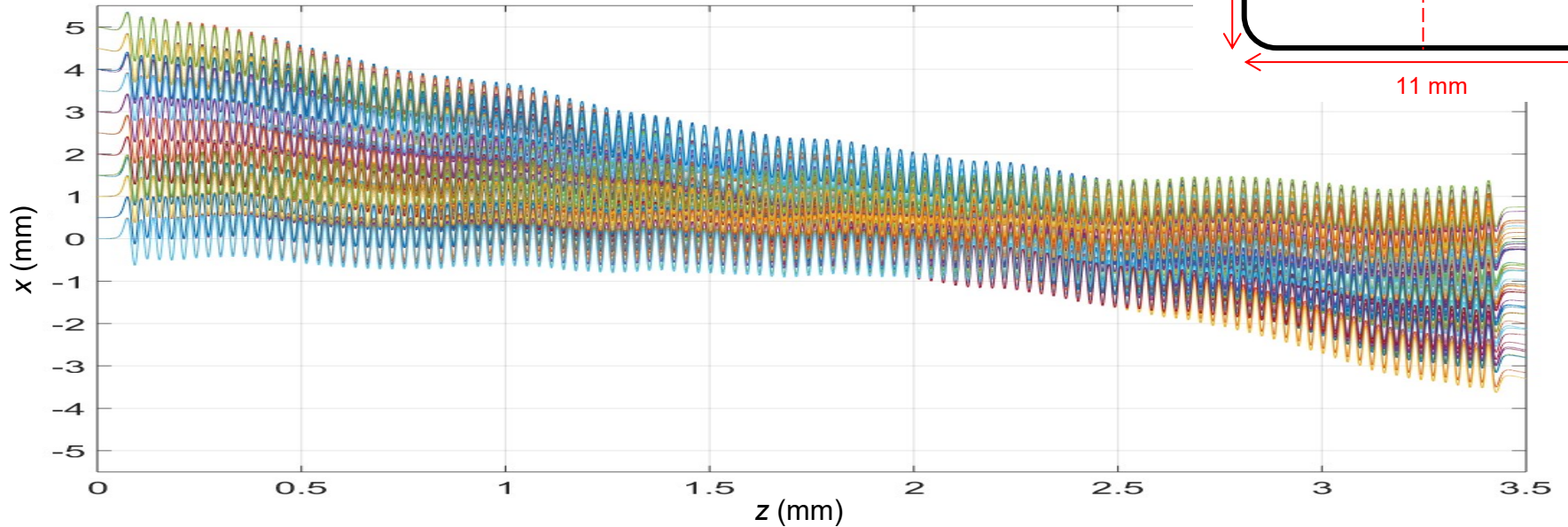
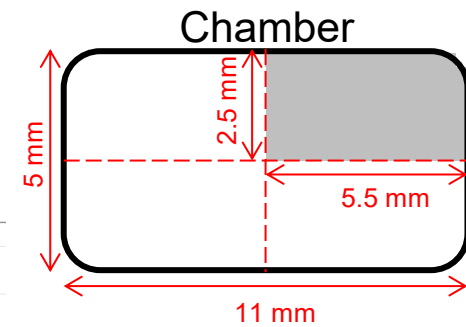
- Find cases that ref. electron can survive in the LCLS-I undulator.
- Maximum initial transverse area.
- Minimum Goal Function (GF).

$$\begin{array}{ll} x_0 = 0 \text{ to } 5 \text{ mm} & x_0' = -3 \text{ to } 2 \text{ mrad} \\ y_0 = 0 \text{ to } 2 \text{ mm} & y_0' = -11 \text{ to } 11 \text{ mrad} \\ (0.5 \text{ mm step size}) & (1 \text{ mrad step size}) \end{array}$$

$$GF = \int \frac{|x(z)| dz}{w} + \int \frac{|y(z)| dz}{h}$$

Single particle simulations

Rough scan



Single particle simulations

Rough scan

