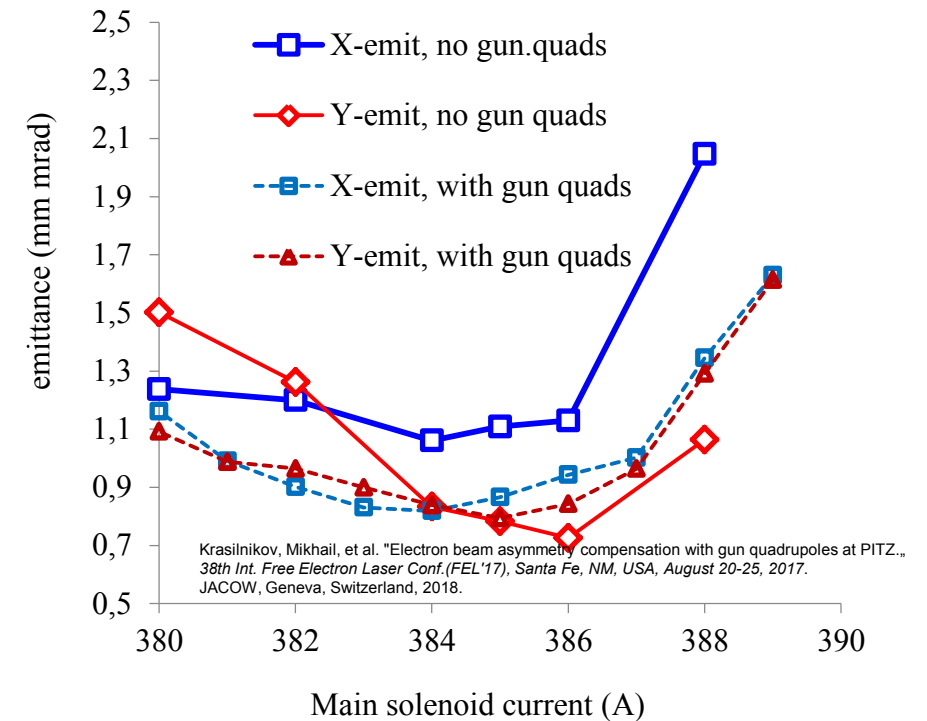
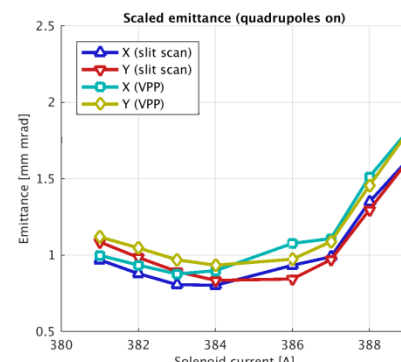
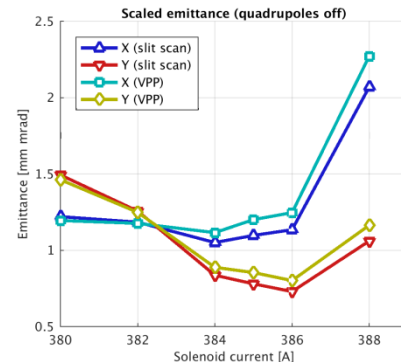
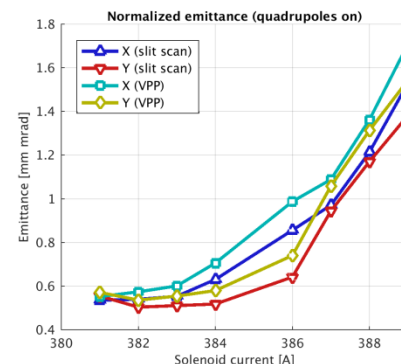
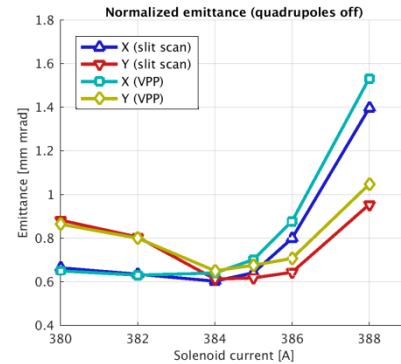


Virtual Pepper-Pot technique: procedure and results



Georgi Georgiev

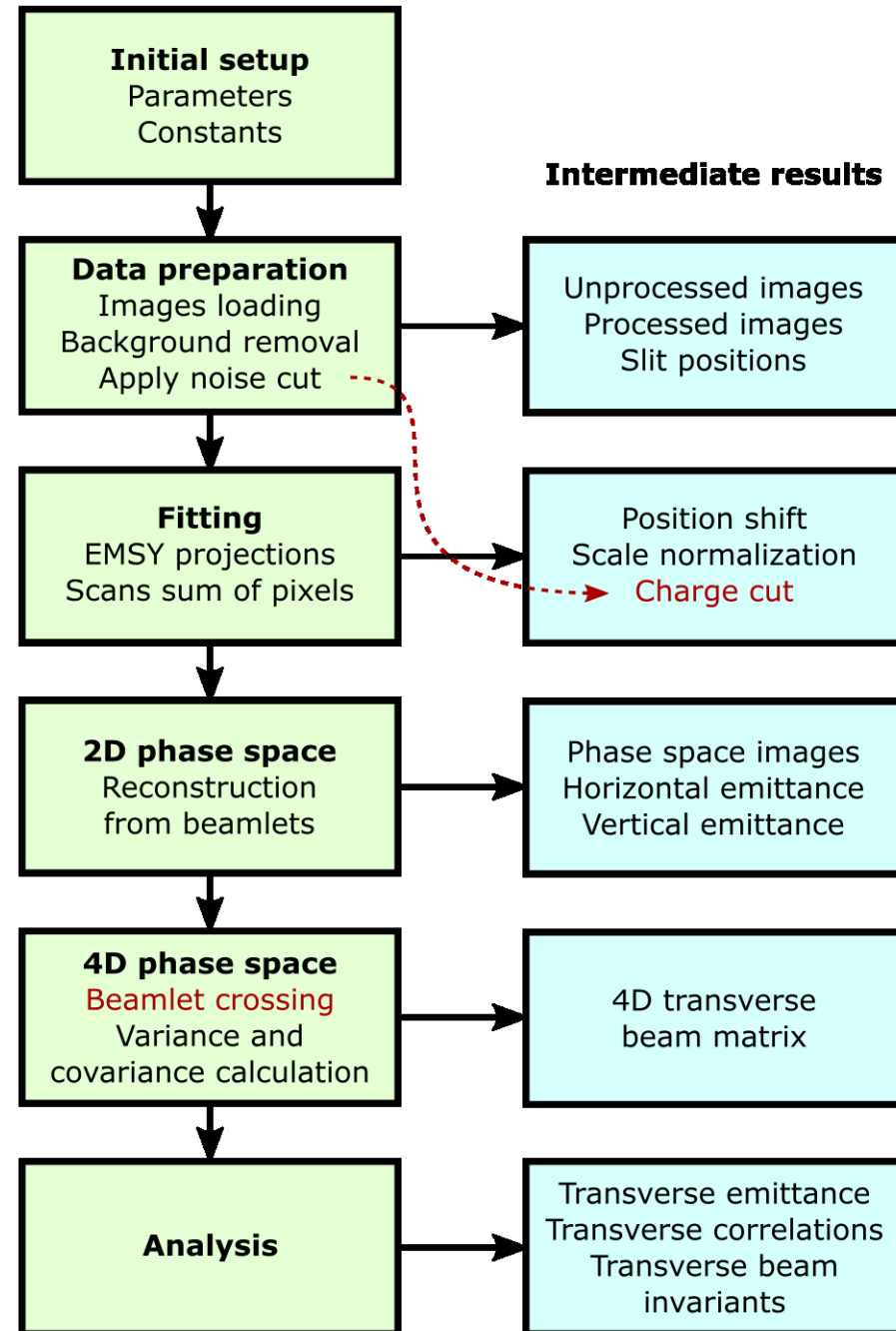
PPS 08.03.2019

Virtual Pepper-Pot

Reintroduction

- Measurement of 4D transverse phase space
- Virtual pepper-pot (VPP) technique
 - **Novel** technique
 - Data analysis
 - Extending slit scans to **4D measurements**
- Slit scan
 - **Only** 2D phase spaces restored
- Pepper-pot mask experiment
 - 4D phase space restored
 - **Difficulties**
 - Mask hole size and spacing, intensity
- VPP procedure overview - diagram

No noise cut
discussion in
this talk



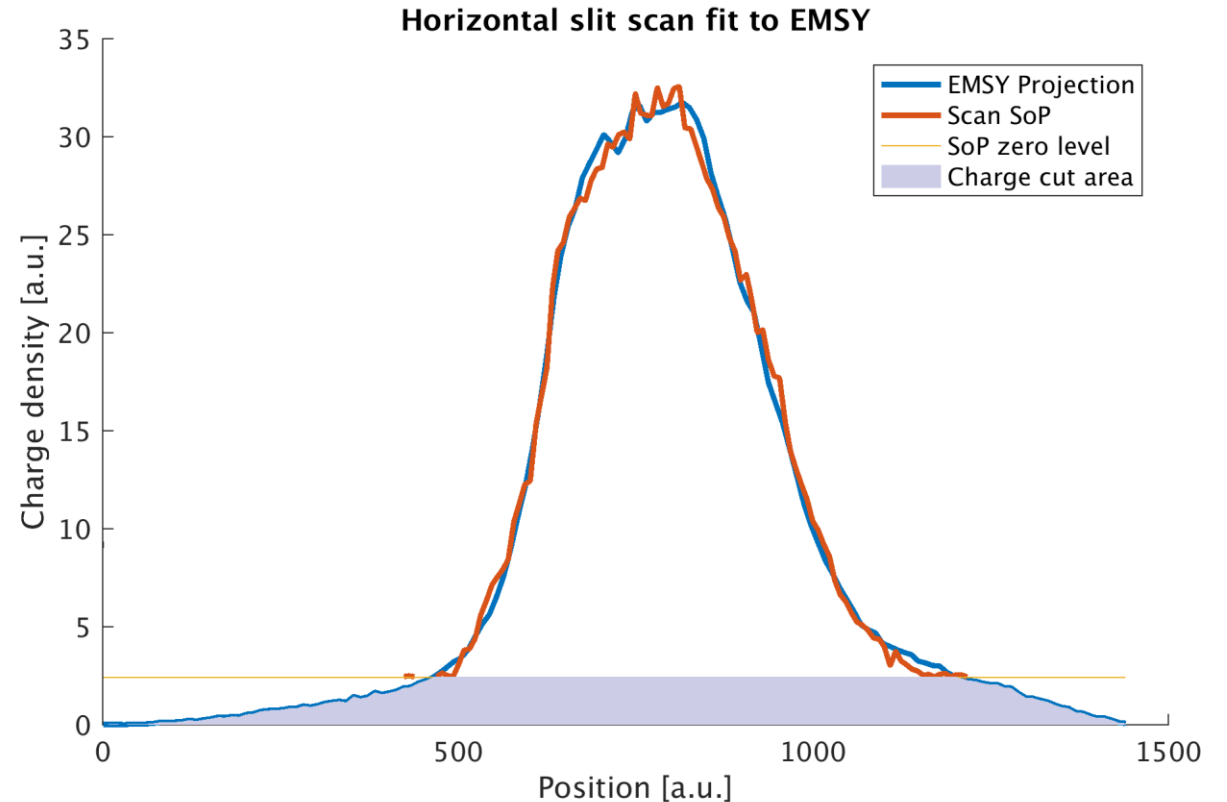
Fitting slit scan and EMSY

Offset, normalization, charge cut

- Same beam – same curves
 - EMSY projection along an axis
 - Sum of pixels (SoP) of beamlets along an axis
- Fitting parameters
 - Position shift
 - Scale normalization
 - Zero level difference
- Charge cut
 - Fraction of the beam **not** measured

Scale normalization to **common point** (EMSY) of X and Y slit scan images.

Part of the beam (halo and tail) **excluded** from further analysis.

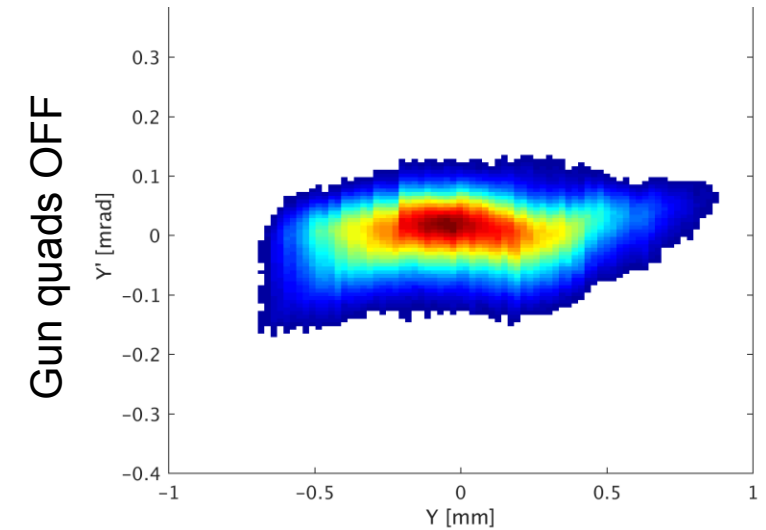
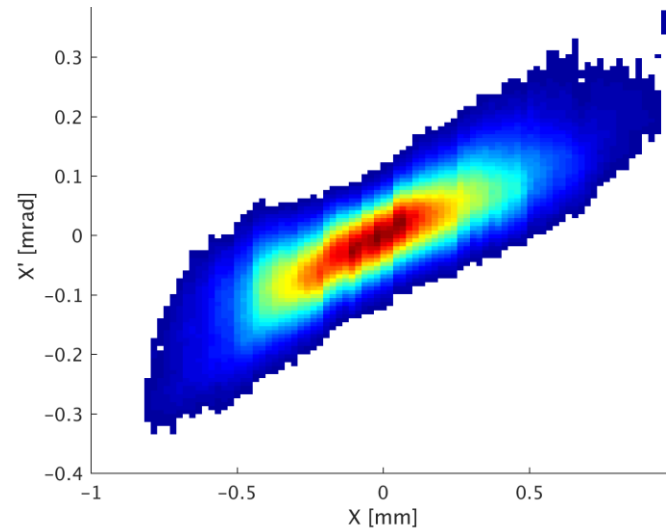
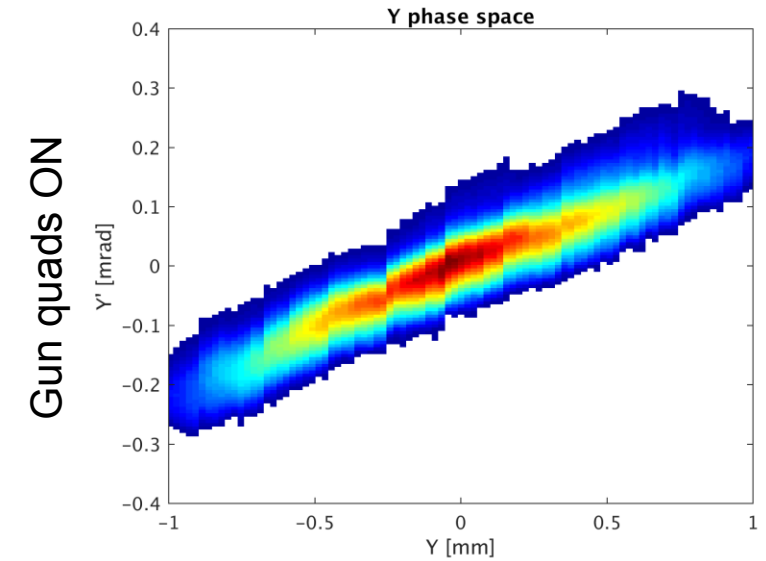
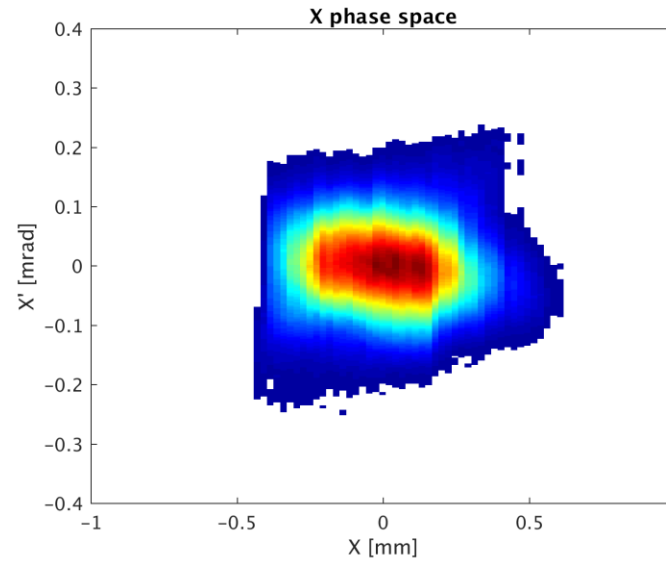


$$SF = \frac{\sigma_{EMSY}}{\sigma_{SoP}}$$

2D phase space

Phase space images and 2D emittance

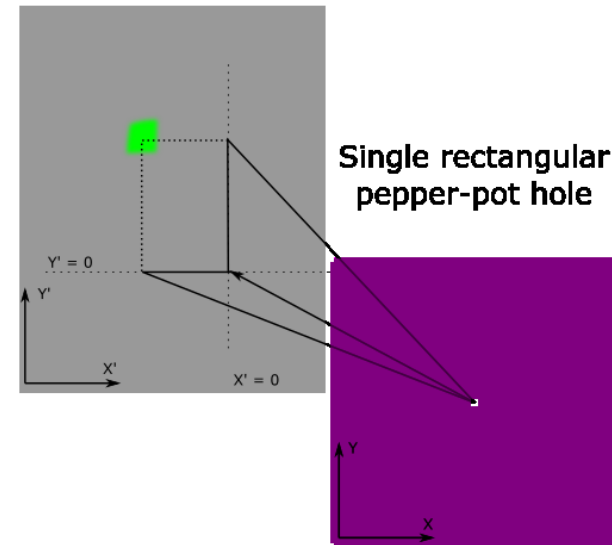
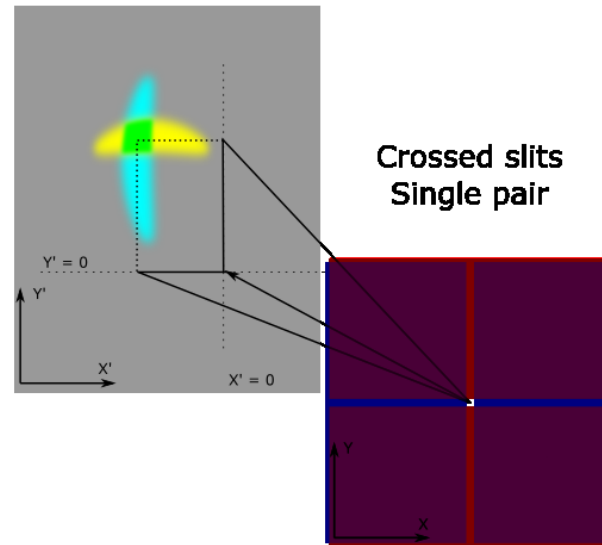
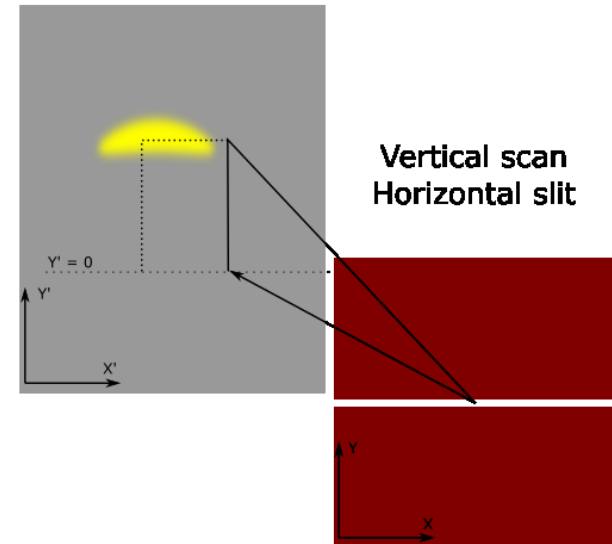
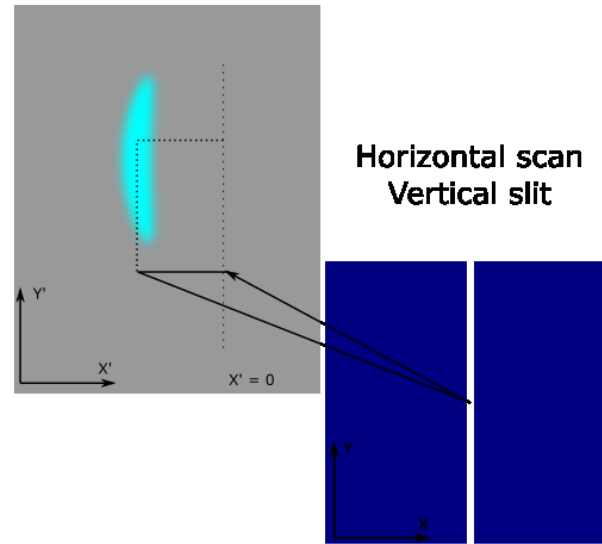
- Reconstructed phase spaces
- Matched with EMcalc3
 - Reproduced noise-cut filter
 - Good emittance agreement
- Reference in further analysis



Beamlet crossing (1)

Basic principle and methods

- Reconstruction
 - Two crossed slits \rightarrow small opening
 - Multiple crossed pairs \rightarrow PP mask
 - Beamlet crossing to slit crossing
 - **Ideally** shall be equivalent
- Crossing methods
 - Must preserve units
 - Must give 0 if any beamlet pixel is 0
 - **Pixel-wise geometric mean**
 - **Pixel-wise minimum value**
 - Normalization **dependent**



Beamlet crossing (2)

Foreign charge and crossing performance

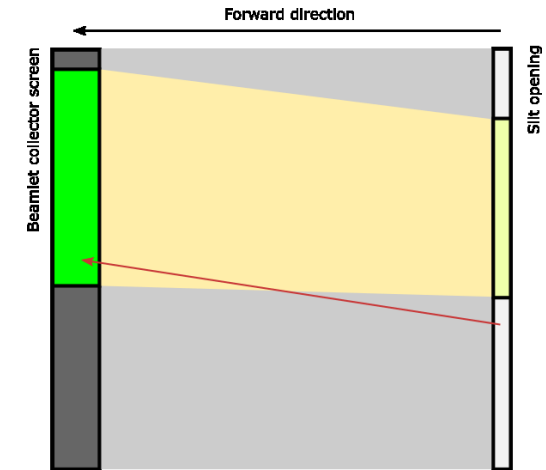
- Challenges
 - X scan, Y scan conditions
 - Image noise
 - Foreign charge**
- Pixel-wise geometric mean
 - Systematic error $\propto \sqrt{Q_{fx}}, \sqrt{Q_{fy}}$
- Pixel-wise minimum value
 - Minimizes** foreign portions
 - Better choice** with foreign charge

Data sample without gun quadrupoles and $I_{main} = 386$ A

Foreign charge model

$$Q_x = Q_0 + Q_{fx}$$

$$Q_y = Q_0 + Q_{fy}$$



$$Q_{cross} = \sqrt{Q_x Q_y} = \sqrt{Q_0(Q_0 + Q_{fx} + Q_{fy}) + Q_{fx} Q_{fy}}$$

$$Q_{cross} = \min(Q_x, Q_y) = Q_0 + \boxed{\min(Q_{fx}, Q_{fy})}$$

Case	ϵ_x (norm.)	ϵ_y (norm.)	Ratio ϵ_x/ϵ_y	$\epsilon_x \epsilon_y$
Slit scan (not VPP)	0,799	0,643	1,24	0,514
Min. val., EMSY normalized	0,922	0,685	1,35	0,632
Min. val., ratio optimized normalization	0,878	0,707	1,24	0,620
Geometrical mean	0,933	0,748	1,25	0,699
Min. val., incorrect normalization A	1,17	0,618	1,88	0,720
Min. val., incorrect normalization B	0,742	0,887	0,84	0,659

4D transverse beam matrix

Definitions and calculation

- Covariance matrix of the transverse phase space
- 4D transverse emittance with **correlations**
- Element calculation in VPP

$$\begin{pmatrix} \langle xx \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle xx' \rangle & \langle x'x' \rangle & \langle yx' \rangle & \langle x'y' \rangle \\ \langle xy \rangle & \langle yx' \rangle & \langle yy \rangle & \langle yy' \rangle \\ \langle xy' \rangle & \langle x'y' \rangle & \langle yy' \rangle & \langle y'y' \rangle \end{pmatrix}$$

$$\epsilon_{4D}^4 = \begin{vmatrix} \langle xx \rangle & \langle xx' \rangle & \langle xy \rangle & \langle xy' \rangle \\ \langle xx' \rangle & \langle x'x' \rangle & \langle yx' \rangle & \langle x'y' \rangle \\ \langle xy \rangle & \langle yx' \rangle & \langle yy \rangle & \langle yy' \rangle \\ \langle xy' \rangle & \langle x'y' \rangle & \langle yy' \rangle & \langle y'y' \rangle \end{vmatrix} = \epsilon_x^2 \epsilon_y^2 - \underline{C_{xy}^4}$$

$$\epsilon_x^2 = \begin{vmatrix} \langle xx \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'x' \rangle \end{vmatrix} = \langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2$$

$$Corr = \sqrt[4]{\frac{\epsilon_x^2 \epsilon_y^2}{\epsilon_{4D}^4} - 1}$$

$$\langle f(x, x', y, y') \rangle = \frac{\sum_i \sum_j \sum_k \sum_l f(x_i, x'_j, y_k, y'_l) w_{ik}(x'_j, y'_l)}{\sum_i \sum_j \sum_k \sum_l w_{ik}(x'_j, y'_l)}$$

w_{ik} - crossed beamlets image for i-th horizontal and k-th vertical slit positions

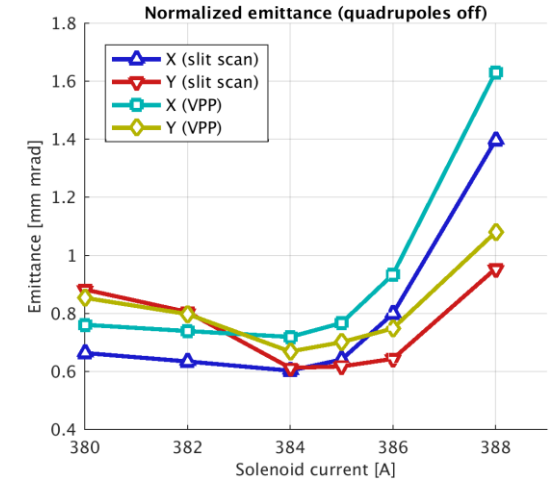
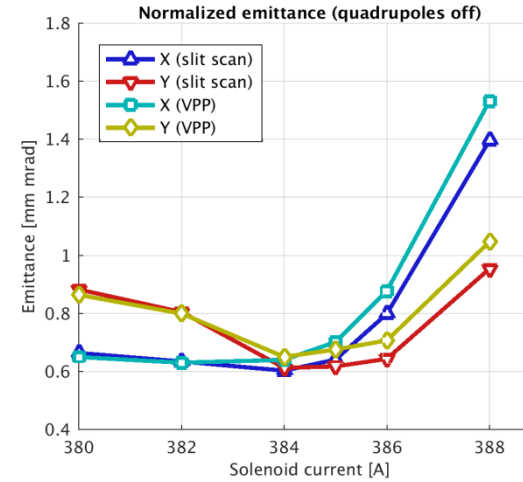
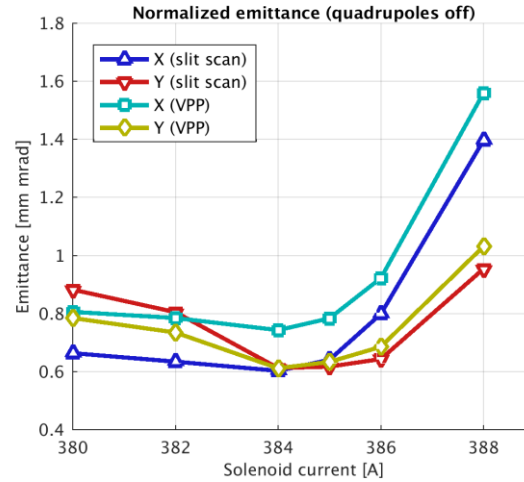
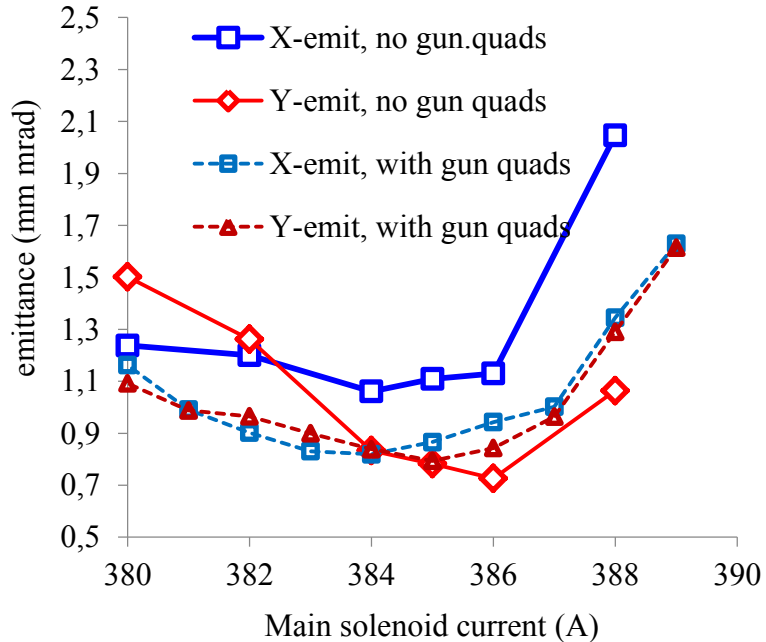
x'_j - x' of j-th pixel column

y'_l - y' of l-th pixel row

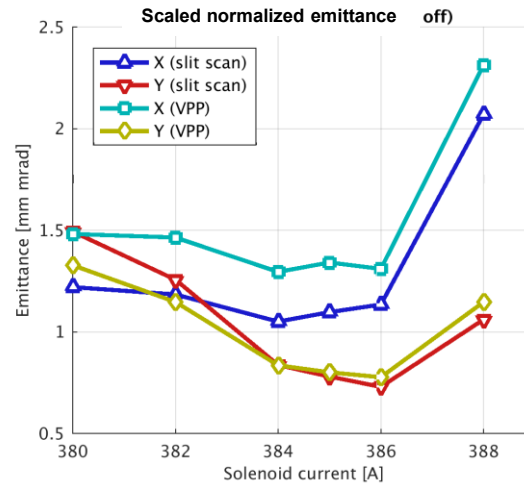
Results: 2D emittance

Method comparison

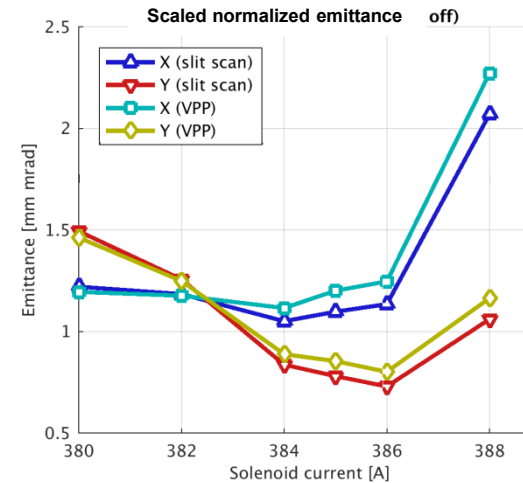
- Min. val. with EMSY norm
 - Horizontal is higher
- Min. val. with norm for ratio
 - **Best agreement**
- Geometrical mean
 - Both are higher



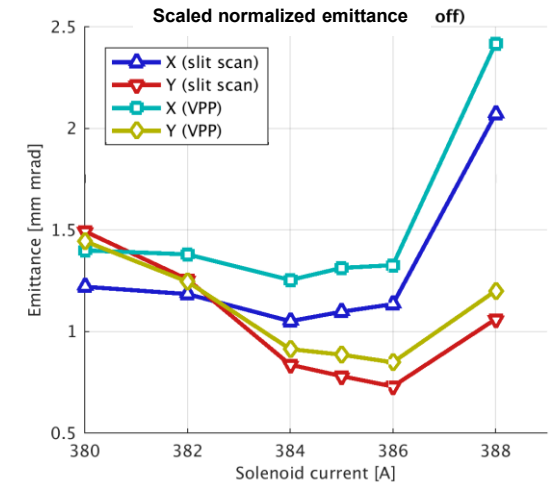
Minimum value, EMSY norm



Minimum value, Ratio norm



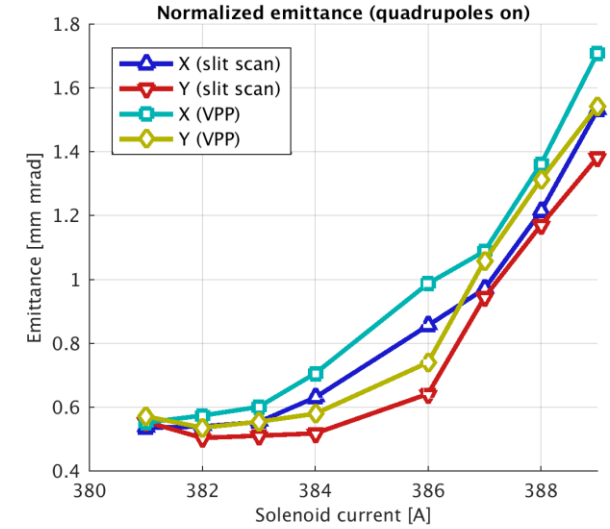
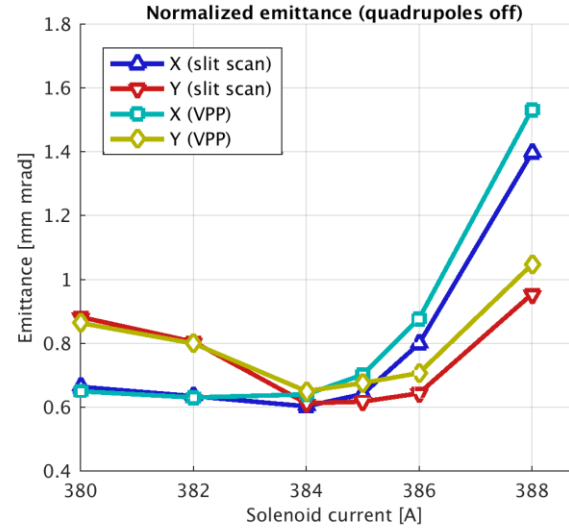
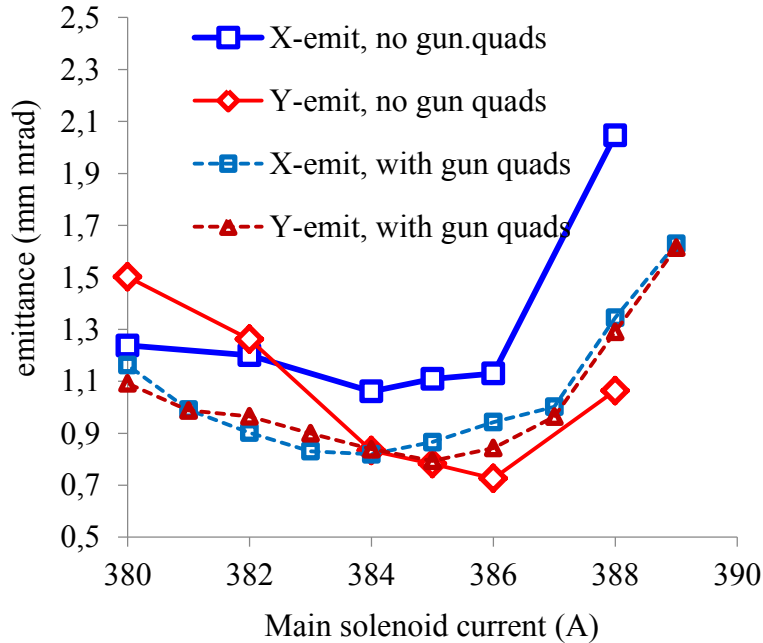
Minimum value, Geom. mean



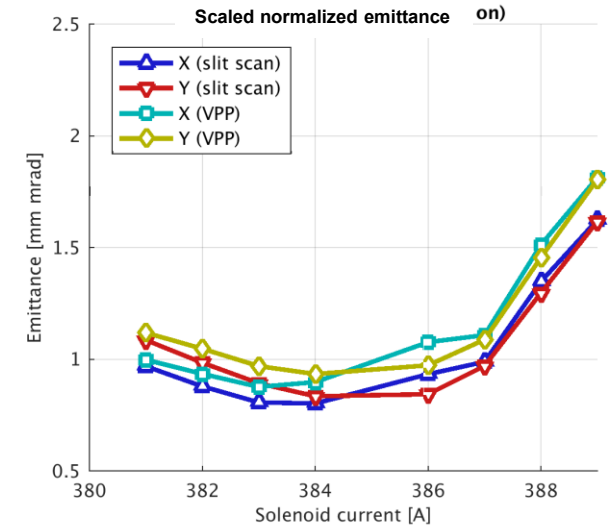
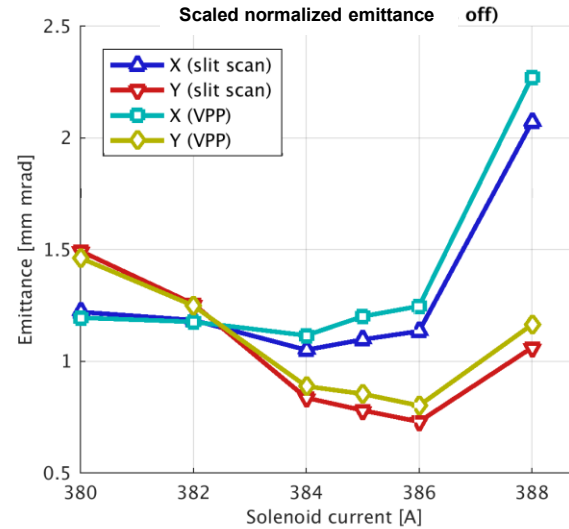
Results: 2D emittance

Gun quads ON and OFF

- Using min. val. crossing for best ratio
- Agreement with slit scan and previous studies
 - Higher at larger I_{main}



Minimum value cross, Ratio optimized norm



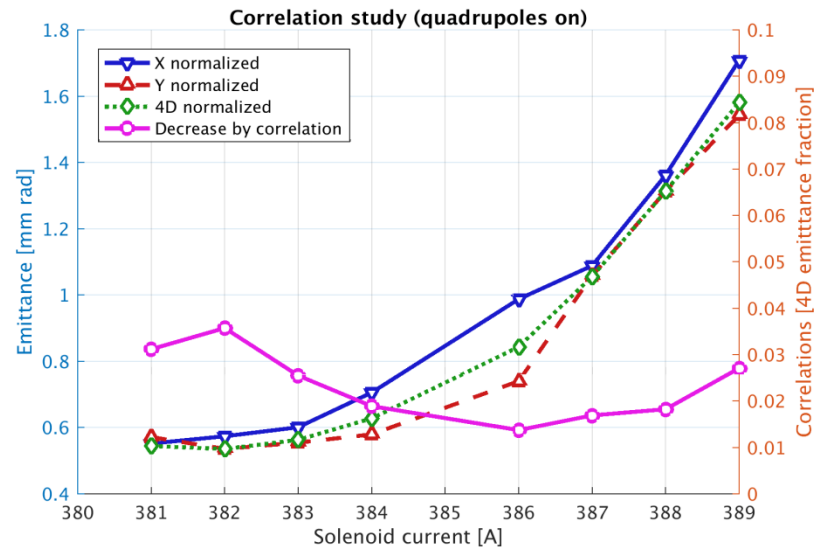
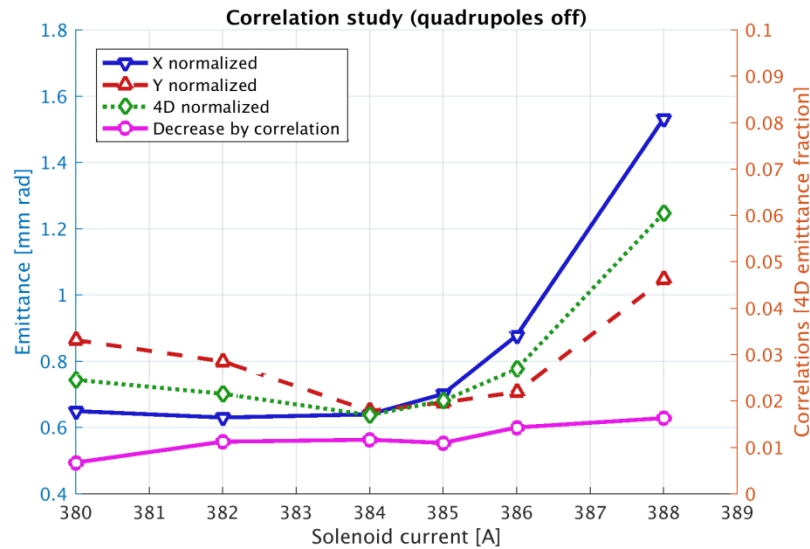
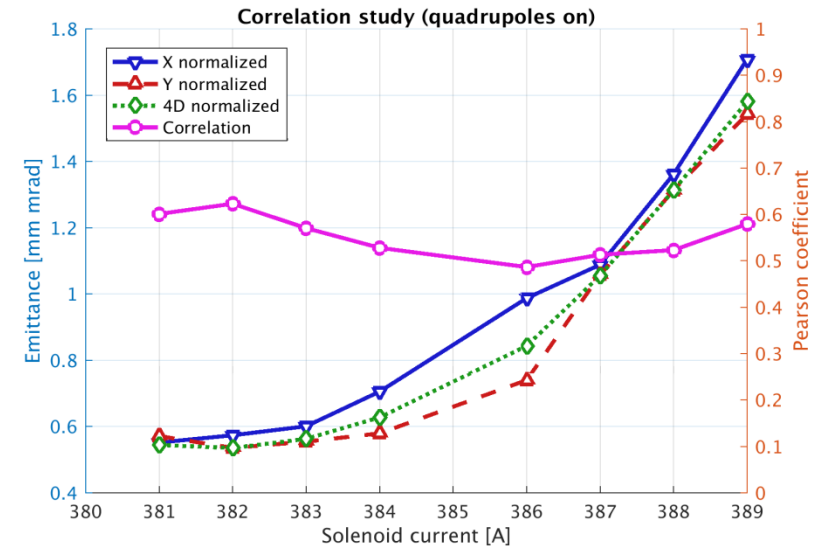
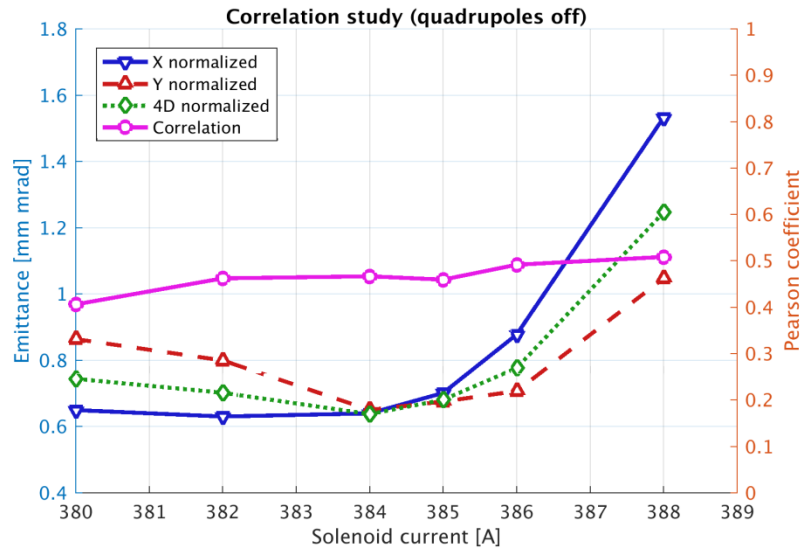
Results: 4D emittance

Correlations

- Pearson coefficient ~ 0.5
 - Coupling between X and Y
 - Small effect on 4D emittance
- Quadrupoles introduce correlations

$$Corr = \sqrt[4]{\frac{\epsilon_x^2 \epsilon_y^2}{\epsilon_{4D}^4} - 1}$$

$$\Delta_{coupling} = \sqrt[4]{\frac{\epsilon_x^2 \epsilon_y^2}{\epsilon_{4D}^4} - 1}$$

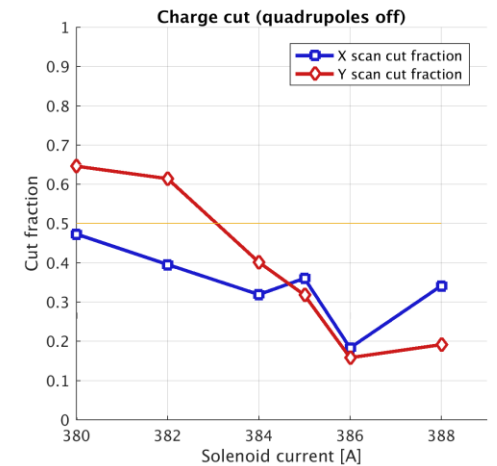
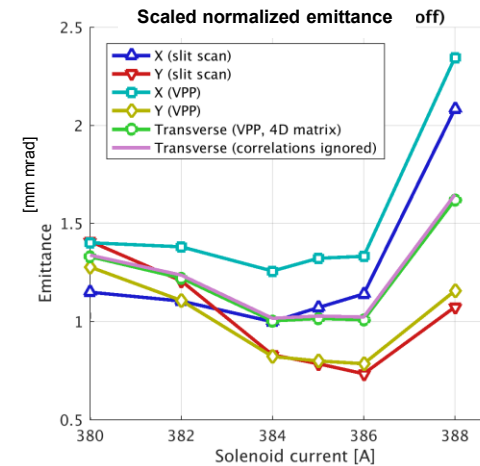
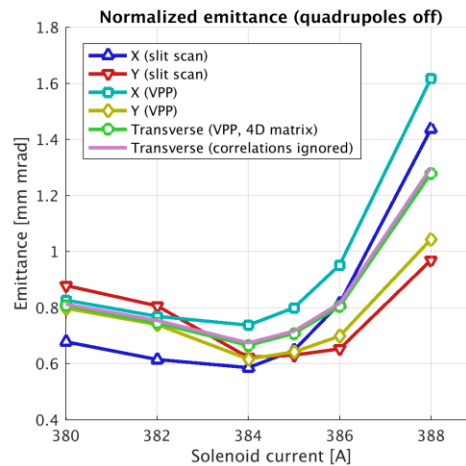
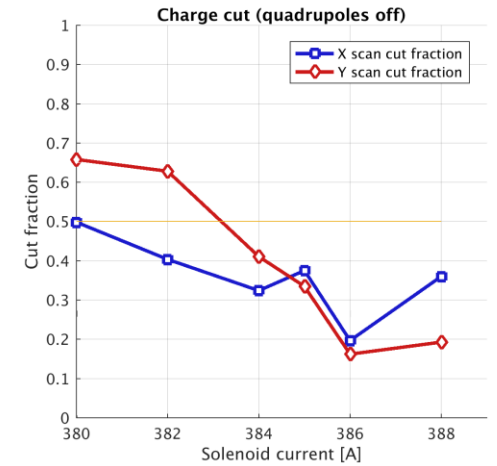
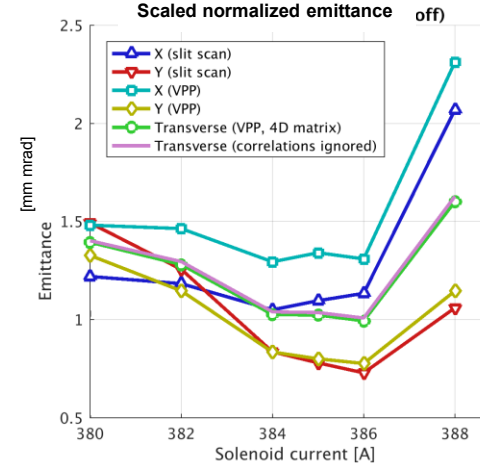
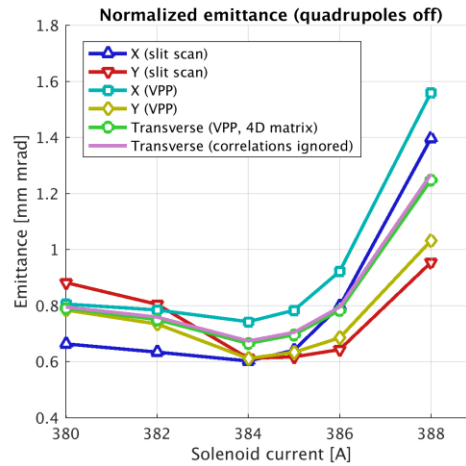


Charge cut

Charge cut and noise cut

- **Significant charge cut**
 - Above 25% on many points
- SNR and median filtering
 - Small charge cut decrease
 - Negligible difference in emittance

Part of the beam (halo and tail)
excluded from further analysis.



Conclusions

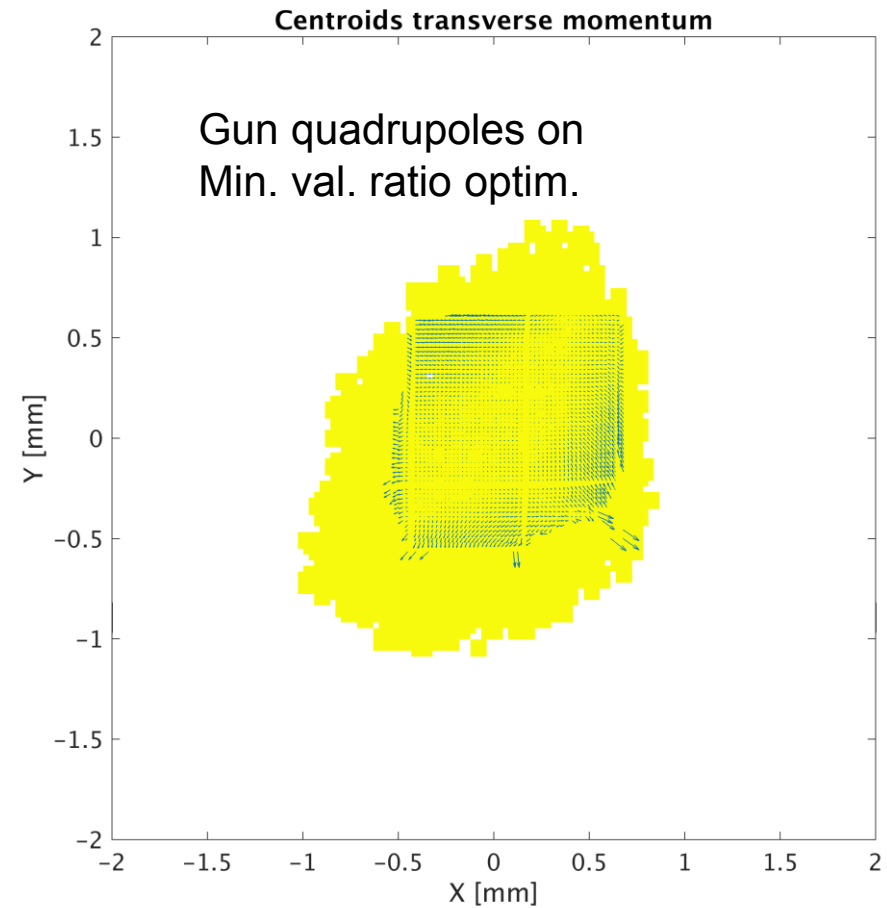
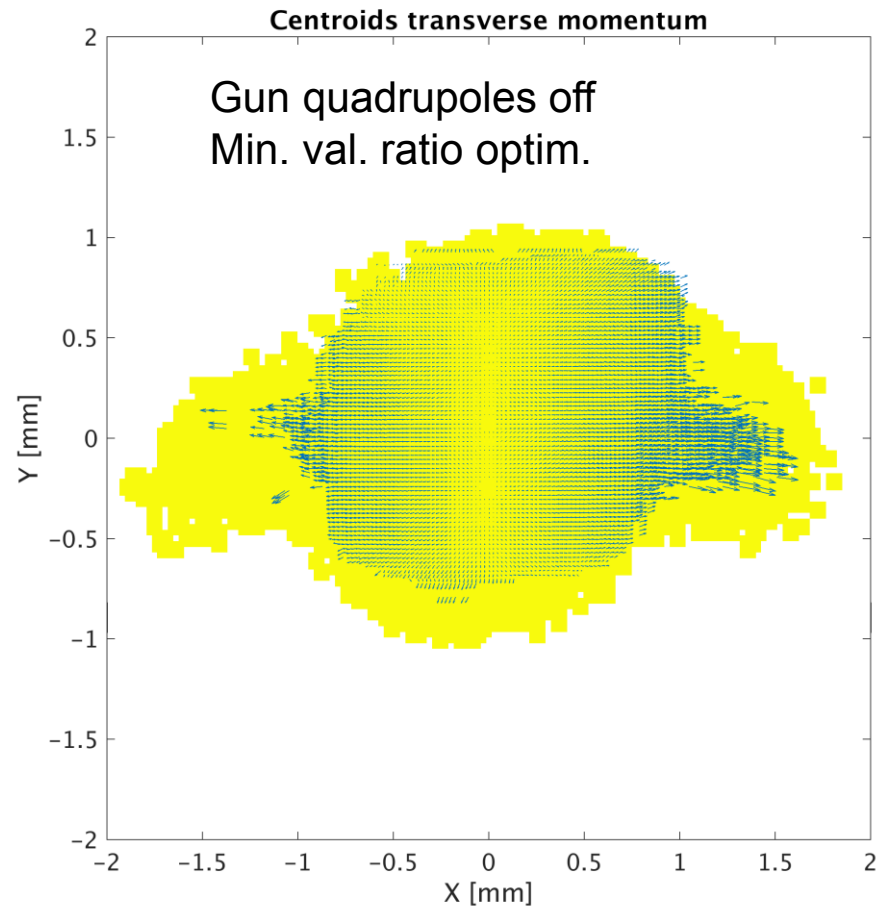
- Virtual Pepper-Pot **results agree** with Emcalc3
 - Minimum value crossing with normalization optimized for emittance ratio
- Correlations discovered
 - Gun quadrupoles increase coupling
- Significant charge cut
- Outlook
 - 4D transverse beam matrix eigenvalues – eigenemittances
 - Charge cut extrapolation to 0
 - Scaling factor studies
 - Full beamlet reconstruction

THANK YOU!

Centroid velocities

(Bonus slide)

- Centroid particle assigned for each crossed image of the VPP



Emittance invariant

4D kinematic invariant (Bonus slide)

- Transverse emittance invariant (for linear optics)
- Increase at stronger I_{main}

$$I_2^{(2)} = \epsilon_x^2 + \epsilon_y^2 + 2 C_{xy}^2$$

