

# Simulation of Undulator Radiation for the THz Source Project at PITZ

## Considerations for the Design of Undulator

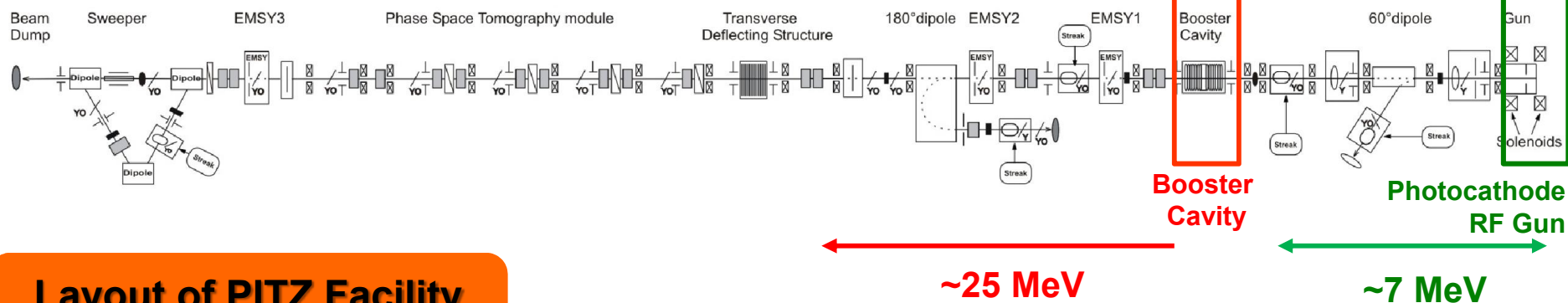
Prach Boonpornprasert

PITZ Physics Seminar  
13.03.2014

# Outline

- > PITZ Facility
- > THz source Project at PITZ
- > Considerations for the Design of Undulator
- > Summary
- > Outlook

# Photo Injector Test Facility at DESY, Location Zeuthen (PITZ)



**Layout of PITZ Facility**

## Goal

Development of high brightness electron source for linac based FELs

## Highlights in 2014

- > Plasma wakefield acceleration experiment
- > Setup of 3D-ellipsoidal laser system

Parameter	Value
RF frequency	1.3 GHz
RF repetition rate	10 Hz
Laser → Flattop → FWHM	~20 ps
e- bunch charge	20 pC – 4 nC
Maximum peak current	~200 A

# THz source Project at PITZ

- > The concept of an accelerator based source of THz/IR radiation for pump-probe experiment at European XFEL was presented in FEL2012 conference. (*E.A.Schiendmiller, M.Yurkov et al., WEPD55*)
- > Due to the identical time structure, PITZ can be considered as a proper site for the development of a THz source prototype that could be placed at the European XFEL site.
- > The preliminary simulations of SASE FEL using GENESIS code were done. The results are comparable to the benchmark results which using FAST code.
- > Suggestions from E.A.Schiendmiller and M.Yurkov for FEL simulation:
  - The goal radiation wavelengths are **5  $\mu\text{m}$ , 20  $\mu\text{m}$  and 100  $\mu\text{m}$ .**
  - Consider the design of APPLE-II type undulator.

Are all goal radiation wavelengths accessible with one undulator,  
**OR** we need 2 undulators with different period lengths ?

# Considerations for the Design of Undulator

Parameter	Corresponding study for its adjustment
Undulator Type	<ul style="list-style-type: none"><li>Polarization type of radiation field</li><li>• Helical type for circular polarization</li><li>• Planar type for linear polarization</li></ul>
Range of gap variation	<ul style="list-style-type: none"><li>• electron beam dynamics in undulator</li><li>• mechanical limitation</li></ul>
Period Length	<ul style="list-style-type: none"><li>• radiation wavelength</li><li>• electron beam momentum</li></ul>
Undulator length	<ul style="list-style-type: none"><li>• saturation length</li><li>• Radiation properties (peak power, bandwidth)</li><li>• Facility space</li></ul>

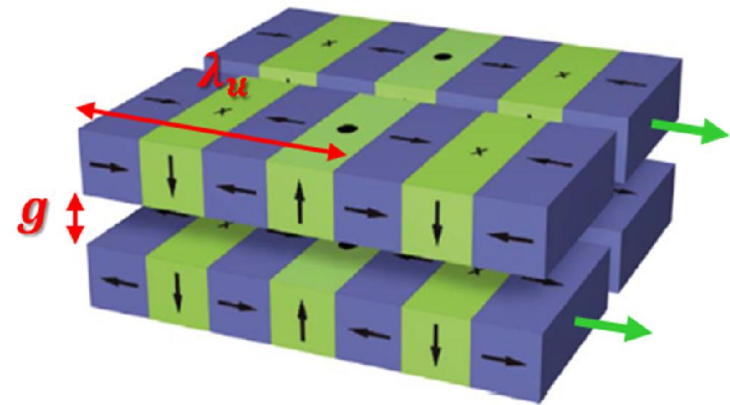
**Note:** In this study, we consider only the helical undulator.

# Design Consideration: Undulator Type

Requirement : Variably Polarized Undulator

## APPLE-II Type Undulator

- > Advanced Planar Polarized Light Emitter → APPLE
- > The undulator is a pure permanent magnet which composed of 4 arrays.
- > **The radiation** can be polarized vertically, horizontally, and circularly by moving two opposing magnet arrays.



Sketch of APPLE- II Undulator\*

\*Source: Conceptual Design Report ST/F-TN-07/12, Fermi@Elettra, 2007

Decision: APPLE-II Type Undulator

# Design Consideration: Undulator Type

## Requirement : Variably Polarized Undulator

- > The Peak magnetic field ( $B_{max}$ ) of an APPLE-II undulator can be derived from following formula:

$$B_{max}[T] = a_1 \times \exp \left[ a_2 \frac{g}{\lambda_u} + a_3 \left( \frac{g}{\lambda_u} \right)^2 \right] ; 0.1 < \frac{g}{\lambda_u} < 1.0$$

where  $a_1 = 1.54$ ,  $a_2 = -4.46$ , and  $a_3 = 0.43$  for the helical mode.

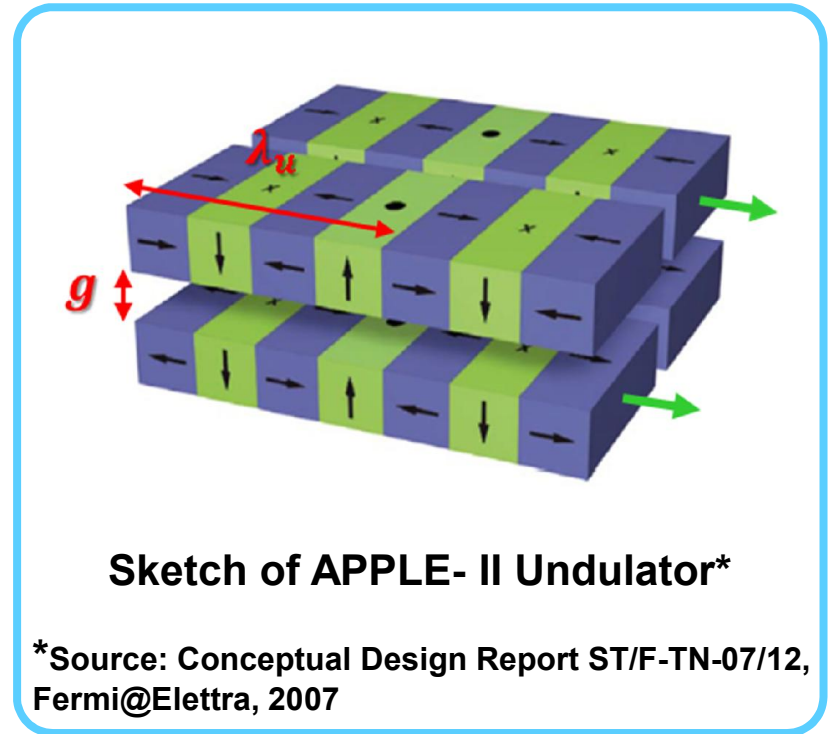
- > Undulator Parameter ( $K$ )

$$K = 0.934 \cdot B_{max}[T] \cdot \lambda_u[\text{cm}]$$

- > Radiation Wavelength ( $\lambda_{rad}$ )

$$\lambda_{rad} = \frac{\lambda_u}{2\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$

where  $\gamma$  is relativistic factor.



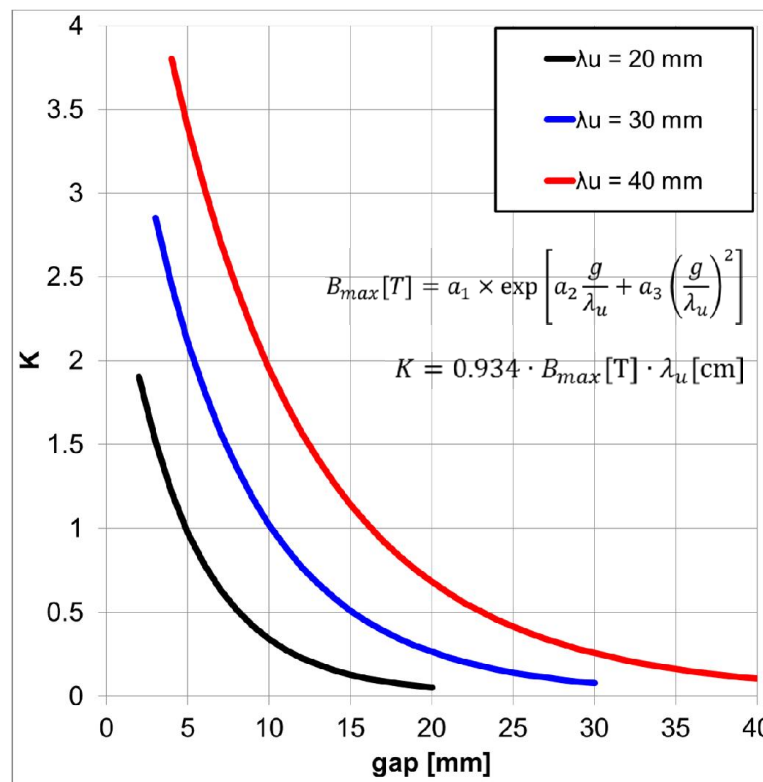
## Decision: APPLE-II Type Undulator

# Design Consideration: Range of Gap Variation

**Requirement : e-beam dynamics aperture ~0.6mm\***

\*From preliminary simulation with 4nC, 15MeV/c e-beam and  $\lambda_u = 40$  mm.

- >  $\lambda_u = 20$ mm, 30mm and 40mm were considered.
- > The range is limited by the condition,  $0.1 < \frac{g}{\lambda_u} < 1.0$ .
- > For in-vacuum undulator, the minimum gap has to be larger than  
(max beam tr size) + (tolerance)  
 $= 0.6 \text{ mm} + 1 \text{ mm} = 1.6 \text{ mm} \approx \mathbf{2 \text{ mm}}$
- > For in-air undulator, the minimum gap has to be larger than  
(max beam tr size) + (tolerance) + (vacuum chamber wall)  
 $= 0.6 \text{ mm} + 1 \text{ mm} + 2 \text{ mm} = 3.6 \text{ mm} \approx \mathbf{4 \text{ mm}}$
- > The maximum gap (open gap) of APPLE-II undulator used in various FEL facility is in general  $\sim 40$ mm.



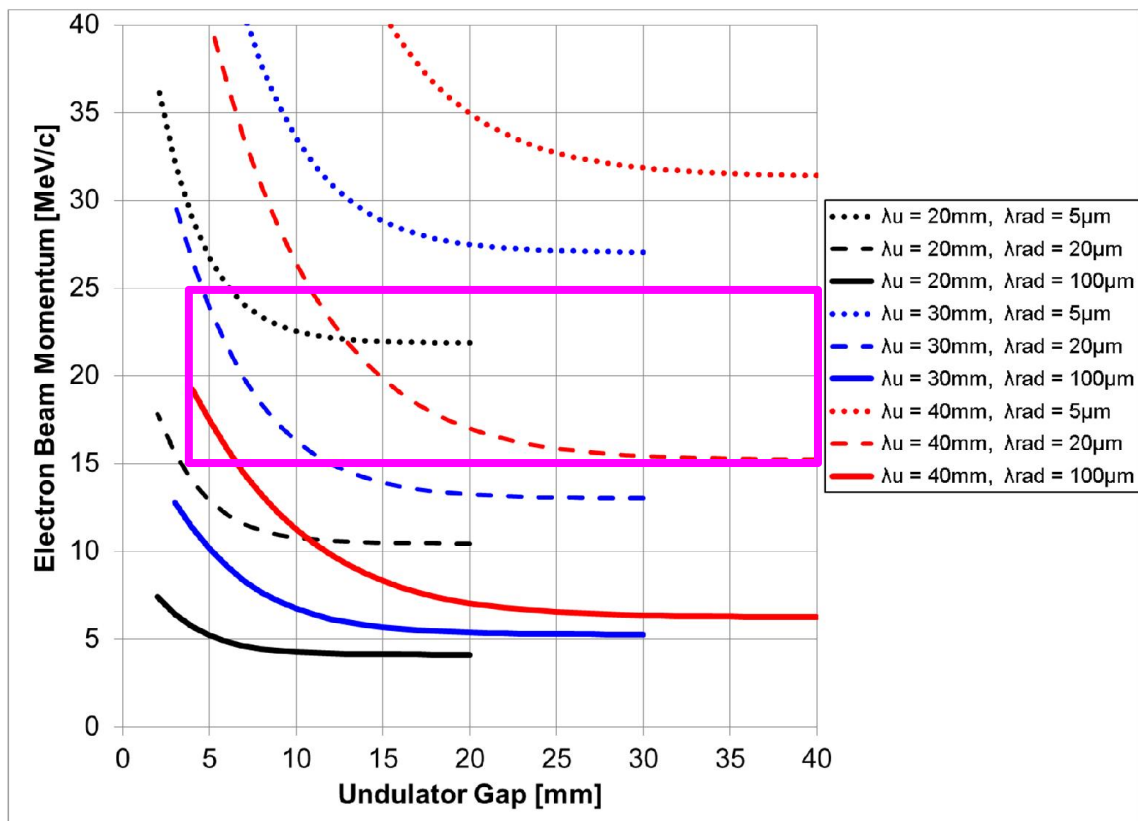
**Decision: 2mm to 40mm for in-vacuum undulator  
4mm to 40mm for in-air undulator**



# Design Consideration: Undulator Period Length

Requirement : in-air undulator, range of e-beam momentum is 15 -25 MeV/c

- >  $\lambda_u = 20\text{mm}$ ,  $30\text{mm}$  and  $40\text{mm}$  were considered.
- >  $\lambda_{rad} = 5\mu\text{m}$ ,  $20\mu\text{m}$  and  $100\mu\text{m}$  were considered.
- > purple box shows the possible operation region.



**Decision:**  $\lambda_u = 20\text{ mm}$  for  $\lambda_{rad} = 5\ \mu\text{m}$   
 $\lambda_u = 40\text{ mm}$  for  $\lambda_{rad} = 20\ \mu\text{m}$  and  $100\ \mu\text{m}$

# Design Consideration: Undulator Length

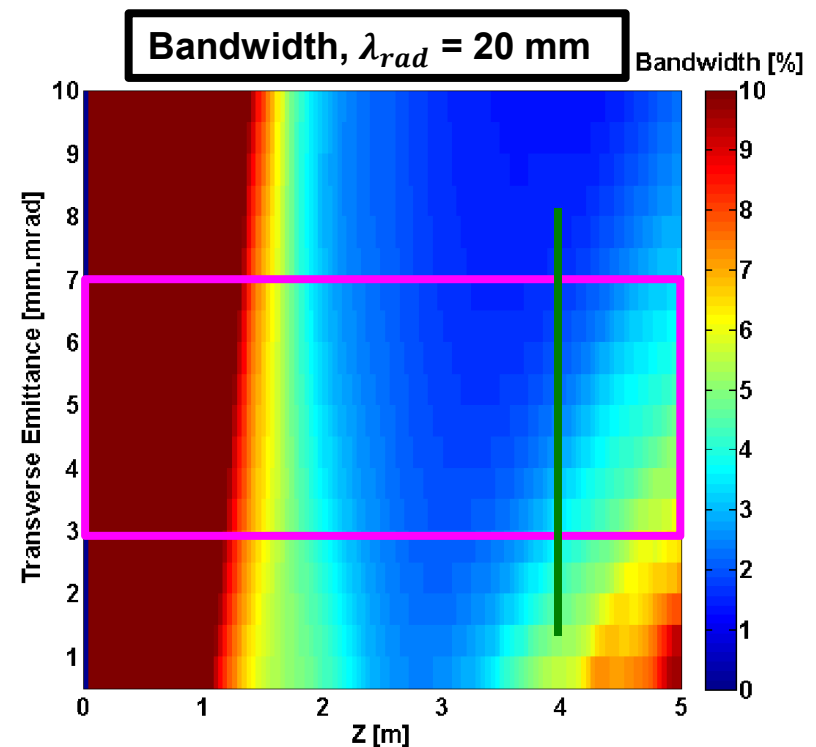
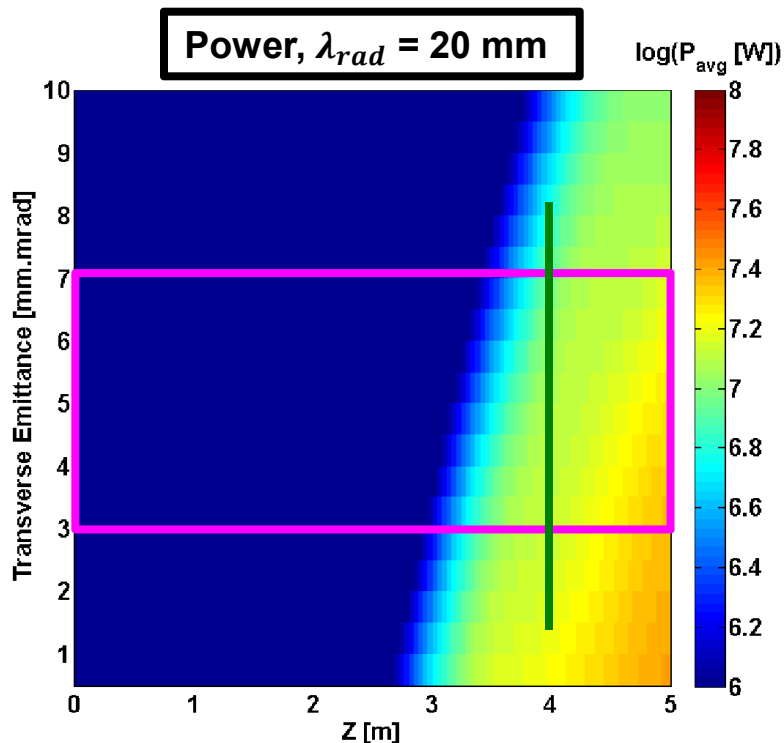
**Requirements:** maximum undulator length of 5 m,  
radiation bandwidth ~5%, peak power in MW level

- > The undulator length is determined from saturation length of SASE FEL radiation.
- > GENESIS1.3 code was used for FEL simulation.
- > The space charge calculation is excluded in the simulation.
- > In this presentation, only **20  $\mu\text{m}$**  and **100  $\mu\text{m}$**  cases were studied. For **5  $\mu\text{m}$**  case, which different period length has to be used, will be studied later.
- > The model Gaussian electron beam with parameters in the right hand side table were used in the simulations.
- > From preliminary beam dynamics simulations, The possible range of  $\varepsilon_{\text{tr,rms}}$  is **3 to 7 mm.mrad**.

Parameter	Detail	
undulator type	Helical	
undulator period length ( $\lambda_u$ )	40 mm	
number of period	125	
radiation wavelength ( $\lambda_{\text{rad}}$ )	20 $\mu\text{m}$	100 $\mu\text{m}$
undulator gap (g)	14 mm	6 mm
$K / \sqrt{2}$	0.90	2.10
$\langle P_z \rangle$	21 MeV/c	16 MeV/c
$P_{z,\text{rms}} / \langle P_z \rangle$	0.1%	
bunch charge	4 nC	
rms current length	2.4 mm	
peak current	200 A	
$\alpha_x, \alpha_y$	0	
$\sigma_x, \sigma_y$	0.2178 mm	

# Design Consideration: Undulator Length (2)

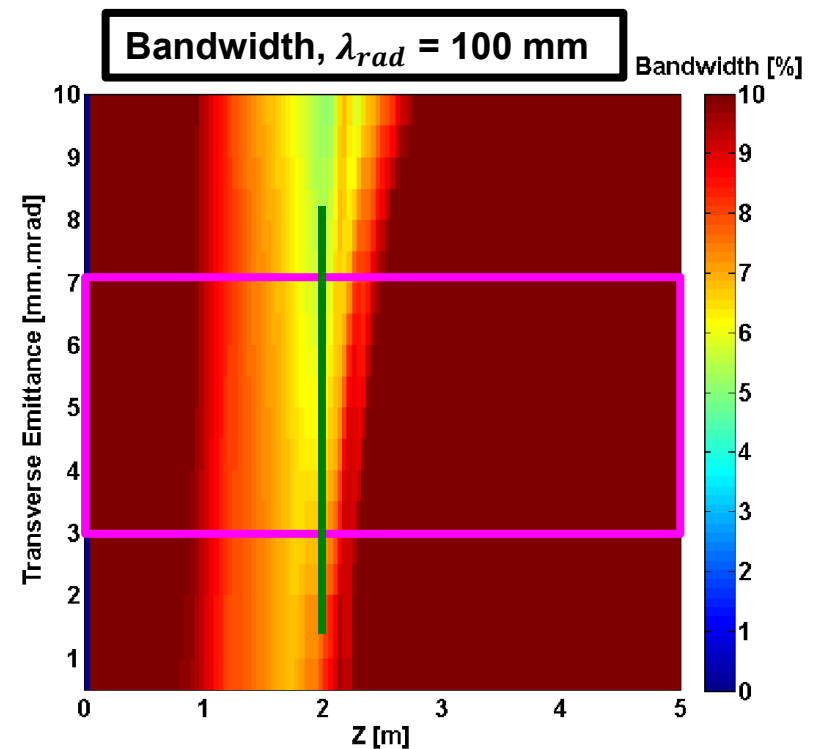
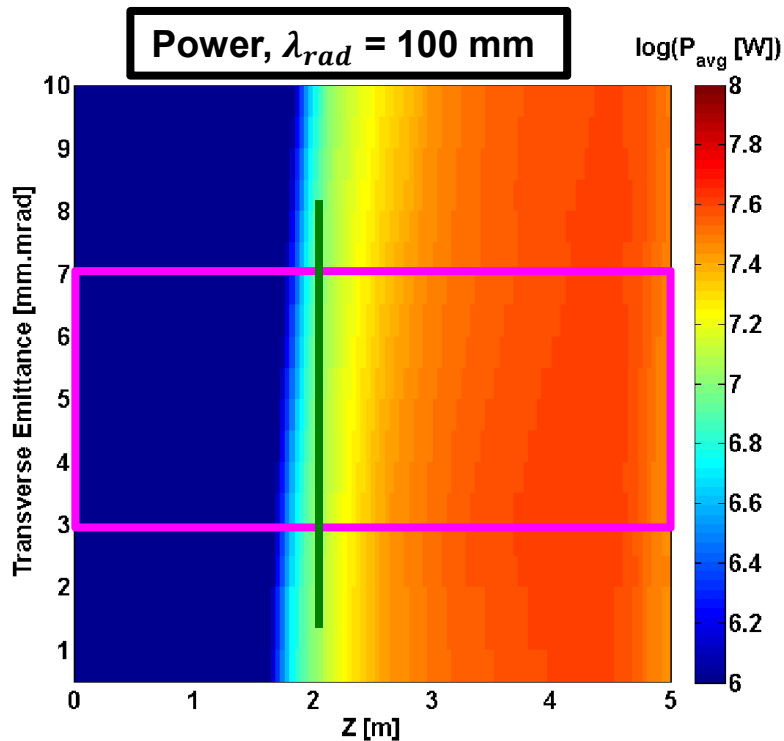
**Requirements:** maximum undulator length of 5 m,  
radiation bandwidth  $\sim 5\%$ , peak power in MW level



By neglecting the space charge effect, the expected peak power and bandwidth correspond to  $\underline{z = 4 \text{ m}}$  for  $\lambda_{rad} = 20 \mu\text{m}$

# Design Consideration: Undulator Length (3)

**Requirements:** maximum undulator length of 5 m,  
radiation bandwidth  $\sim 5\%$ , peak power in MW level



By neglecting the space charge effect, the expected peak power and bandwidth correspond to  **$z = 2 \text{ m}$**  for  $\lambda_{rad} = 100 \mu\text{m}$

# Summary

The considered undulator parameters are shown in following table:

Specification	Decision
Undulator Type	APPLE-II type undulator, in-air
Range of gap variation	4mm to 40mm
Period Length	$\lambda_u = 20 \text{ mm}$ for $\lambda_{rad} = 5 \text{ }\mu\text{m}$ $\lambda_u = 40 \text{ mm}$ for $\lambda_{rad} = 20 \text{ }\mu\text{m}$ $\lambda_u = 40 \text{ mm}$ for $\lambda_{rad} = 100 \text{ }\mu\text{m}$
Undulator length	under study...

# Outlook

- > Repeat the scans concerning the power and bandwidth as a function of emittance of the electron bunch including space charge effect.
- > Perform the same scan for  $\lambda_{\text{rad}} = 5 \mu\text{m}$ .
- > Start to End (S2E) simulation for SASE FEL
- > Simulation of the production of THz radiation using Coherent Transition Radiation.

**This point only for PPS**

Publish paper in topic,  
***“Start-to-End Simulation of THz Source Project at PITZ ”***

**Thanks for your attention !**

# Backup: more information of APPLE-II

## APPLE-II Type Undulator\*

- > The Peak magnetic field ( $B_{max}$ ) of an APPLE-II undulator can be derived from the formula:

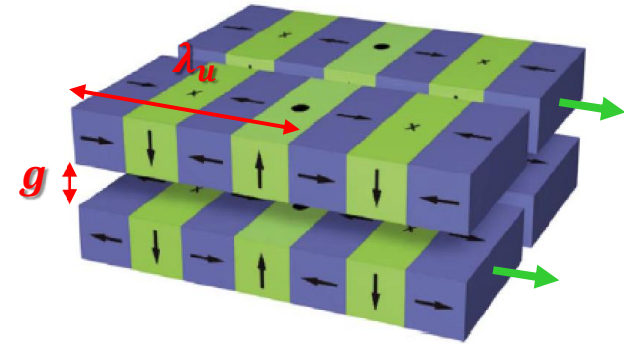
$$B_{max}[T] = a_1 \times \exp \left[ a_2 \frac{g}{\lambda_u} + a_3 \left( \frac{g}{\lambda_u} \right)^2 \right],$$

where  $0.1 < \frac{g}{\lambda_u} < 1$ .

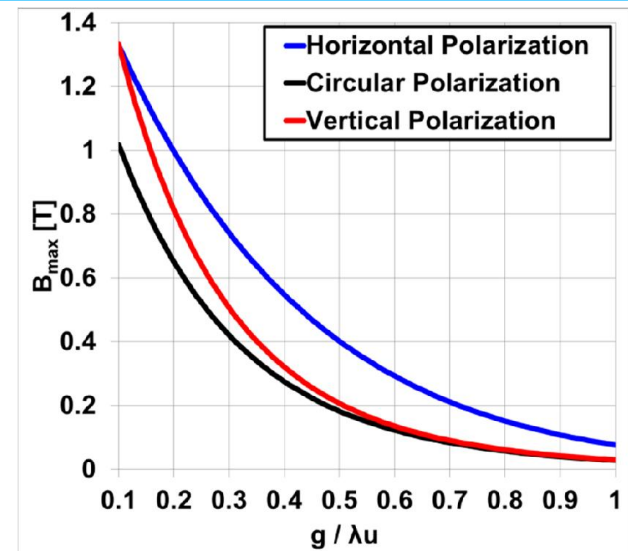
- > The coefficients for each mode of APPLE-II are listed in the following table:

Polarization	$a_1$	$a_2$	$a_3$
Horizontal	1.76	-2.77	-0.37
Circular	1.54	-4.46	0.43
Vertical	2.22	-5.19	0.88

\*Reference: Conceptual Design Report ST/F-TN-07/12, Fermi@Elettra, 2007



Sketch of APPLE- II Undulator



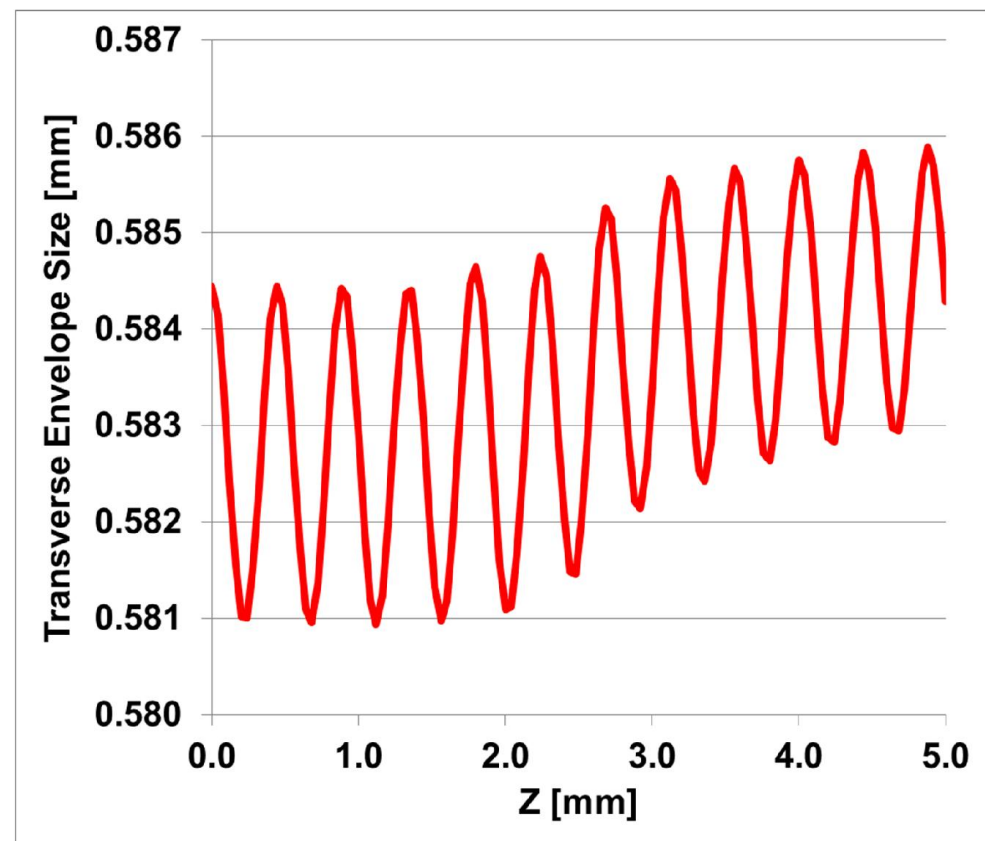
$B_{max}$  from Various Polarization Mode



# Backup: Preliminary results of beam dynamics along the undulator

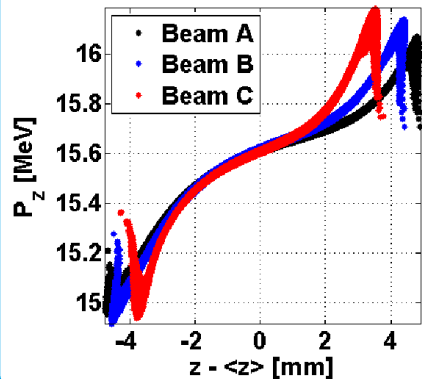
Transverse envelope size =  $6 \cdot \sigma_{x,y}$

Parameter	Detail
undulator type	Helical
$K / \sqrt{2}$	1.9092
undulator period length ( $\lambda_u$ )	4 cm
number of period	125
radiation wavelength ( $\lambda_{rad}$ )	100 $\mu$ m
bunch charge	4 nC
rms current length	2.4 mm
peak current	200 A
e-beam energy	15 MeV
energy spread	20 keV
$\beta_x, \beta_y$	14.4 cm
$\epsilon_x, \epsilon_y$	10 mm.mrad
$\alpha_x, \alpha_y$	0

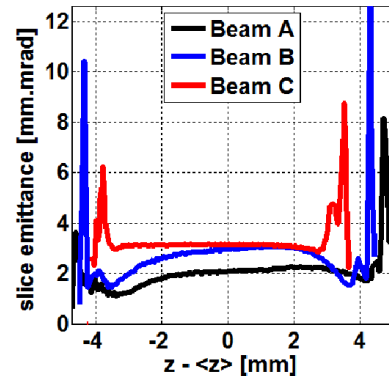


# Backup: Preliminary Beam Dynamics simulations

## Long. Phase Space



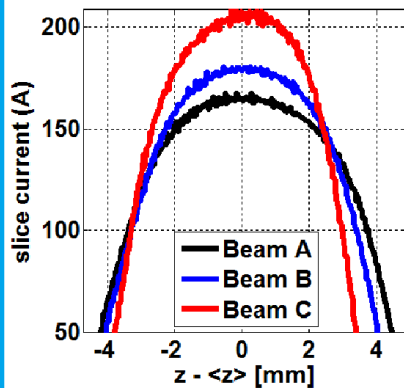
## Slice Tr. Emittance



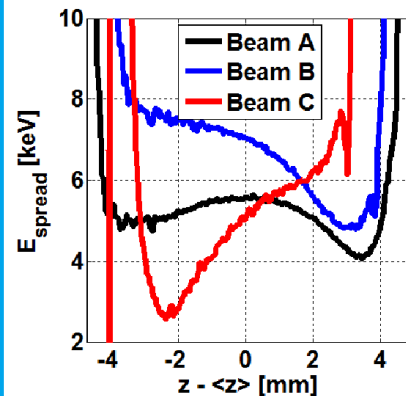
## ASTRA input parameters

Parameter	Beam A	Beam B	Beam C
rms laser spot size (mm)	1.092	1.455	3.500
$I_{\text{main}}$ (A)	378	380	340
$\Phi_{\text{gun}}$ (degree)	-1.404	-1.404	-1.404
$E_{\text{max,booster}}$ (MV/m)	10.2	10.2	10.2

## Beam Current



## Slice Energy Spread



## Beam parameters after matching

Parameter	Beam A	Beam B	Beam C
$\epsilon_{\text{tr},n}$ (mm.mrad)	2.66	4.99	7.01
$\langle \epsilon_{\text{slice}} \rangle$ (mm.mrad)	2.06	2.74	3.33
$\langle E_{\text{spread,slice}} \rangle$ (keV)	7.35	9.23	9.60
$I_{\text{peak}}$ (A)	160	170	205