

# Characterization of the transverse profile of the photocathode laser

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Characterization of the transverse profile of  
the PITZ photocathode laser

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# Introduction

- Previous studies suggest flat-top transverse laser profile for best emittance
- Further studies: modulations on flat-top have negative influence on emittance
- Up to now only 2 parameters for laser characterization: intensity & BSA size
- New parameters have to be found in order to characterize inhomogeneities and investigate their influence on beam emittance



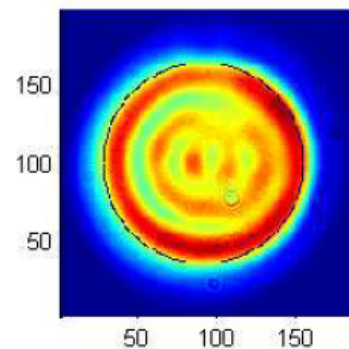
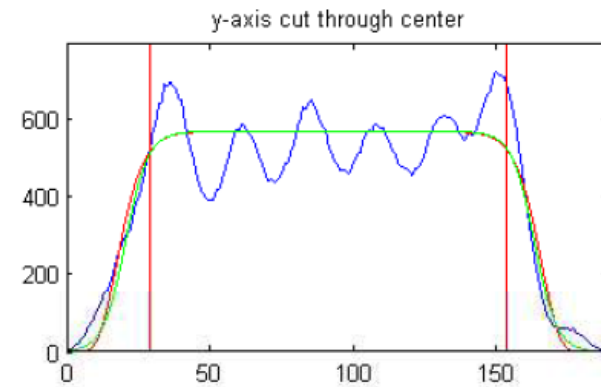
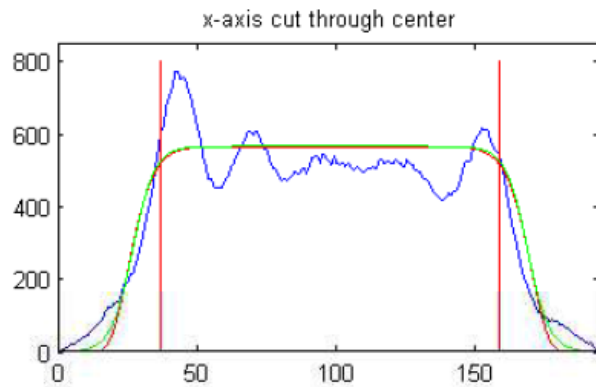
# Area of interest

- > Reason for Aoi: limit homogeneity analysis to flat-top part, exclude flanks
- > Aoi finding must be automated for reproducible results
- > First 1D approach with projections on x- and y axis failed (too inaccurate)
- > New approach: 2D-fitting



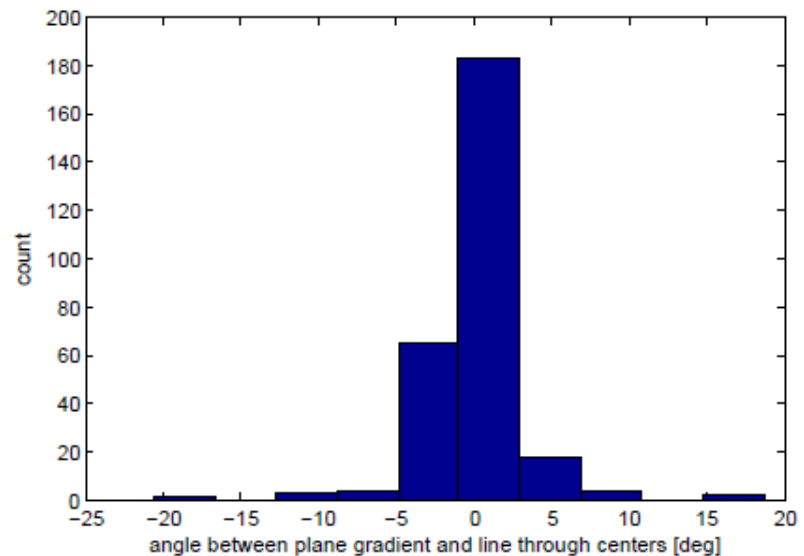
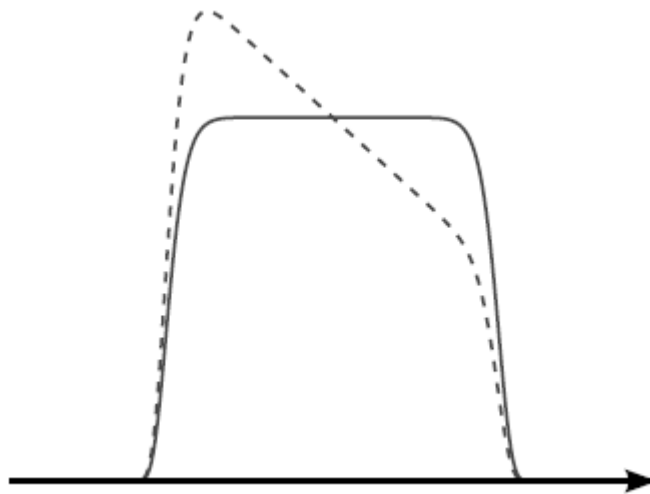
# Area of interest – 2D fit

- Request: ellipsoidal, not round
- Fit function: Fermi edge like later replaced by Super-gaussian
- Aol = area, where Super-Gaussian  $> 90\%$  of maximum



# Area of interest – 2D fit

- Issues with asymmetric distributions → fit didn't find parameters
- Try with plane multiplied on Super-gaussian (→possible characterization parameters): solved fitting issue but biased results:



- Issues solved by using non default fitting algorithm (Levenberg-Marquardt instead of trust-region-reflective)

# Filtering

- Necessity of filtering out those laser spots that will not work with the algorithm:
  - small BSA spots with non flat-top distribution
  - large BSA spot with inhomogeneous illumination of BSA (though asymmetric illumination should work)

Image: 20110413M\_1210.mat

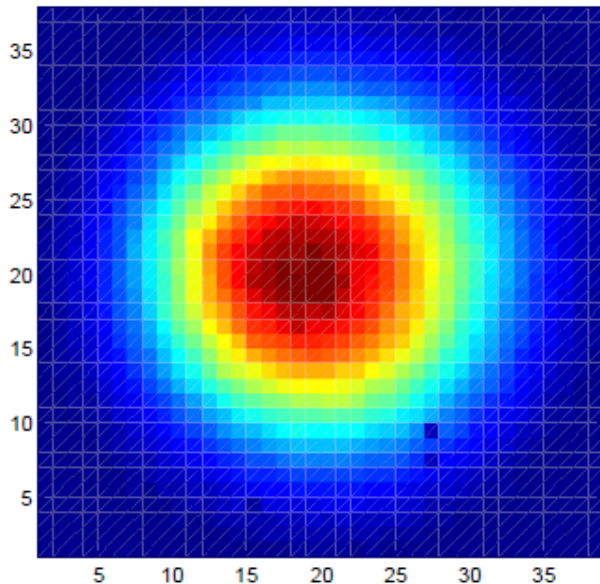


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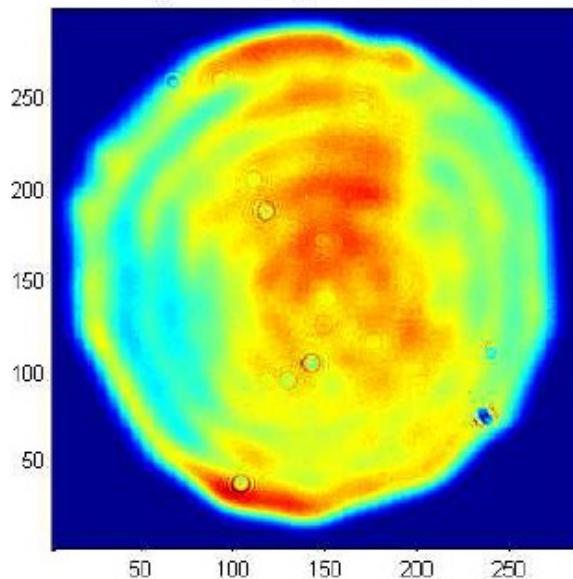
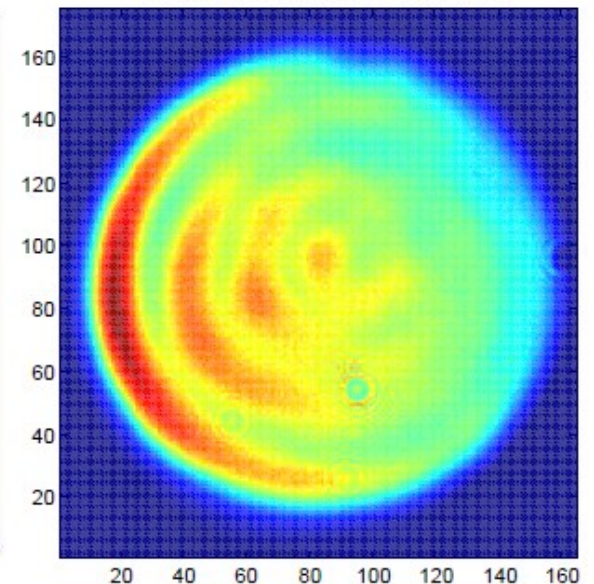
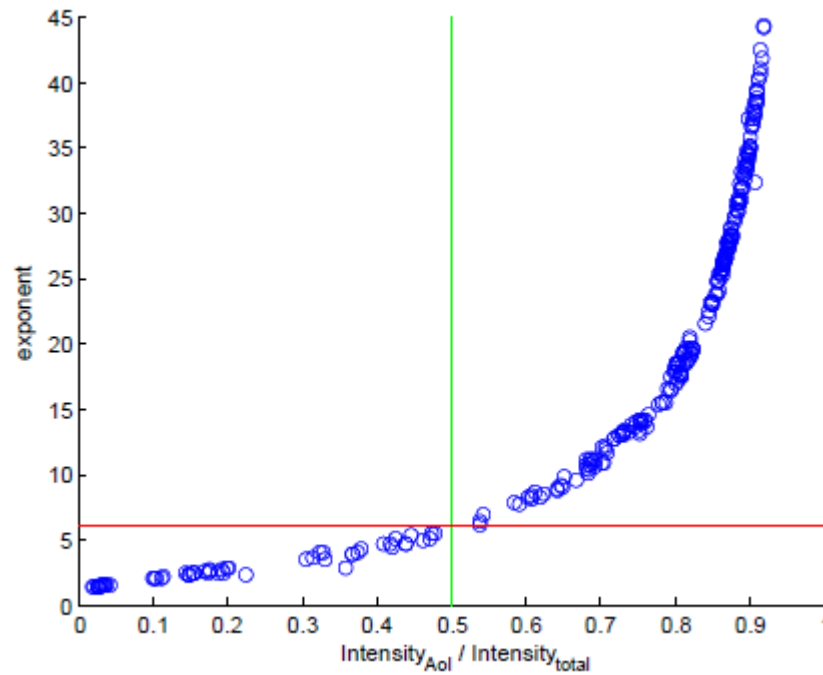


Image: 20110416N\_0441\_bsa07.mat



# Filtering

- Tried parameters: rms error from fit,  $\chi^2$ , exponent, BSA size, intensity,  $\frac{Intensity_{AoI}}{Intensity_{total}}$ ,  $\frac{rms\ error}{Amplitude}$
- Only working:  $\frac{Intensity_{AoI}}{Intensity_{total}}$  or exponent





# Beam characterization parameters

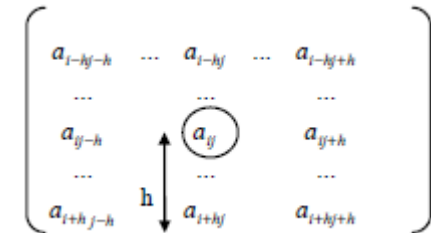
- Parameters: rms error from mean, skew, kurtosis, Intensity, 'Amplitude', BSA size, ratio of half axes,  $\frac{Intensity_{AoI}}{Intensity_{total}}$

- Spatial correlation (Fusco et al.):

$$\text{cov}(a, h) = \frac{1}{T} \sum_{i=1}^N \sum_{j=1}^M (a_{ij} - \langle a \rangle) \cdot (a_{ijh} - \langle a \rangle)$$

with 
$$a_{ijh} = \frac{1}{(2h+1)^2 - 1} \left[ \sum_{l=-h}^h \sum_{m=-h}^h a_{i+l, j+m} - a_{ij} \right]$$

→ 
$$\Lambda(a, h) = \frac{\text{cov}(a, h)}{\sigma_a^2}$$



- → almost correlation coefficient between  $a_{ij}$  and  $a_{ijh}$  → small difference for larger range of variation (found empirically by Fusco)

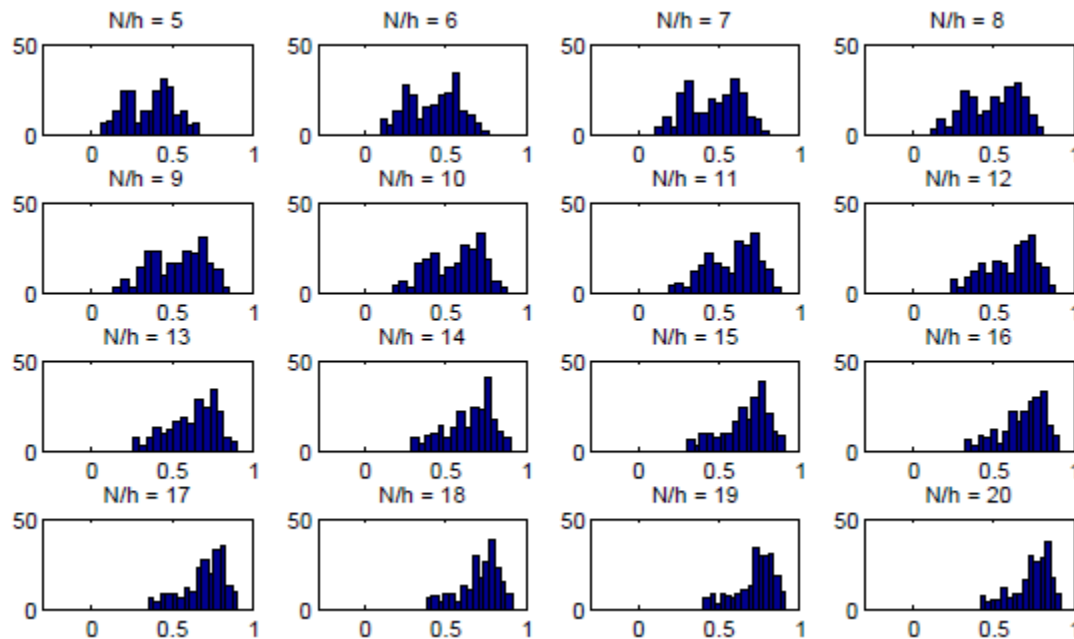


# Spatial correlation

➤ Problem: how large should  $h$  (=‘resolution’) be?

➤ Fusco:  $N/h=20$  (resolution relative to spot size)

➤ PITZ:



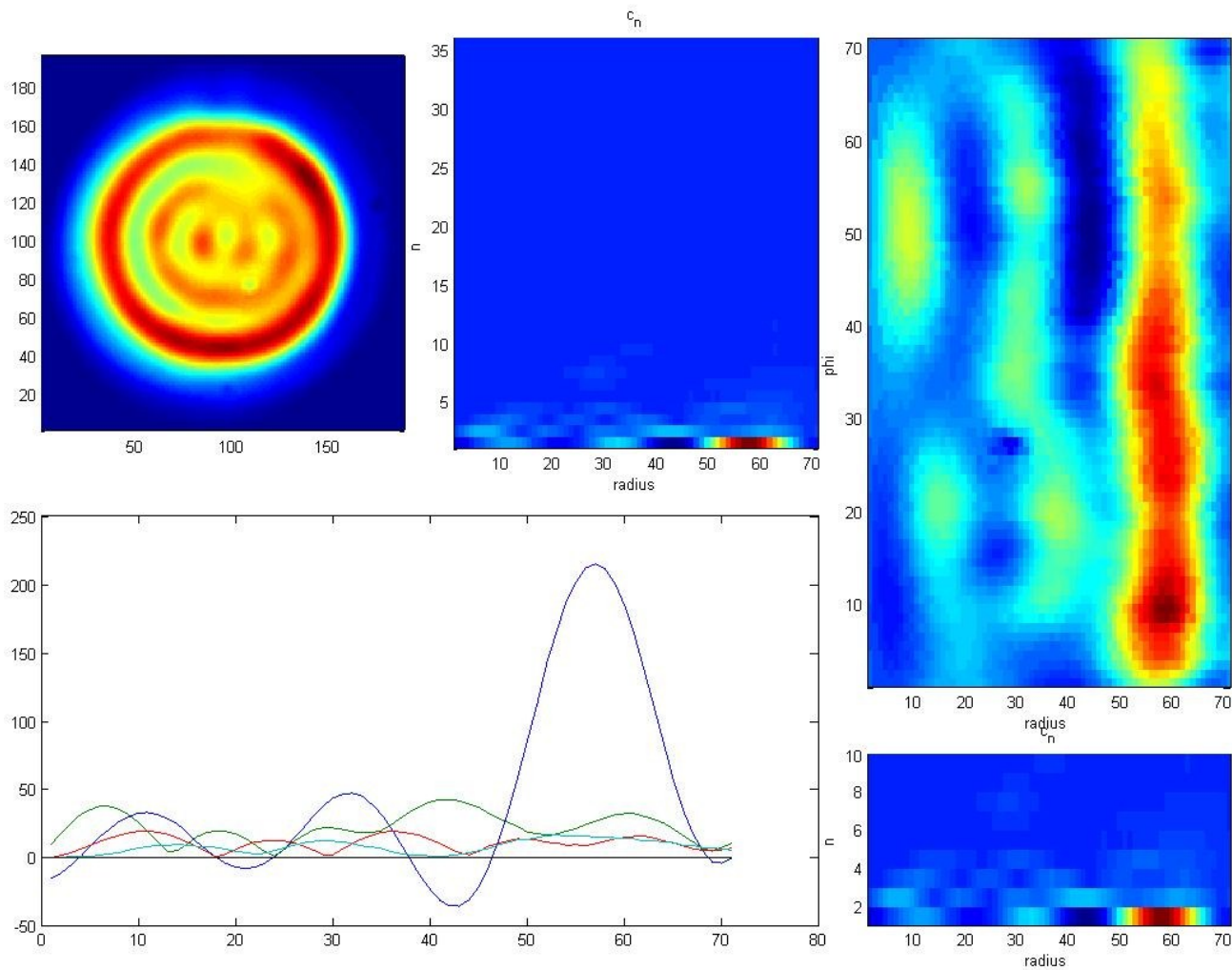
➤ → broadest distribution (range of variation) with  $N/h$  approx. 10, but no decision can be made without simulation or measurement of emittance

# Fourier and Bessel transform

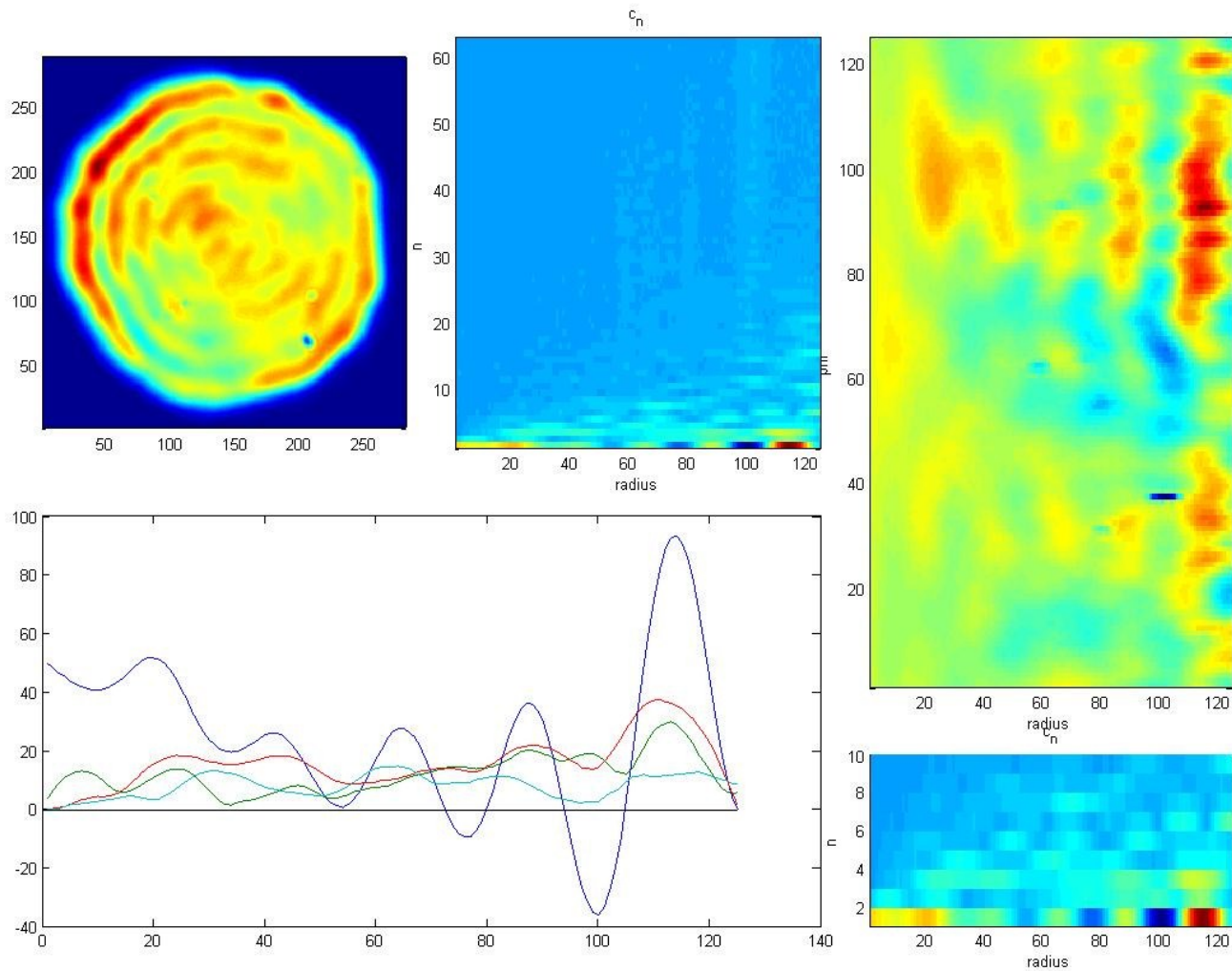
- Transforms of the laser spot in might help analyze the inhomogeneities with only few parameters
- Options: Fourier (diffraction pattern can be explained by Fourier optics) and Bessel functions (due to polar nature of diffraction pattern)
- Necessary: discrete Cartesian to polar coordinates → information loss
- Simple but good enough approach: smoothing of Cartesian spot, then get nearest pixel value for given polar coordinate
- Transform: either Fourier in azimuthal (definitely periodic) angle and Bessel in radius or Fourier in both



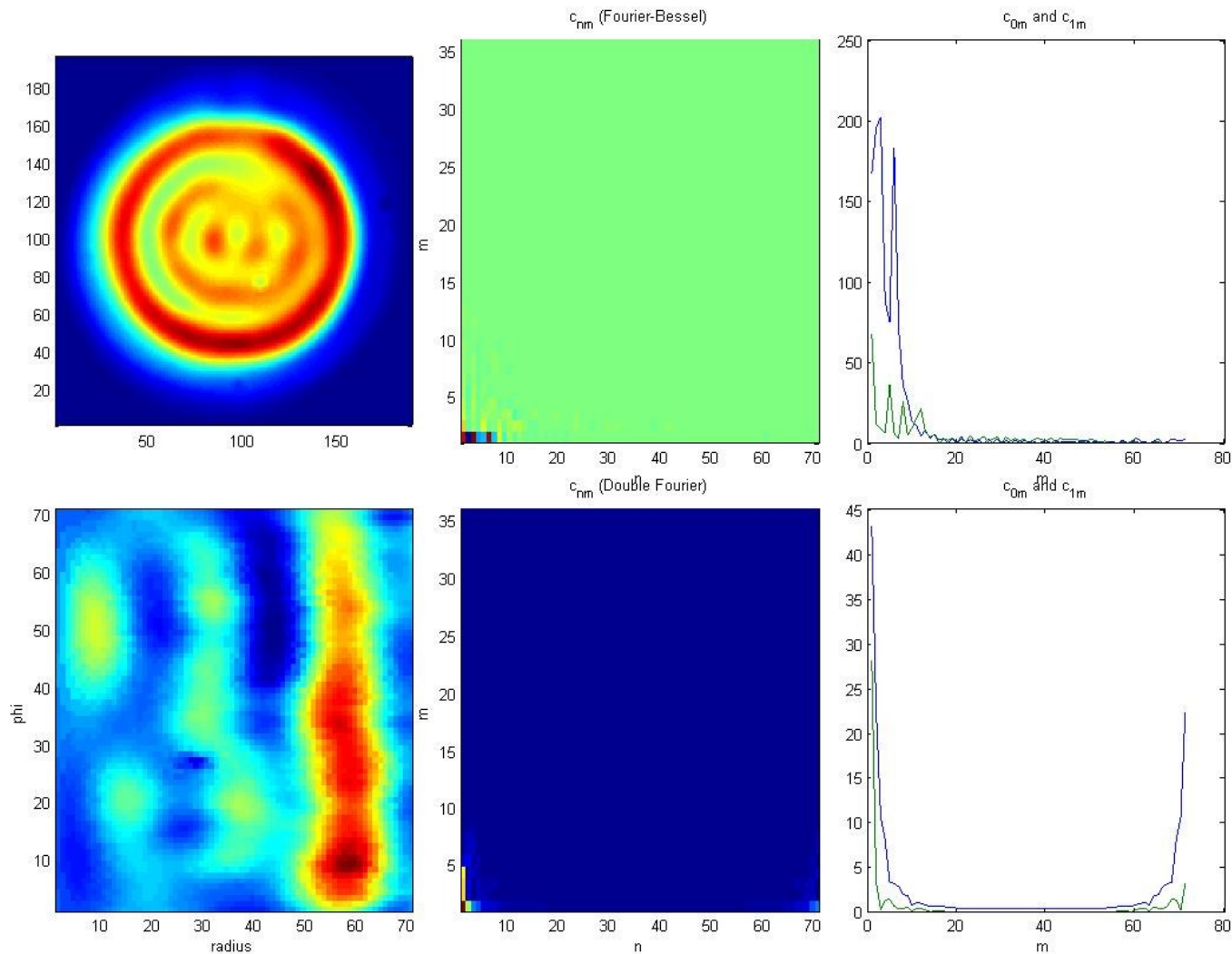
# Fourier transform in azimuthal angle only



# Fourier transform in azimuthal angle only



# Fourier or Bessel transform in radius



# Fourier or Bessel transform in radius

- > No interesting results, relatively broad spectrum, especially for Bessel function → obviously not good transform function
- > No single characterization parameters (e.g. line spectrum) from 2D transform
- > Some interesting results from “1D” Fourier transform



- Possible things to investigate from Fourier transform in azimuthal angle:
  - cut of at some frequency and look if back transform reproduces spot well (without noise and low frequency modulations of diffraction features)
  - 2D-→ 1D with weighted projection (→ reduction of parameters)
  - Correlation of  $c_n$  and  $c_0$  → distinguish between diffraction and inhomogeneous illumination of BSA

