

Optical Methods for transverse Beam Profile (Emittance) Diagnostics

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- Introduction
- Diagnostics for Linacs:
OTR, ODR, Screens



Accelerator Key Parameters

● light source: spectral brilliance

- measure for phase space density of photon flux

$$B = \frac{\text{Number of photons}}{[\text{sec}][\text{mm}^2][\text{mrad}^2][0.1\% \text{ bandwidth}]}$$

- user requirement: high brightness
 - lot of monochromatic photons on sample
- connection to machine parameters

$$B \propto \frac{N_\gamma}{\sigma_x \sigma_{x'} \sigma_z \sigma_{z'}} \propto \frac{I}{\varepsilon_x \varepsilon_z}$$

➤ requirements

i) high beam current

- achieve high currents
- cope with high heat load (stability)

● collider: luminosity \mathcal{L}

- measure for the collider performance

$$\dot{N} = \mathcal{L} \cdot \sigma$$

relativistic invariant proportionality factor between cross section σ (property of interaction) and number of interactions per second

- user requirement: high luminosity
 - lot of interactions in reaction channel
- connection to machine parameters

$$\mathcal{L} \propto \frac{I_1 \cdot I_2}{\varepsilon}$$

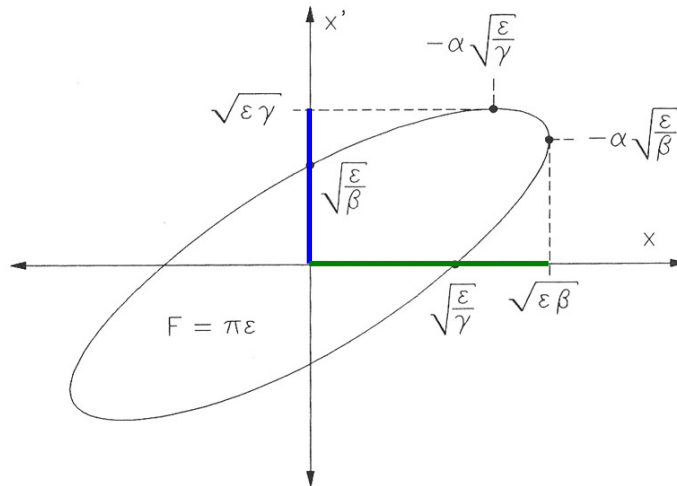
for two identical beams with emittances $\varepsilon_x = \varepsilon_z = \varepsilon$

ii) small beam emittance

- achieve small emittance (task of lattice designer)
- preserve emittance (stability)
- **measure small emittance**

Beam Emittance (Circ. Accelerator)

- projected area of transverse phase space volume
- emittance ε not directly accessible for beam diagnostics



beam size

$$\sigma = \sqrt{\varepsilon \beta}$$

beam divergence

$$\sigma' = \sqrt{\varepsilon \gamma}$$

- dispersion:

$$\sigma = \sqrt{\varepsilon \beta + (\eta \Delta p / p)^2}$$

$$\sigma' = \sqrt{\varepsilon \gamma + (\eta' \Delta p / p)^2}$$

- influence of physical process σ_{pp}

radiation generation

- monitor resolution σ_{mon}

measure \Rightarrow beam spot σ_s

calculate $\Rightarrow \varepsilon(\beta, \gamma, \eta, \eta', \Delta p / p, \sigma_s, \sigma_{\text{mon}}, \sigma_{pp})$

Radiation Generation: Considerations

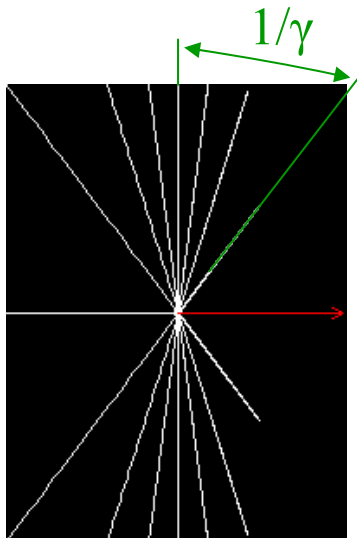
- radiation generation via particle interaction with matter

- luminescent screen monitors

- radiation generation via particle electromagnetic field

- particle electromagnetic field

- relativistic contraction characterized by Lorentz factor



electric field lines
in LAB frame

$$\gamma = E / m_0 c^2$$

E : total energy

$m_0 c^2$: rest mass energy

proton: $m_p c^2 = 938.272 \text{ MeV}$

electron: $m_e c^2 = 0.511 \text{ MeV}$

$\gamma \rightarrow \infty$: plane wave

- $mc^2 = 0 \text{ MeV}$:

light \rightarrow „real photon“

- ultra relativistic energies :

idealization \rightarrow „virtual photon“

Separation of Particle Field

- electromagnetic field bound to particle
observation in far field (large distances) } separate field from particle

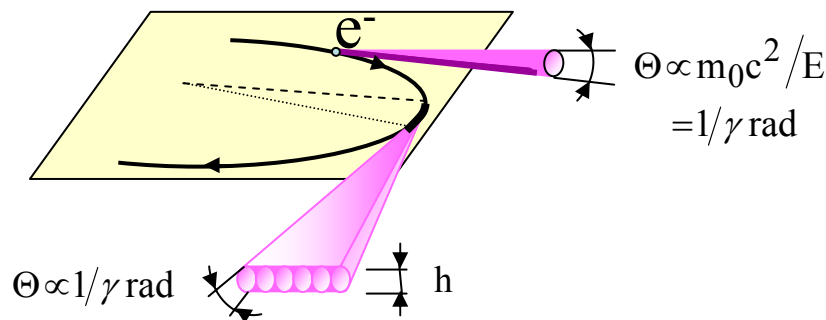
• separation mechanisms

- bending of particle via magnetic field

synchrotron radiation



circular accelerators



linear accelerators: no particle bending ???

- diffraction of particle electromagnetic field via material structures

exploit analogy between real/virtual photons:

- | | | | |
|--|---|--|---|
| - light reflection/refraction at surface | ↔ | backward/forward transition radiation (TR) | ← |
| - light diffraction at edges | ↔ | diffraction radiation (DR) | ← |
| - light diffraction at grating | ↔ | Smith-Purcell radiation | ← |
| - light (X-ray) diffraction in crystal | ↔ | parametric X-ray radiation (PXR) ... | ← |

- **profile monitors at linear accelerators**
 - experience from **FLASH @ DESY**
 - of special interest for the **European XFEL @ DESY**
 - **standard:** Optical Transition Radiation (OTR) based monitors
 - **trends:** Optical Diffraction Radiation (ODR) based monitors
 - **pitfalls:** comments on coherent radiation production

- **luminescent screen monitors**
 - beam tests @ MAMI: October 2009

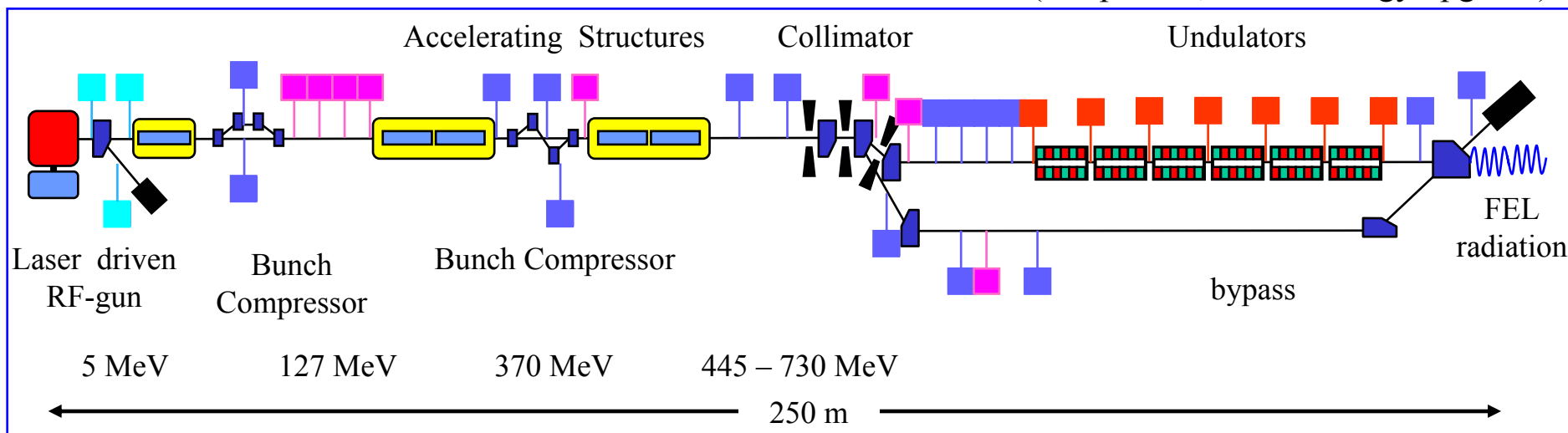
- **(high resolution profile monitors at circular accelerators)**
 - trends in synchrotron radiation based diagnostics

- **(synchrotron radiation for proton beam diagnostics)**





Trans. Profile Diagnostics @ FLASH

FLASH

(setup 2005, before energy upgrade)



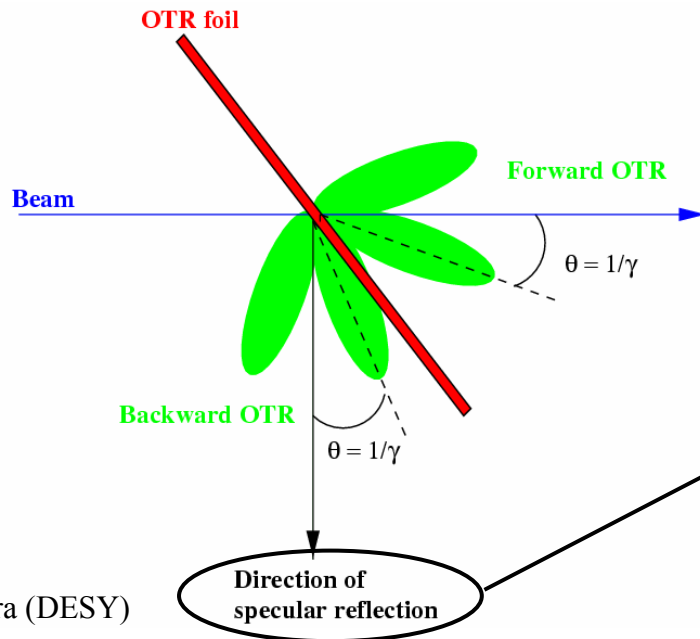
transverse beam profile monitors:

-  **3 Ce:YAG screens**
-  **16 OTR stations**
-  **8 OTR + WS stations**
-  **7 WS stations (hor.+ vert.)**

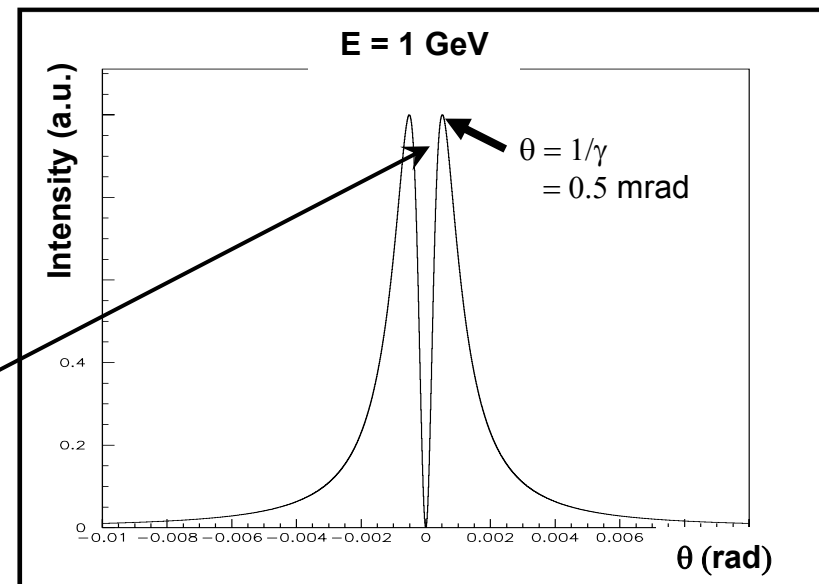
courtesy: K. Honkavaara (DESY)

Optical Transition Radiation

- **transition radiation:** electromagnetic radiation emitted when a charged particle crosses boundary between two media with different optical properties
- **visible part:** **Optical Transition Radiation (OTR)**
- **beam diagnostics:** backward OTR (reflection of virtual photons)
typical setup: image beam profile with optical system
→ beam image and measurements of beam shape and size
- **advantage:** fast single shot measurement, linear response (neglect coherence !)
- **disadvantage:** high charge densities may destroy radiator



angular distribution

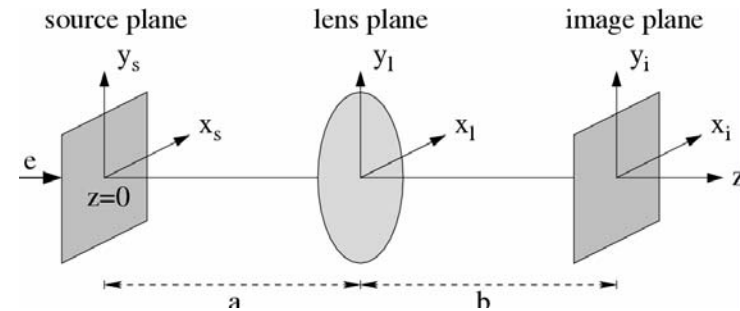
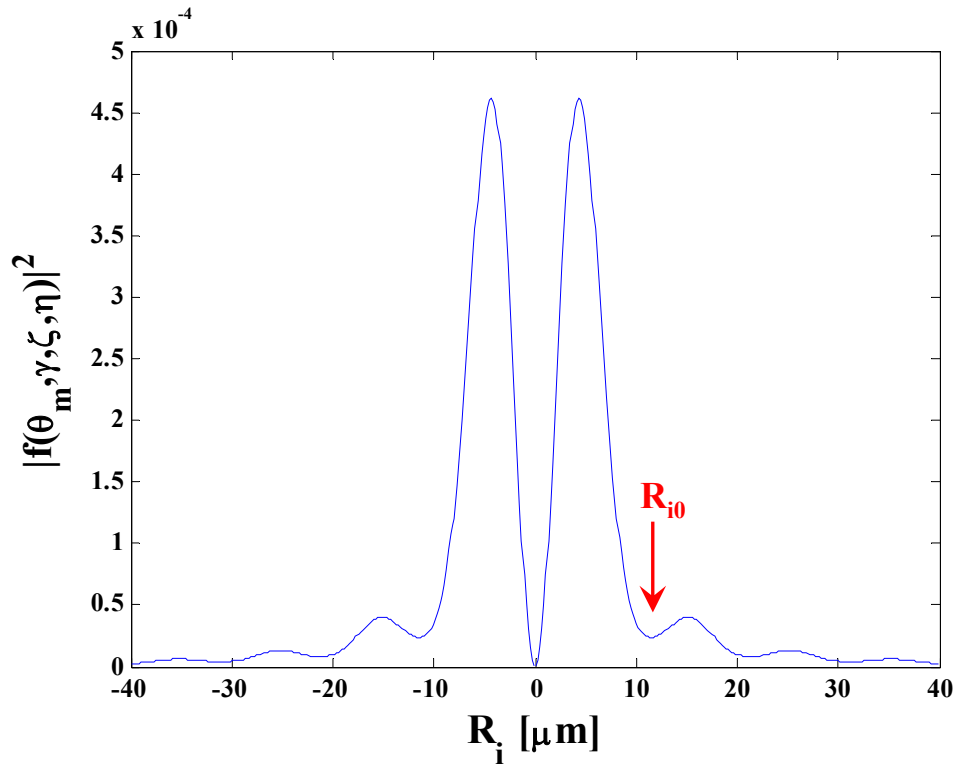


courtesy:
K. Honkavaara (DESY)

OTR Monitor Resolution

● calculation of point spread function in image plane

G. Kube, TESLA-FEL Report 2008-01



➤ parameters of calculation

E = 1 GeV
 $\lambda = 500 \text{ nm}$
f = 250 mm
a = b = 500 mm (1:1 imaging)
lens- $\varnothing = 50.8 \text{ mm}$

● OTR resolution

➤ resolution definition according to classical optics:

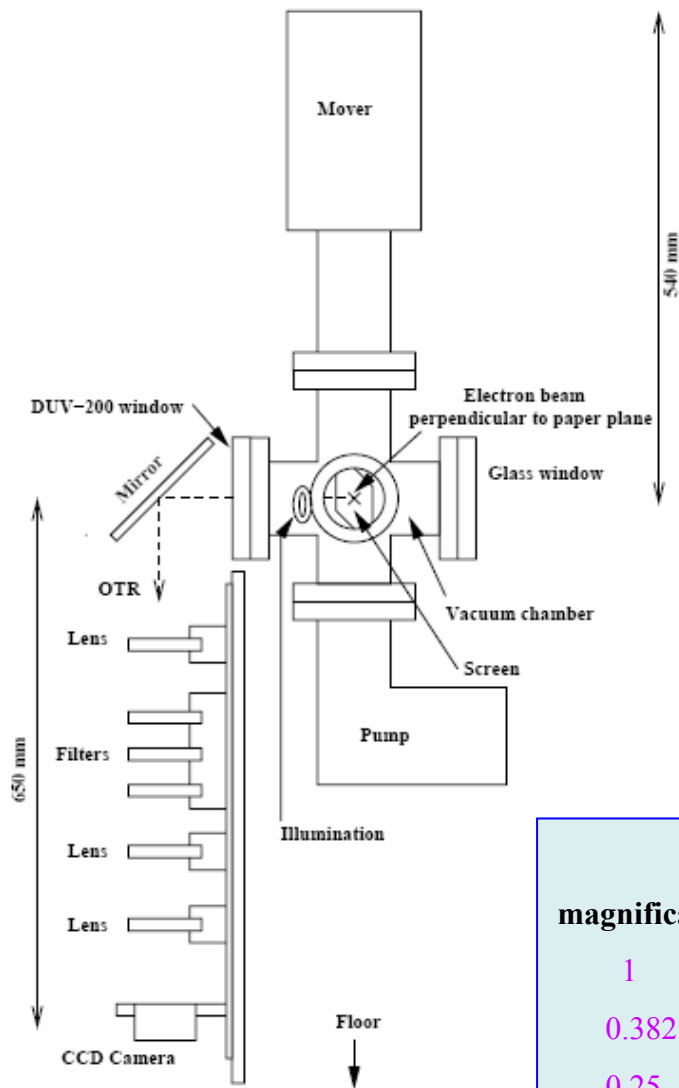
⇒ first minimum of PSF (→ diameter of Airy disk)

$$R_{i0} \approx 1.12 \frac{M\lambda}{\theta_m}$$

M: magnification

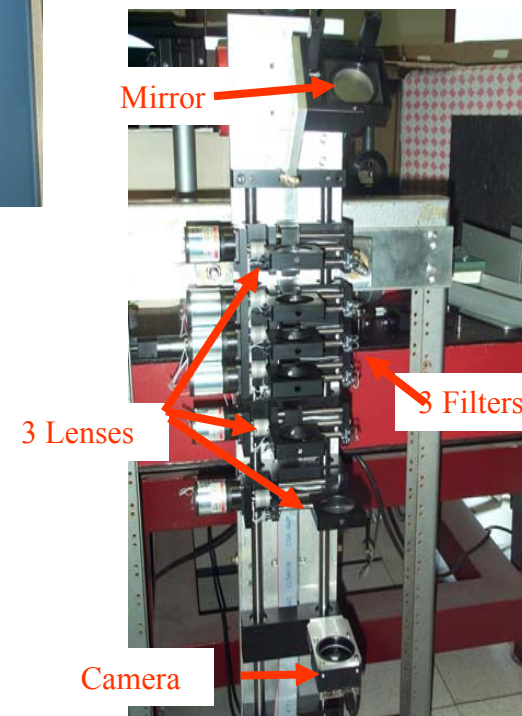
θ_m : lens acceptance angle

OTR Monitors at FLASH



K. Honkavaara et al.,
Proc. PAC 2003, p.2476

optical system			
magnification	f / mm	a / mm	b / mm
1	250	500	500
0.382	200	724	276
0.25	160	800	200



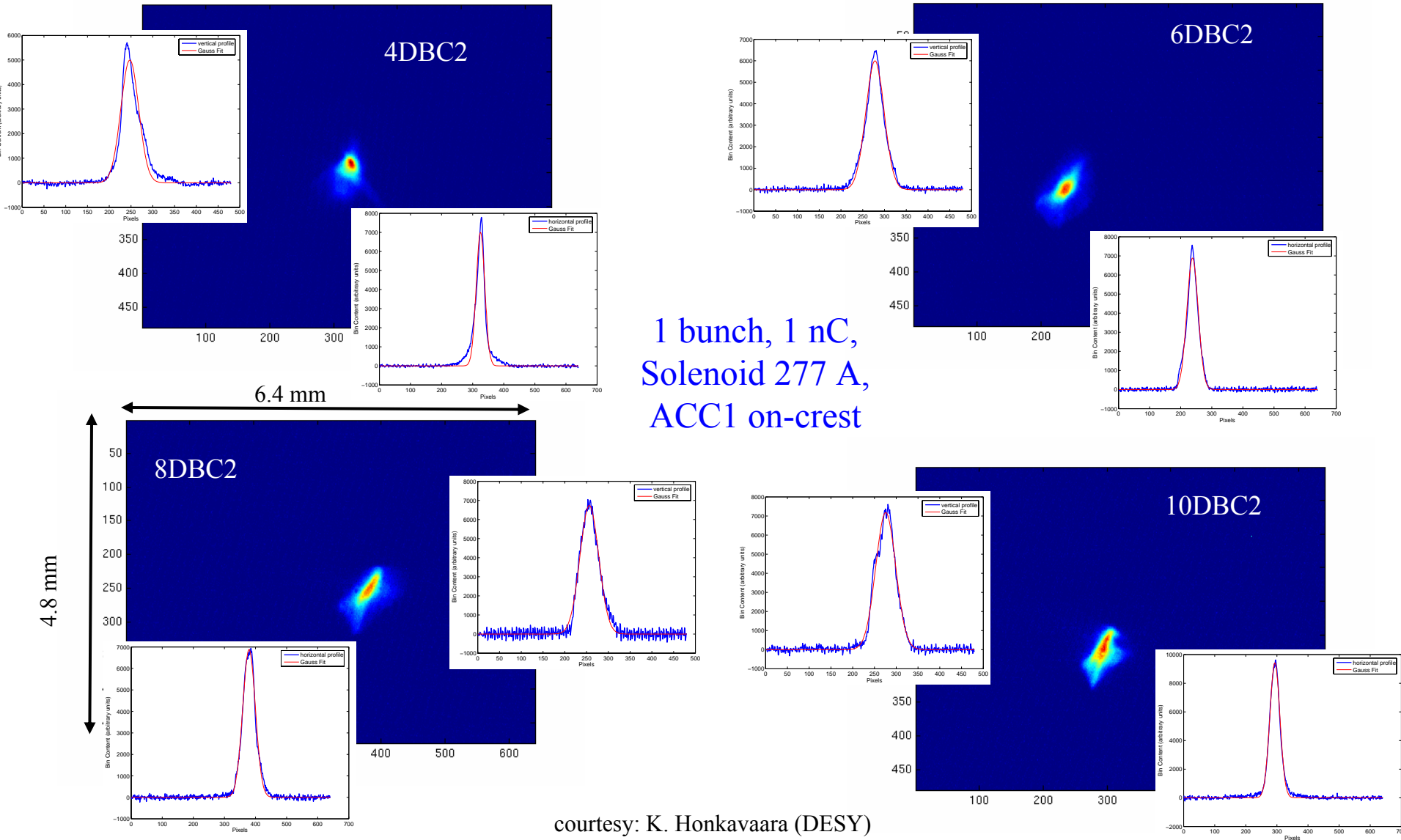
OTR Monitors at FLASH

Emittance Measurement Setup at the Injector

courtesy: K. Honkavaara (DESY)



Example of Beam Images (matched)



Optical Diffraction Radiation (ODR)

- **problem OTR:** screen degradation/damage
 - limited to only few bunch operation, no permanent observation
- **ODR:** excellent candidate to measure beam parameters parasitically

➤ DR generation via interaction between the EM fields of the moving charge and the conducting screen

→ diffraction of “virtual photons”

➤ extension of EM field of a relativistic particle is flat circle

→ radius $\lambda\beta\gamma/2\pi$

➤ radiation intensity scales proportional to $|E|^2$:

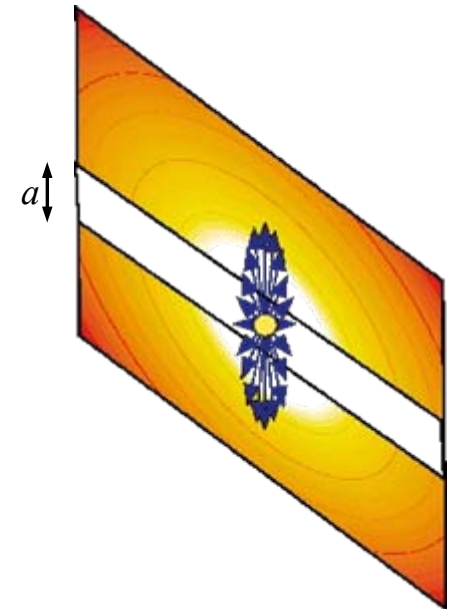
$$I \propto e^{-a/h_{\text{int}}} \quad \text{with} \quad h_{\text{int}} = \frac{\lambda\beta\gamma}{4\pi}$$

➤ dependency on impact parameter h_{int} :

$a \gg h_{\text{int}}$: no radiation

$a \cong h_{\text{int}}$: DR

$a \ll h_{\text{int}}$: TR



Principle of ODR Diagnostics

- **imaging with ODR:** no beam image, illuminated slit
→ seems not suitable for beam diagnostics
nevertheless, attempts to use ODR imaging:

A. Lumpkin et al., Proc. BIW 2008, TUPTPF061

- **exploit ODR angular distribution:**

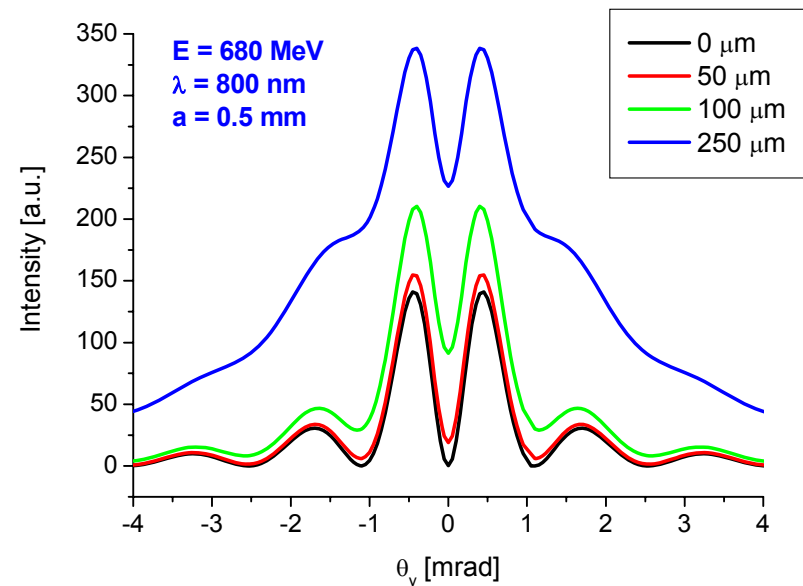
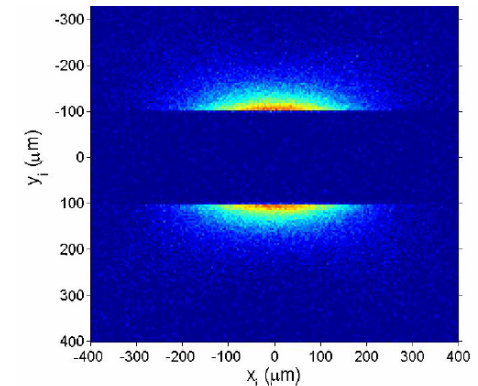
visibility of interference fringes can be used to determine transverse size of a bunch of electrons crossing the slit

→ increasing σ_y both the peak intensity and the central minimum increase

- **research project @ FLASH**



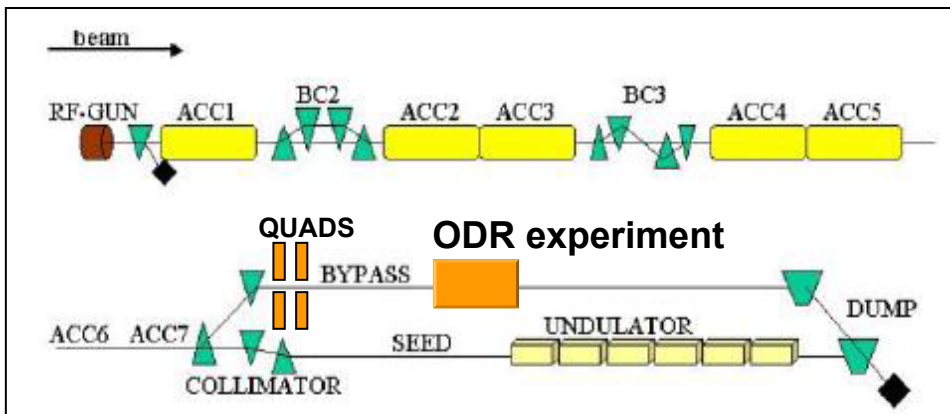
D. Xiang et al., PRST AB 10, 062801 (2007)



courtesy: E. Chiadroni (INFN)

ODR Experimental Setup @ FLASH

overview

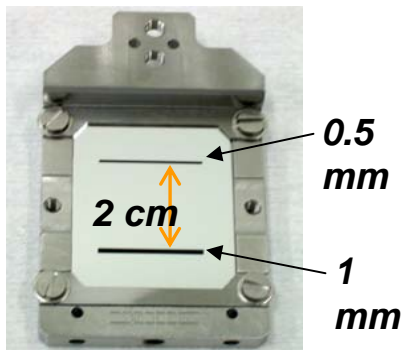


- › high energy, up to 1 GeV
- › long bunch trains, up to 800 bunches per macro-pulse
- › repetition rate 5 Hz
- › good long term stability
- › small transverse emittance, ~ 2 mm mrad

target

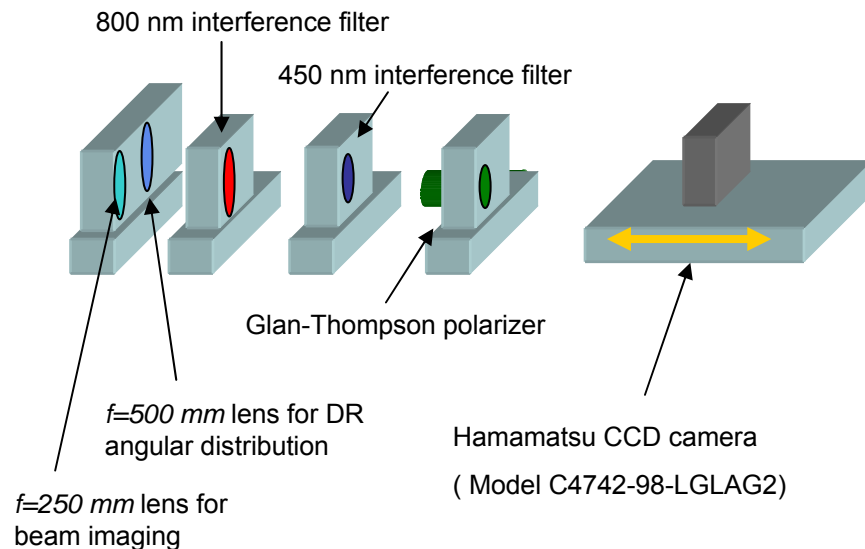
realized with **lithographic technique**:

starting from silicon nitride wafer, opening slit by means of chemical etching.



Al deposition enhances reflectivity more than a factor of 2

optical system



● CCD image



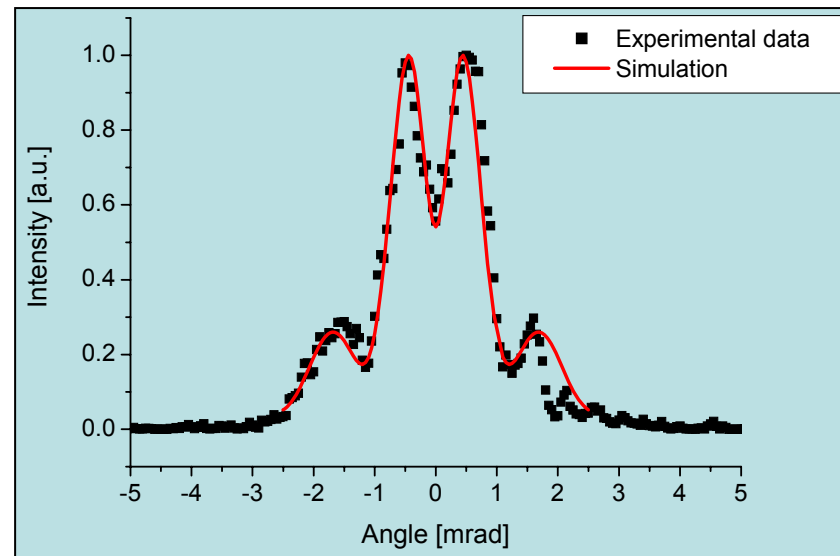
Beam transport optimization

- 0.7 nC
- 25 bunches
- 2 s exposure time
- E_{beam} (nominal) = 680 MeV
- 800 nm filter and polarizer in

● comparison

Simulation parameters:

- $a = 0.5$ mm
- Gaussian distributed beam
- $\sigma_y = 80$ μm
- $\sigma'_y = 125$ μrad
- $E_{\text{beam}} = 610$ MeV



E. Chiadroni, M. Castellano, A. Cianchi, K. Honkavaara, G. Kube, V. Merlo, F. Stella,

Non-intercepting electron beam transverse diagnostics with optical diffraction radiation at the DESY FLASH facility

NIM B 266 (2008) 3789–3796 and Proc. of PAC 2007, p.3982

ODR Interferometry (ODRI)

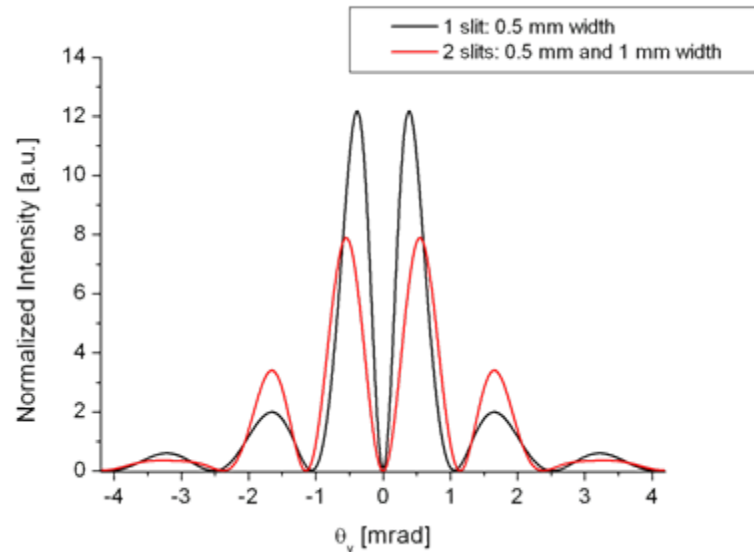
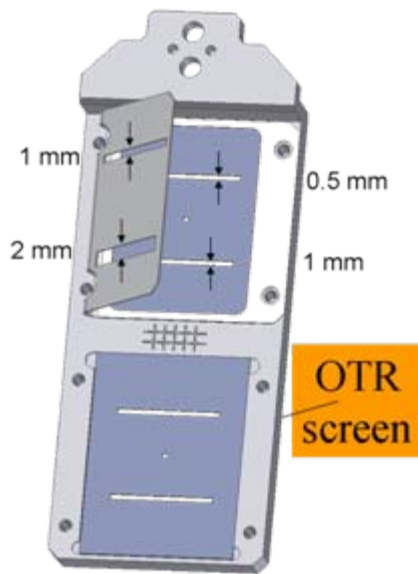
- reduction of synchrotron radiation background

courtesy: E. Chiadroni (INFN)

→ stainless steel shield in front of ODR screen with larger cut

In the case of a wavelength of 800 nm and 1 GeV beam energy the 1 mm cut is not large enough to prevent the production of ODR in the forward direction, reflected by the screen and interfering with the backward ODR produced by the screen itself.

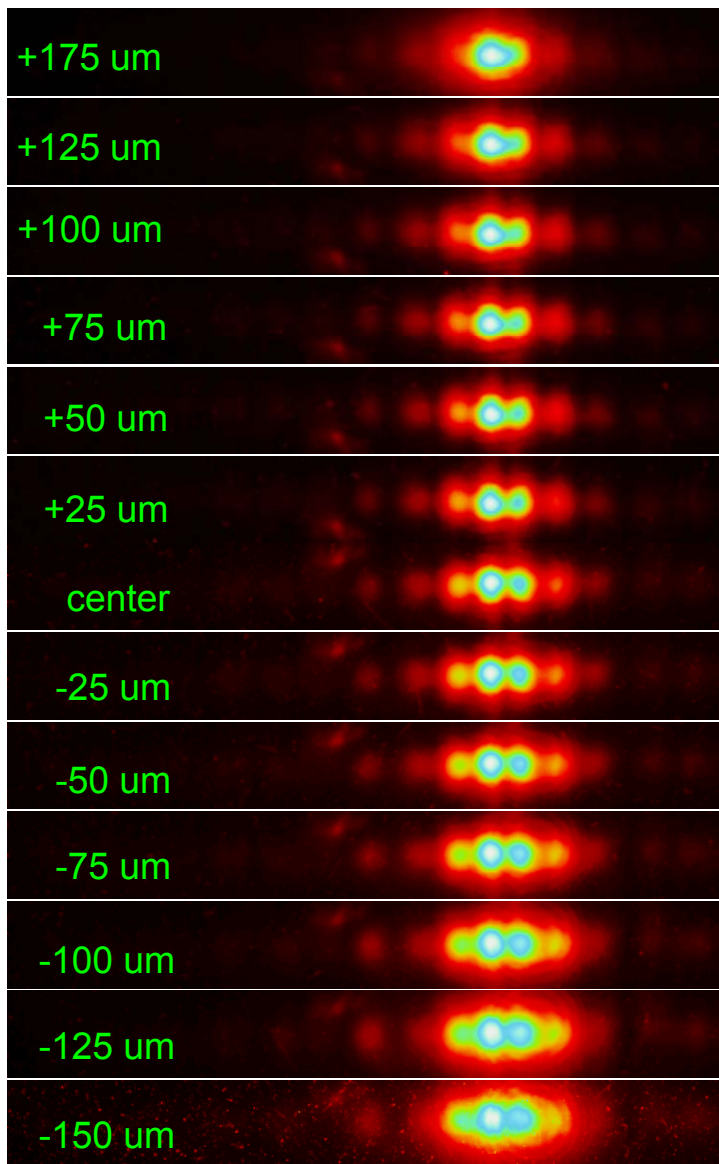
An ODR analogous of the Wartski interferometer used for OTR, with the difference that in this case the two interfering amplitudes are different in intensity and angular distribution



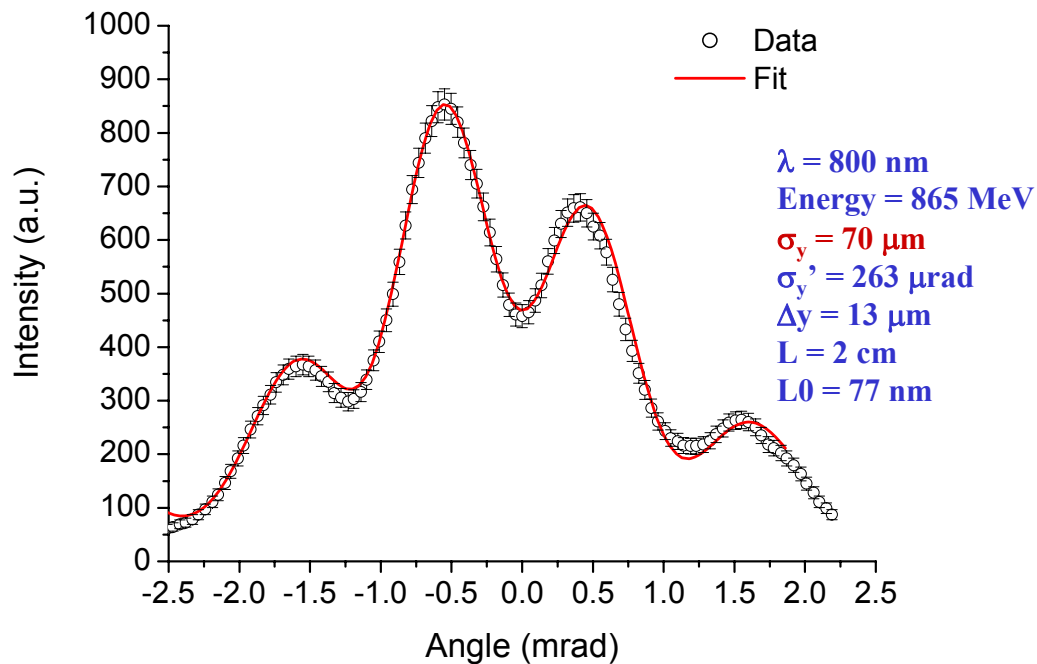
Single particle going through the center of both slits with 900 MeV energy and 800 nm wavelength

ODRI Measurements

courtesy: E. Chiadroni (INFN)



- transverse scan within the slit
- fit of ODRI angular distribution



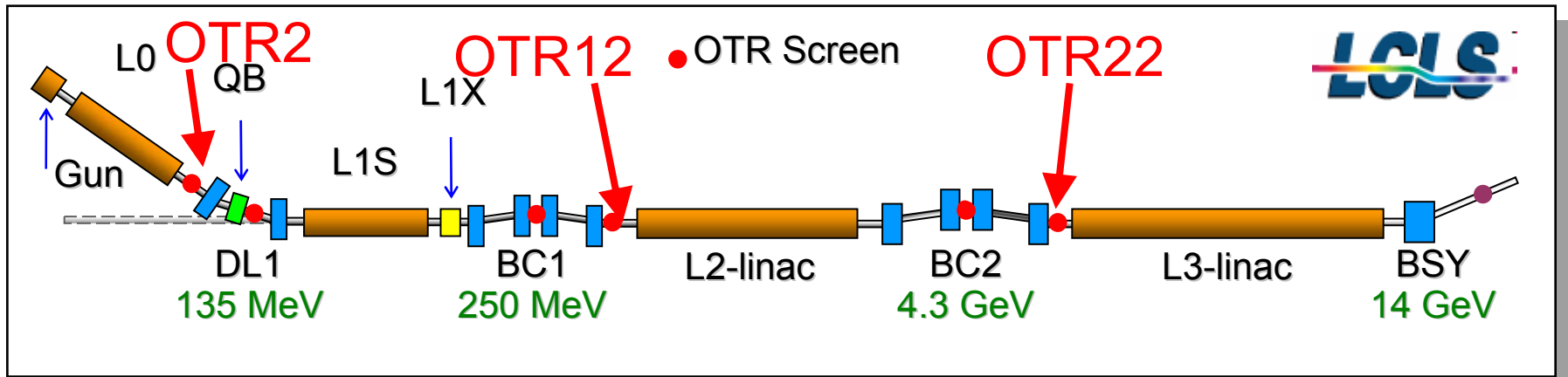
*E. Chiadroni, M. Castellano, A. Cianchi, K. Honkavaara, G. Kube,
Optical diffraction radiation interferometry as electron transverse diagnostics
Proc. DIPAC 2009, p.151*

⇒ activities to explore ODRI properties will continue this year after redesign of target and optics

OTR/ODR Diagnostics: Pitfalls

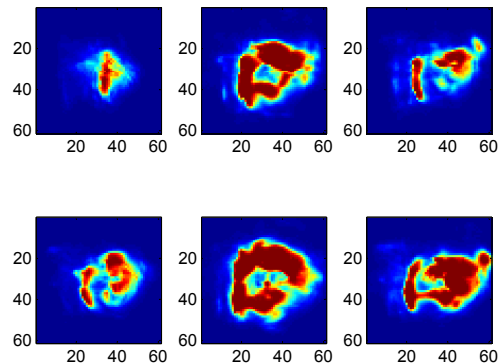
Linac Coherent Light Source (LCLS) @ SLAC

courtesy: H. Loos (SLAC)

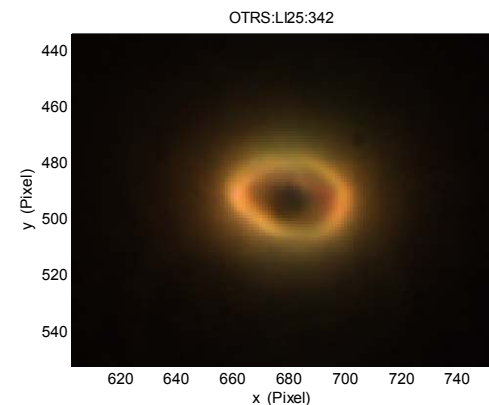


OTR monitor observation with BC1, BC2 switched on

OTR 12



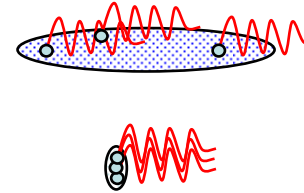
OTR 22



⇒ measured spot is no image of beam

Coherent OTR (COTR)

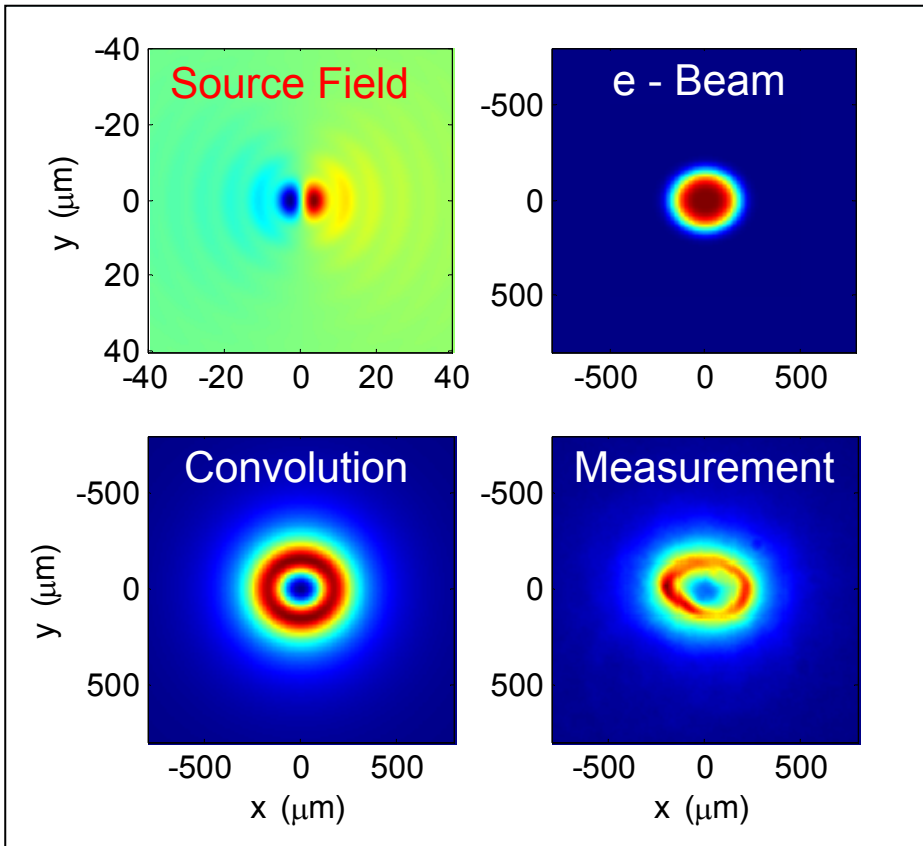
- interpretation: coherent OTR emission
 - strong compression in bunch compressors
- simulation



long bunch ($\lambda < \sigma_z$)

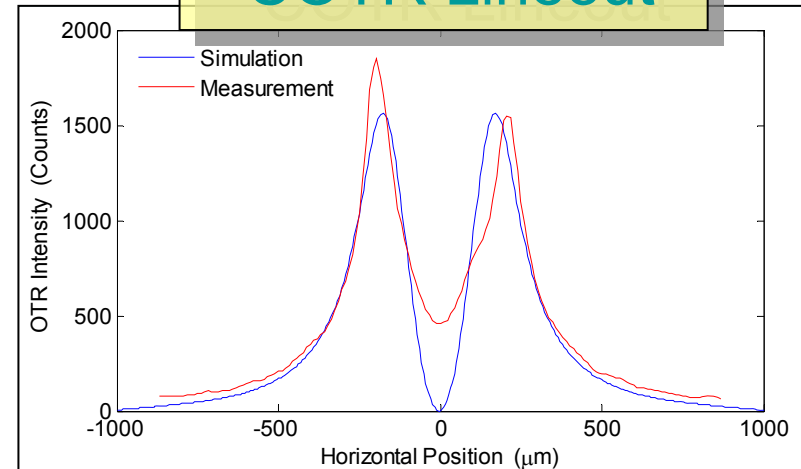
short bunch ($\lambda > \sigma_z$)

H. Loos et al., Proc. FEL 2008, p.485



OTR22, 250 pC, 4.3 GeV
10 μm bunch length
100 μm rms beam size
Super-Gaussian

COTR Lineout



Consequences

- **LCLS: coherent emission compromise use of OTR as reliable beam diagnostics**

→ wire scanners for transverse beam diagnostics instead of OTR

- **XFEL: experience from FLASH**

→ no COTR observation in standard operation

...better to be prepared in advance...

- **alternative schemes for transverse profile diagnostics**

- ▶ **ODRI**

coherent effects may also appear → possibility to extract information from angular distribution ???

- ▶ **TR at smaller wavelengths (EUV-TR)**

test experiment performed March 2010

- ▶ **screen monitors**

widely used at hadron accelerators, nearly no information available for high energy electron machines

⇒ **motivation for test experiment**

Inorganic Scintillators

properties

- radiation resistant → widely used in high energy physics, astrophysics, dosimetry,...
- high stopping power → high light yield
- short decay time → reduced saturation

generation of scintillation light

- energy conversion (characteristic time $10^{-18} - 10^{-9}$ sec)

Formation of el. magn. shower. Below threshold of e^+e^- pair creation relaxation of primary electrons/holes by generation of secondary ones, phonons, plasmons, and other electronic excitations.

- thermalization of secondary electrons/holes ($10^{-16} - 10^{-12}$ sec)

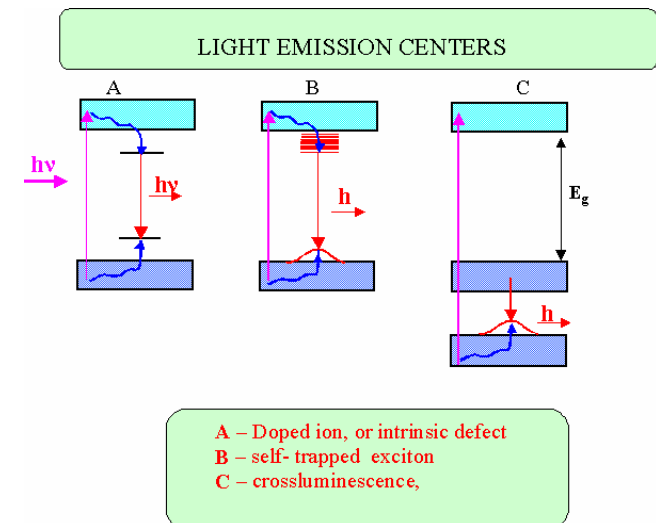
Inelastic processes: cooling down the energy by coupling to the lattice vibration modes until they reach top of valence resp. bottom of conduction band.

- transfer to luminescent center ($10^{-12} - 10^{-8}$ sec)

Energy transfer from e-h pairs to luminescent centers.

- photon emission ($> 10^{-10}$ sec)

radiative relaxation of excited luminescence centers



Implication on Transverse Resolution

Which effects may affect transverse resolution ?

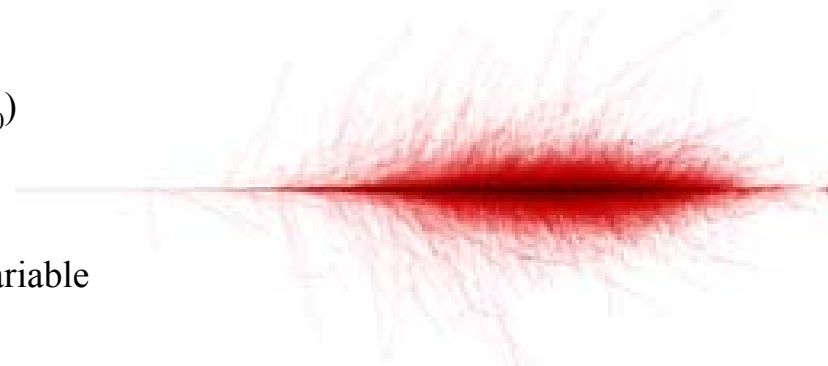
- ▶ light generation: energy conversion → transverse range of ionization
- ▶ light propagation → total reflection at scintillator surface

● energy conversion

- ▶ „thick target“ : formation of electromagnetic shower
(thickness in the order of radiation length X_0)
- ▶ transverse shower dimension: *Molière radius* as scaling variable
→ containing 90% of shower energy

$$R_M \approx 0.0265 X_0 (Z + 1.2)$$

X_0 : radiation length, Z : atomic number



F. Schmidt, "CORSIKA Shower Images",
<http://www.ast.leeds.ac.uk/~fs/showerimages.html>

Implication on Transverse Resolution

energy loss

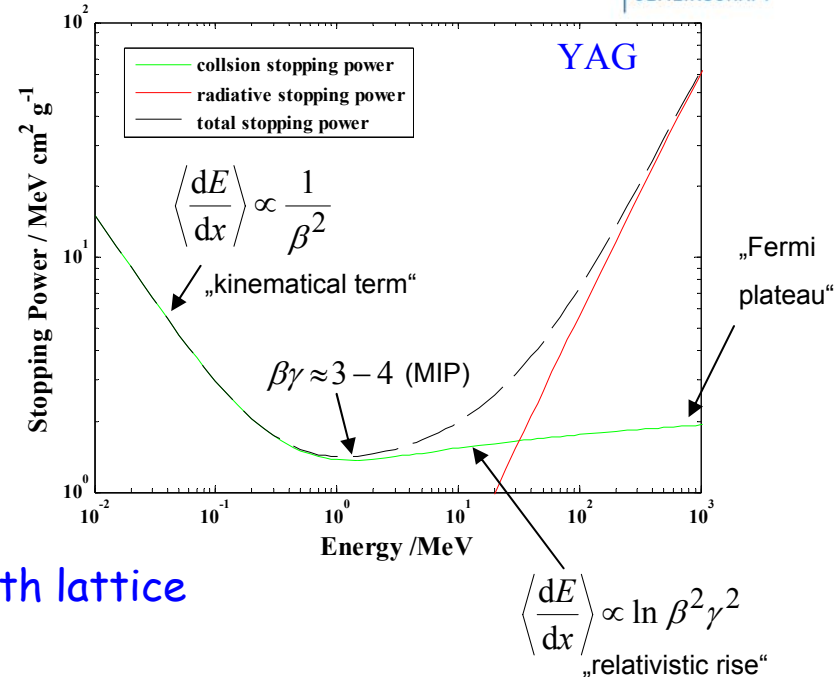
- Bethe-Bloch (collision)
- Bremsstrahlung (radiative)

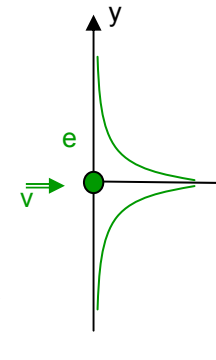
energy deposition in "thin target"

- ignore radiative contribution
 - thickness / $X_0 \approx 10^{-2}$
 - small amount of re-absorption in material

ionization: interaction of particle em. field with lattice

- particle field
 - virtual photons, in classical picture transverse evanescent waves
- relativistic rise
 - increase of transverse field extension
- Fermi plateau
 - cancellation of incoming particle field by induced polarization field of electrons in medium
 - saturation range as scaling variable R_δ





$\vec{E} \propto e^{-y/y_0}$

with $y_0 = \tilde{\lambda} \beta_m \gamma_m$
 $\beta_m = \beta \sqrt{\epsilon(\omega)}$

Implication on Transverse Resolution

extension radius

- limiting value:

$$R_{\delta} = \frac{c}{\omega} \sqrt{1 - \varepsilon(\omega)}$$

$\varepsilon(\omega)$: complex dielectric function

- approximation as free electron gas (Drude model)

$$R_{\delta} = \frac{\hbar c}{\hbar \omega_p}$$

ω_p : plasma frequency

$$\hbar \omega_p = 28.816 \sqrt{\rho \langle Z/A \rangle} \text{ eV}$$

light propagation

- light generated inside scintillator has to cross surface

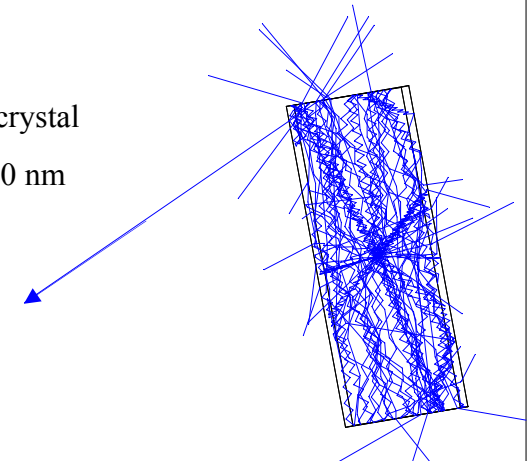
refractive index n

inorganic scintillators

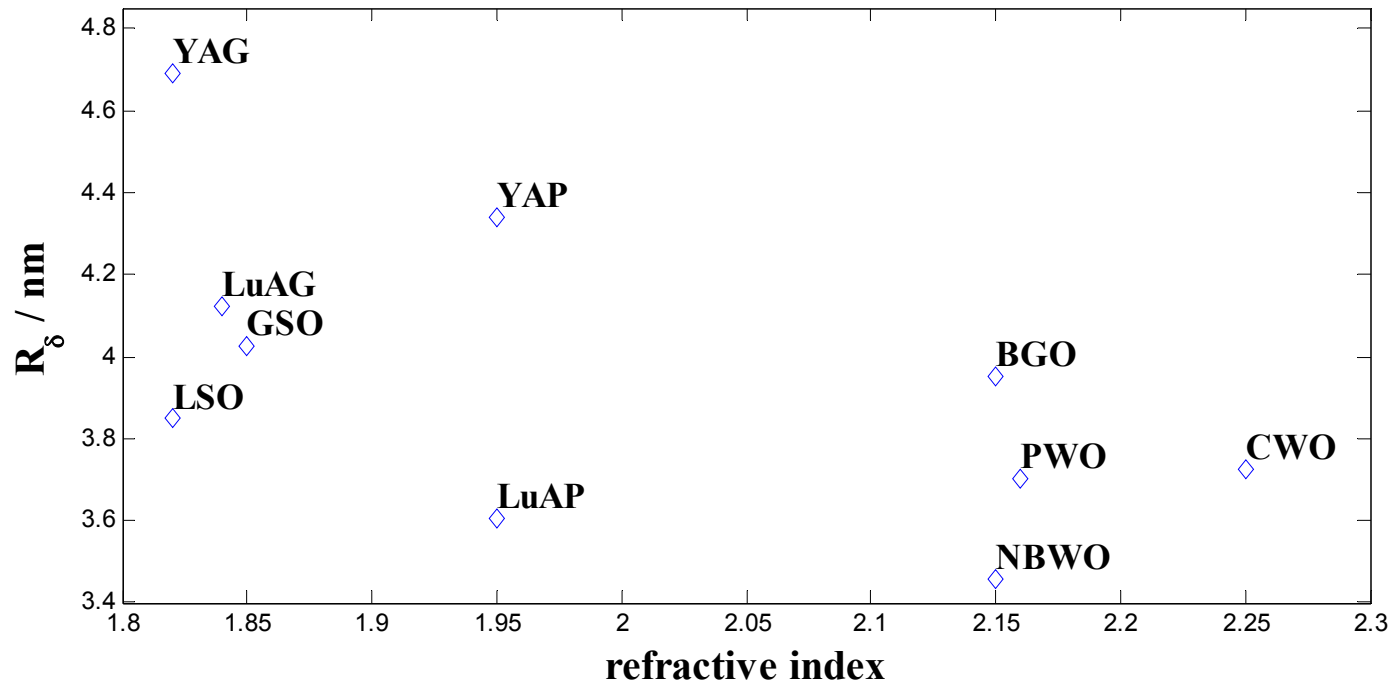
→ high n , i.e. large contribution of total reflection

BGO crystal

$\lambda = 480 \text{ nm}$



Scintillator Material Properties

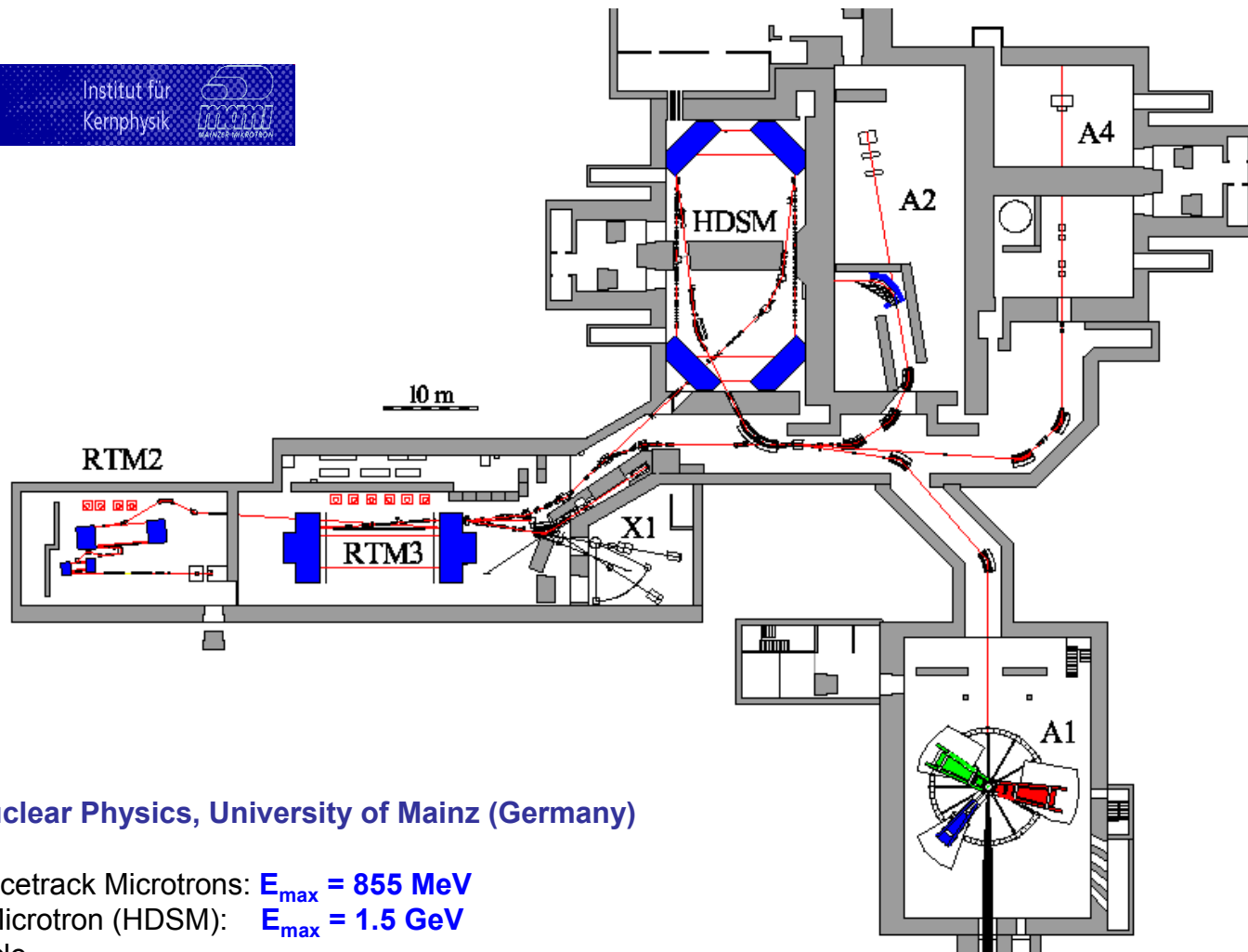


scintillators under investigation

- BGO: 0.5 mm
- PWO: 0.3 mm
- LYSO: 0.8 mm, 0.5 mm
(Prelude 420)
- YAG: 1.0 mm, 0.2 mm, phosphor

	ρ [g/cm ³]	$\hbar\omega_p$ [eV]	R_M [cm]	λ_{\max} [nm]	yield [1/keV]	n @ λ_{\max}	R_δ [nm]
BGO	7.13	49.9	2.23	480	8	2.15	3.95
PWO	8.28	53.3	2.00	420	0.1	2.16	3.70
LSO:Ce	7.1	51.3	2.08	420	32	1.82	3.85
YAG:Ce	4.55	45.5	2.77	550	11	1.95	4.34

Mainz Microtron MAMI

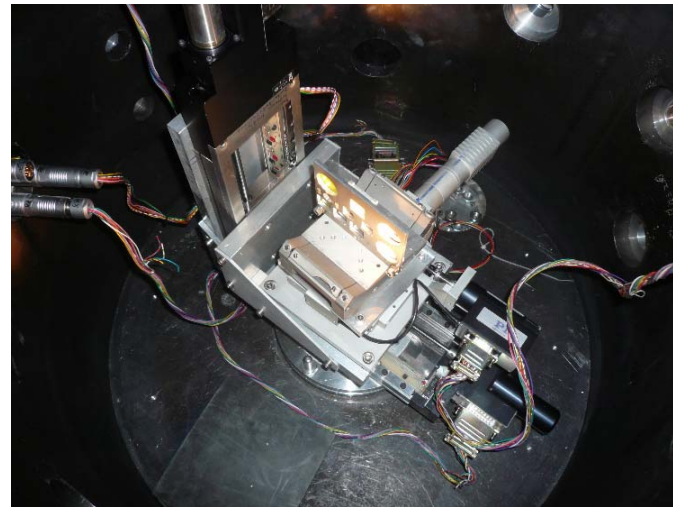
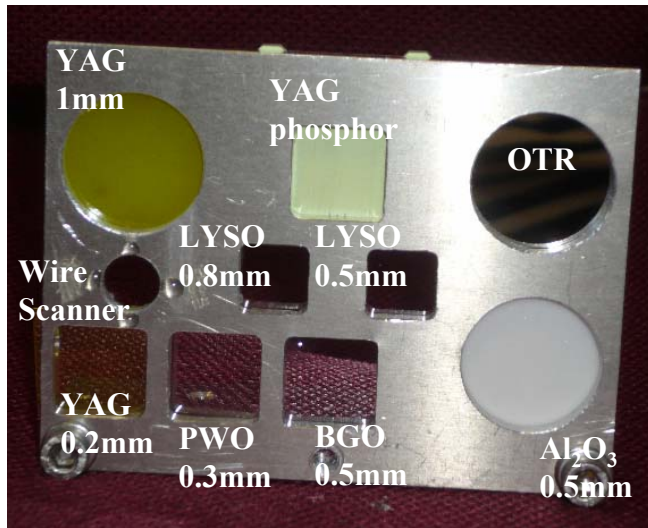


Institute of Nuclear Physics, University of Mainz (Germany)

3 cascaded Racetrack Microtrons: $E_{\max} = 855 \text{ MeV}$
double-sided Microtron (HDSM): $E_{\max} = 1.5 \text{ GeV}$
100 % duty cycle
polarized electron beam ($\sim 80\%$)

Experimental Setup

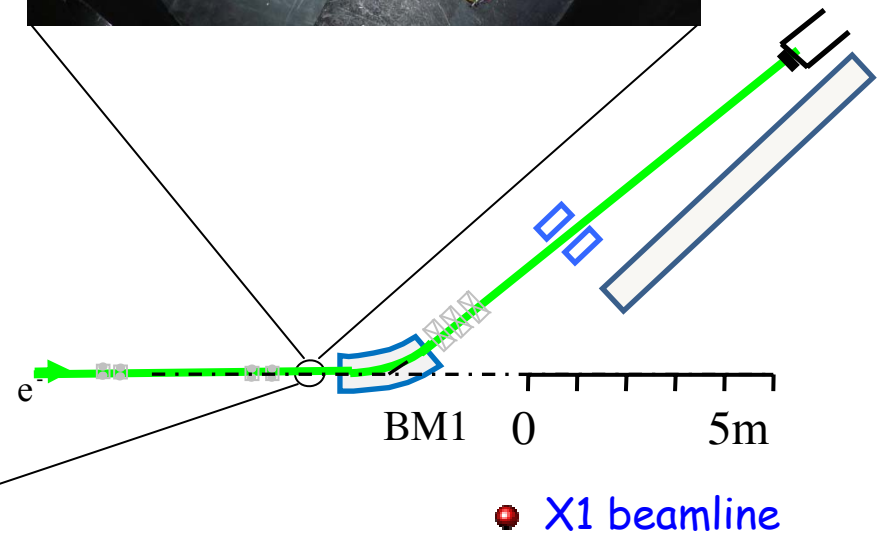
target



observation geometry

-22.5° w.r.t. beam axis

camera: BASLER A311f
659 x 494 pixel
pixel size 9.9 μ m x 9.9 μ m



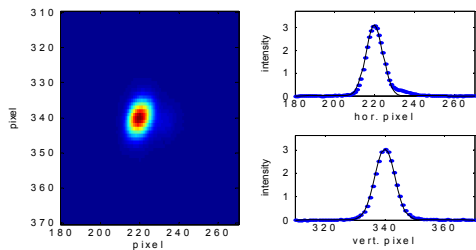
Beam Images

measurement and analysis:

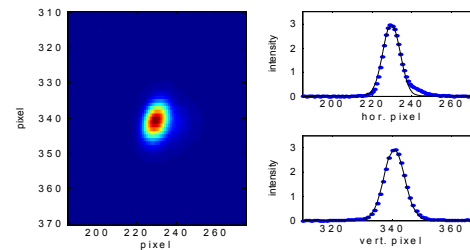
I = 46 pA

5 signal and 1 background frame

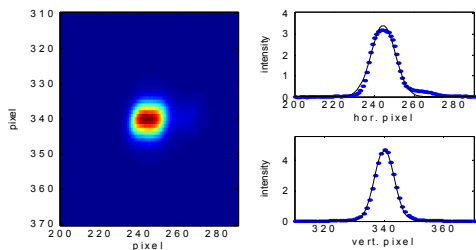
➤ LYSO:Ce
(0.5mm)



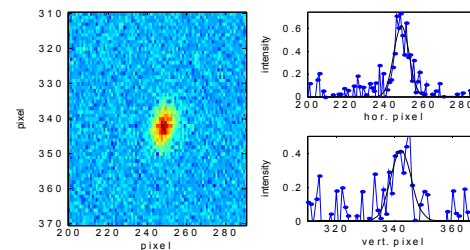
➤ BGO
(0.5mm)



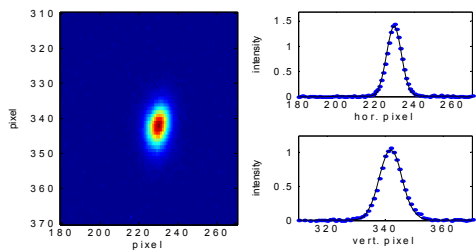
➤ LYSO:Ce
(0.8mm)



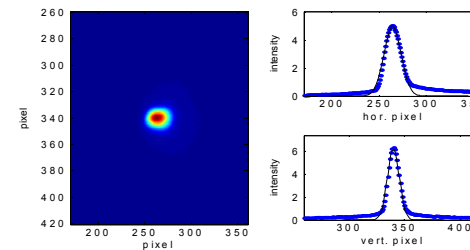
➤ PWO
(0.3mm)



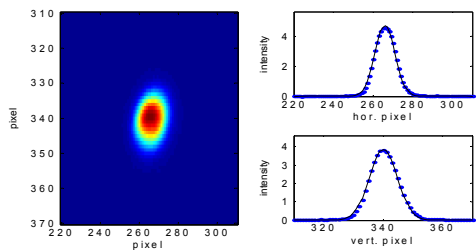
➤ YAG:Ce
(powder)



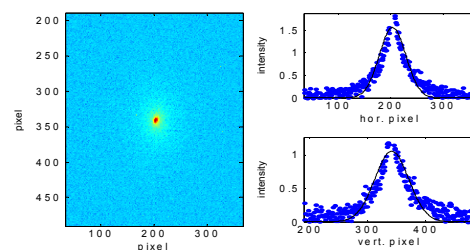
➤ YAG:Ce
(1mm)



➤ YAG:Ce
(0.2mm)



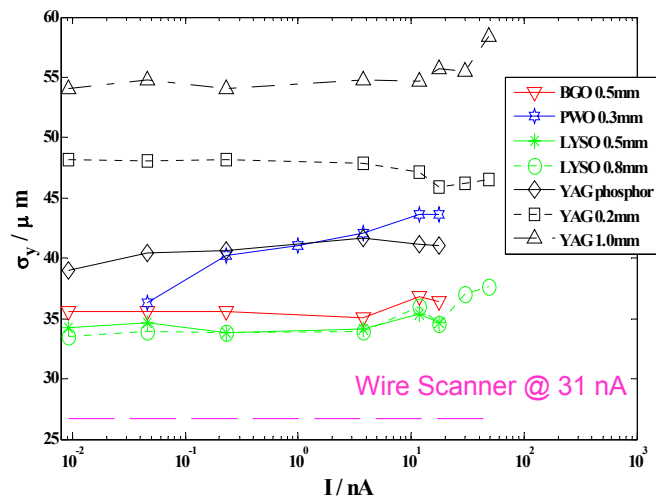
➤ Al₂O₃
(0.5mm)



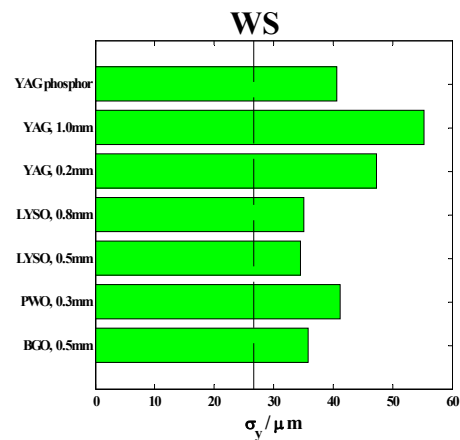
different scale!

Results

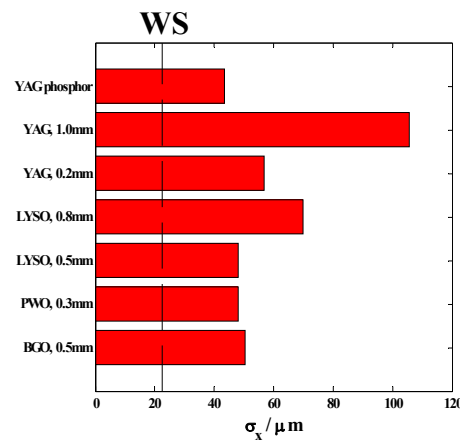
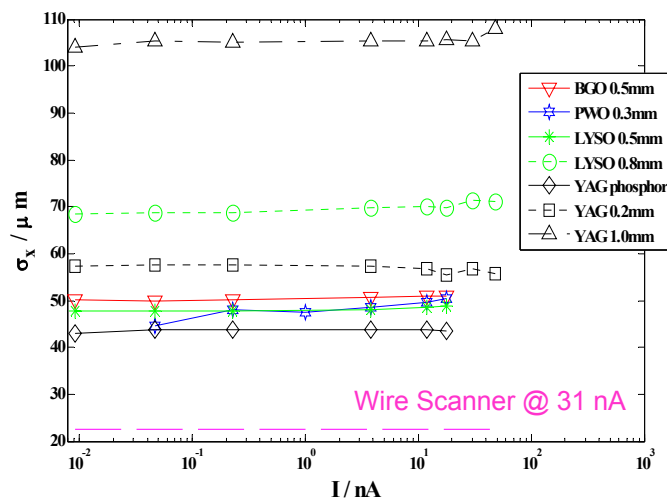
vertical beam size



mean values



horizontal beam size



⇒ dependency on observation geometry

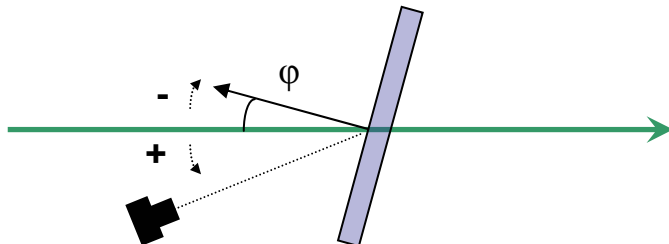
Observation Geometry

● beam diagnostics

→ popular OTR-like observation geometry:

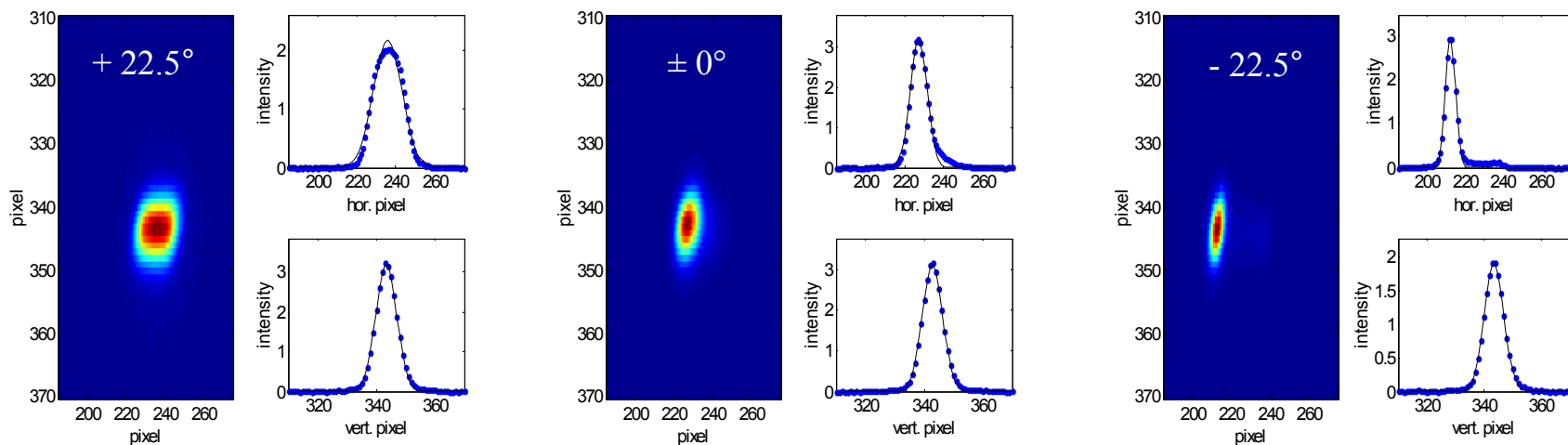
- 45° tilt of screen
- observation under 90°

● scintillator tilt versus beam axis

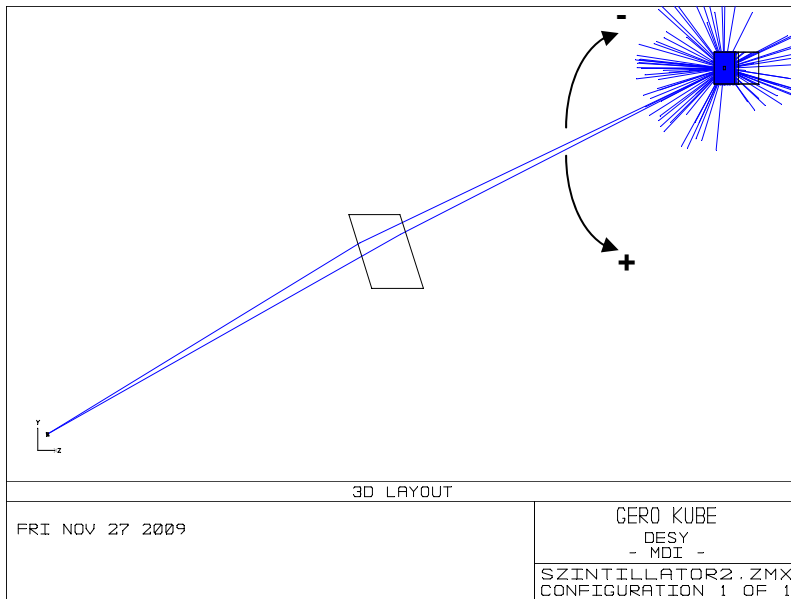


- BGO crystal
- micro-focused beam
- $I = 3.8 \text{ nA}$

● measured beam spots



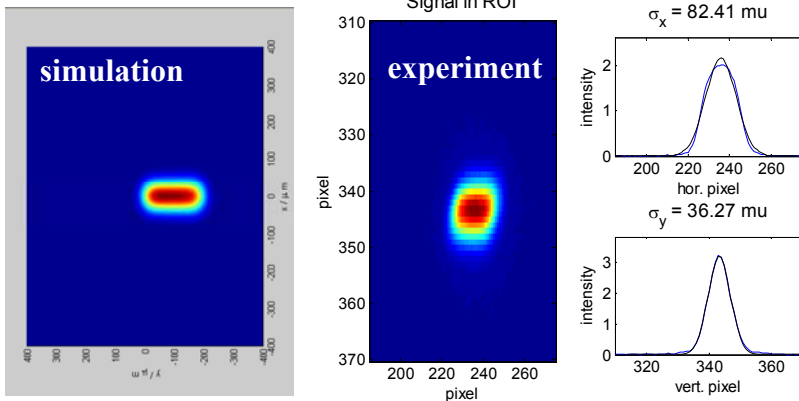
Simulation of Light Propagation



Analysis:

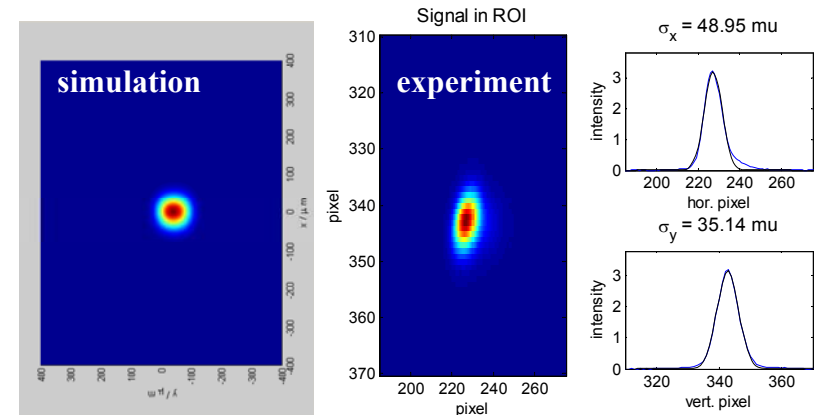
- ZEMAX calculation of 2-dim PSF
- calculation of 2-dim beam profile
- convolution of PSF and beam profile
- horizontal / vertical projection of resulting distribution
- determination of 2nd moment (standard deviation)

➤ + 22.5°

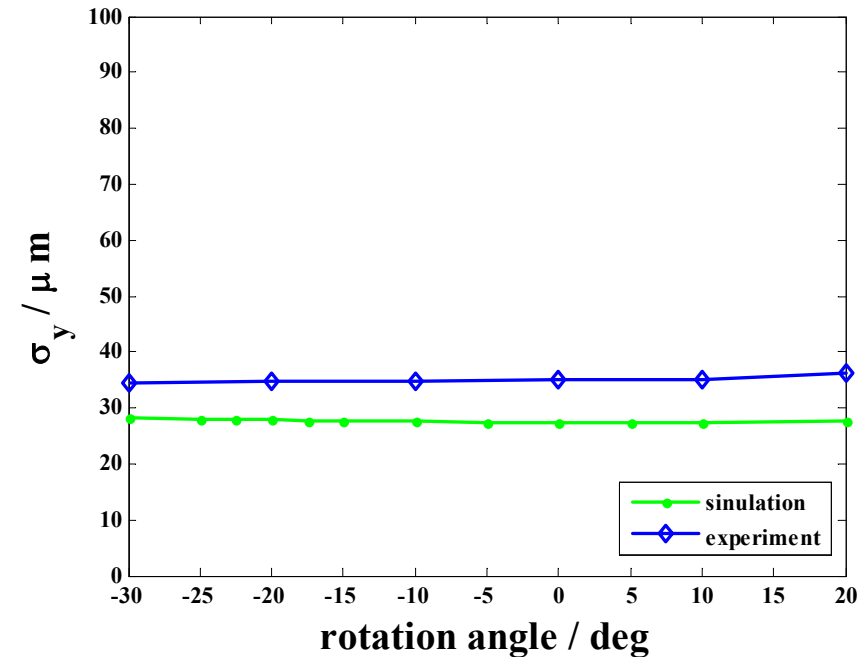
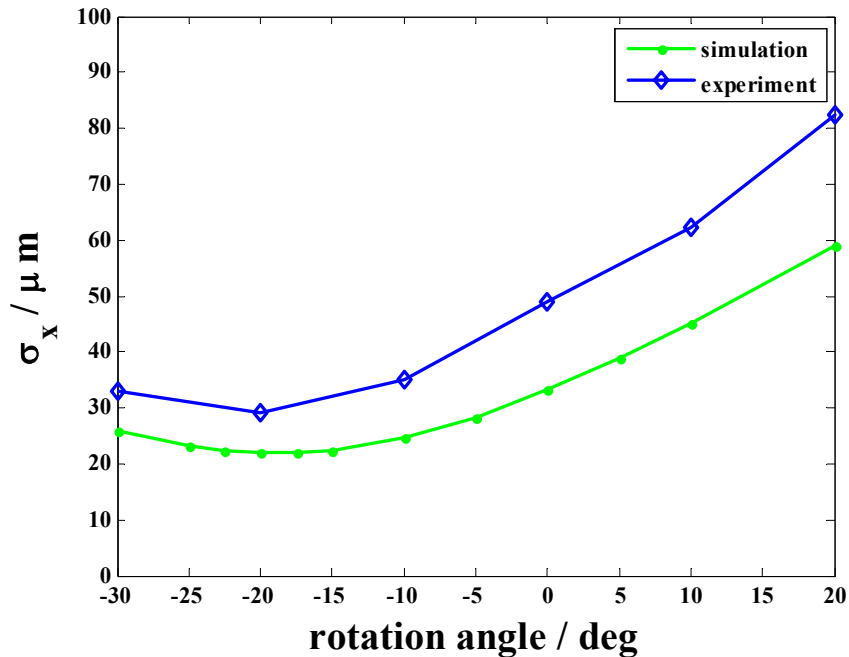


different scale !

➤ 0°



Comparison



- satisfactory agreement between simulation and measurement

 - simulation reproduces observed trend in beam size

- measured beam size systematically larger than simulated one

 - effect of extension radius not included in calculation → increase in PSF

- results summarized in IPAC'10 proceedings: [G. Kube, C. Behrens, W. Lauth, MOPD088](#)

- improve simulation to include effect of energy conversion
 - continue search for optimum scintillator material
 - CRY-19 (Crytur) has promising properties similar to LYSO
 - systematic studies of influence of scintillator thickness
 - influence on observation geometry for different materials and thicknesses
- ⇒ order of new screen materials in preparation

open point

- screen saturation

saturation at high intensities (> 0.04 pC/cm²) observed for YAG:Ce screens

A. Murokh et al., Proc. PAC 2001, 1333

- material properties of interest:
 - band gap
 - scintillation decay time