



Beam Dynamics and FEL Simulations for FLASH

Igor Zagorodnov and Martin Dohlus

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Beam Dynamics Meeting, DESY

FLASH I parameters

FLASH I layout is considered. But the results are equally applicable for FLASH II (SASE).

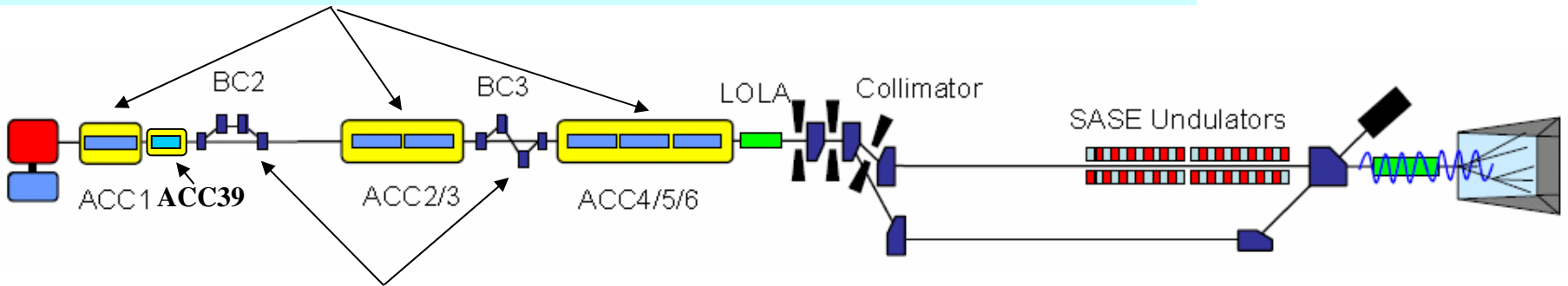
short radiation wavelength

$$\lambda \sim \frac{1}{\gamma^2}$$

high electron energy

In accelerator modules ACC1, ACC2,..., ACC6 the energy of the electrons is increased from 5 MeV (gun) to **1000 MeV** (undulator).

$\lambda \sim 6.5$ nm



In compressors the peak current I is increased from 1.5-50 A (gun) to **2500 A** (undulator).

short gain length

$$L_g \sim \frac{\epsilon^{5/6}}{\sqrt{I}} \left(1 + O(\sigma_E^2) \right) \quad (\text{for the optimal beta function})$$

high peak current

FLASH I parameters

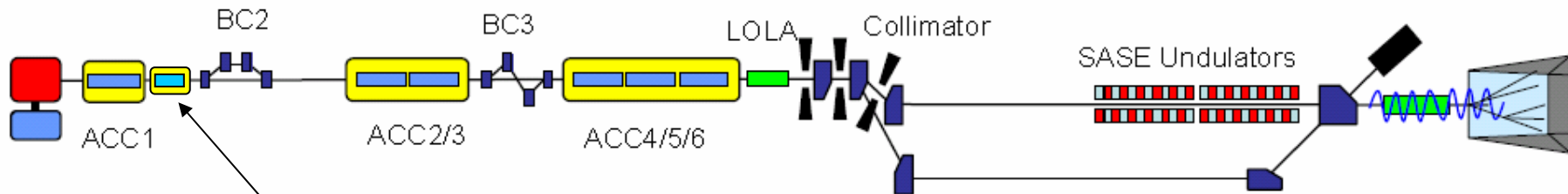
short gain length

$$L_g \sim \frac{\varepsilon^{5/6}}{\sqrt{I}} \left(1 + O(\sigma_E^2)\right) \quad (\text{for the optimal beta function})$$

Annotations:
- $\varepsilon^{5/6}$: small emittance
- \sqrt{I} : high peak current
- $O(\sigma_E^2)$: small energy spread

Electron beam properties for good lasing

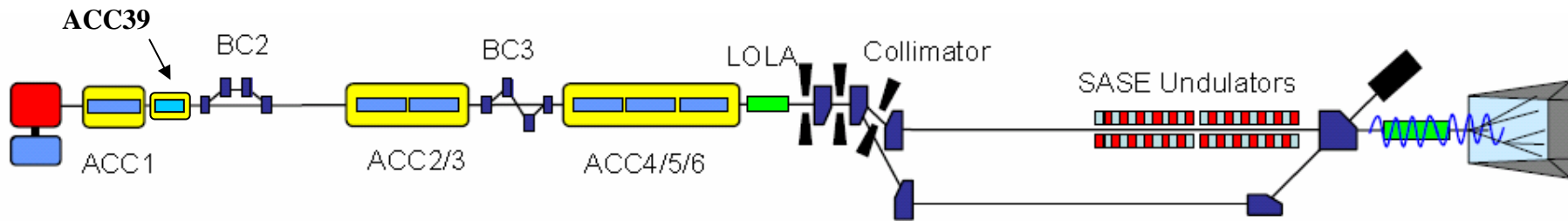
High peak current ~ 2500 A.
Small slice emittance ε (0.4-1 μm).
Small slice energy spread σ_E (< 300 keV).



High harmonic module in 2010

FLASH I parameters

energy 1 GeV
radiation wavelength ~ 6.5 nm



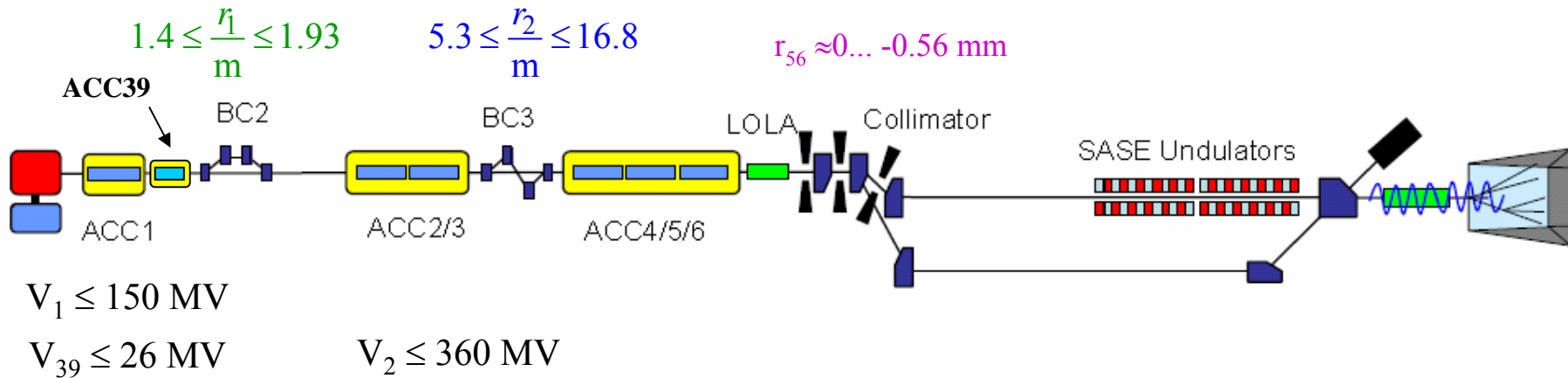
Only **SASE mode** of operation is investigated.

Charge tuning (20-1000 pC) allows to tune

- the radiation **pulse energy** (**30-1400 μ J**),
- the **pulse width FWHM** (**2-70 fs**).

FLASH I parameters

Technical constrains

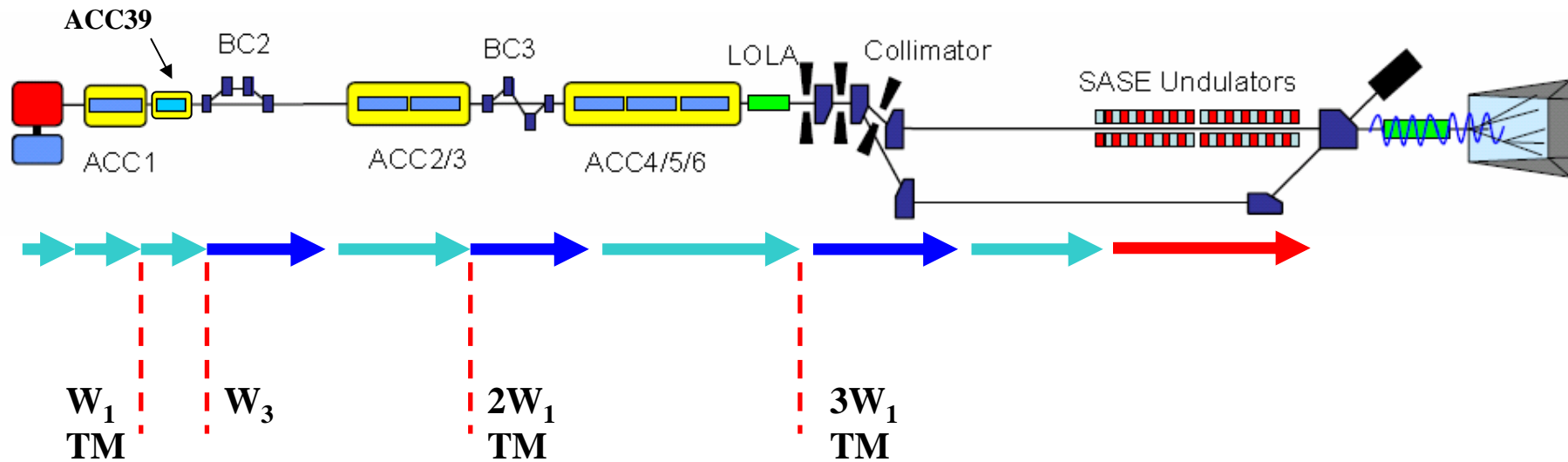


How to provide (1) a well conditioned electron beam and
(2) what are the properties of the radiation?

- (1) Self consistent beam dynamics simulations.
- (2) FEL simulations.


FLASH I

3d simulation method (self-consistent)



 **ASTRA** (tracking with space charge, DESY)

 **CSRtrack** (tracking through dipoles, DESY)

 **ALICE** (3D FEL code, DESY)

W1 -TESLA cryomodule wake (TESLA Report 2003-19, DESY, 2003)

W3 - ACC39 wake (TESLA Report 2004-01, DESY, 2004)

TM - transverse matching to the design optics (V2+, V.Balandin &N.Golubeva)

FLASH I

simulation methods (looking for working points)

1d analytical solution without collective effects
(8 macroparameters -> 6 RF settings)

1d tracking with space charge and wakes

~ **seconds**
(1 cpu)

→	accelerator	$E_1(s_1) = E_0(s_0) + V \cos(ks_0 + \varphi)$ $s_1 = s_0$
→	compressor	$E_1(s_1) = E_0(s_0)$ $s_1(s_0) = s_0 + (r_{56}\delta + t_{566}\delta^2 + u_{5666}\delta^3)$

quasi 3d tracking with all collective effects

~ **30 min**
(1 cpu)

→	accelerator	$E_1(s_1) = E_0(s_0) + V \cos(ks_0 + \varphi)$ $s_1 = s_0$
→	CSRtrack	matrix transport for x & y

3d tracking with all collective effects

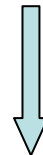
~ **10 h**
(46 cpu-s)

→	Astra
→	CSRtrack

initial guess



~ 5 iterations



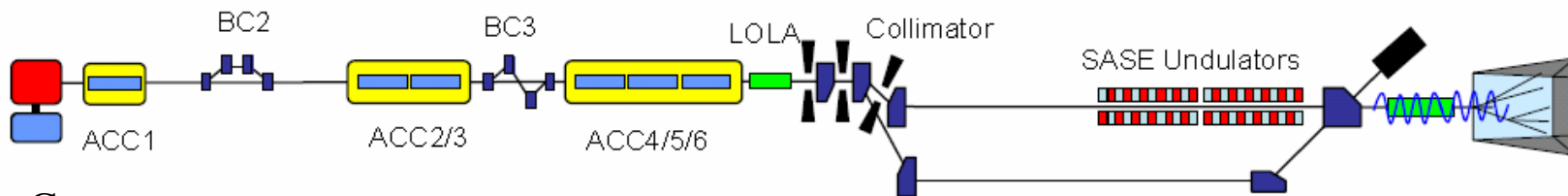
~ 5 iterations



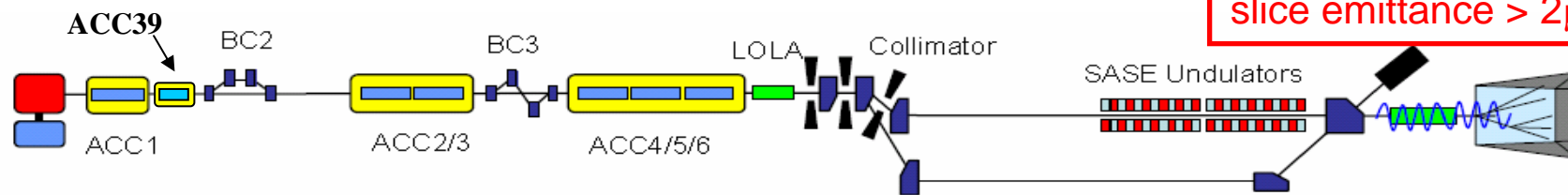
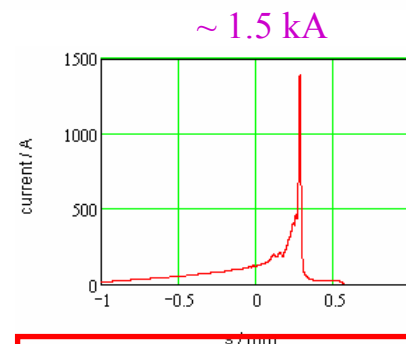
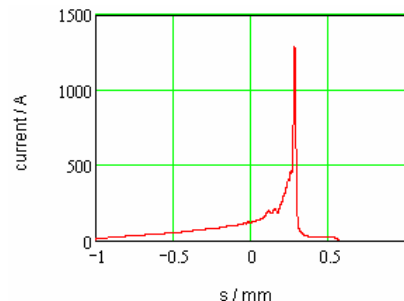
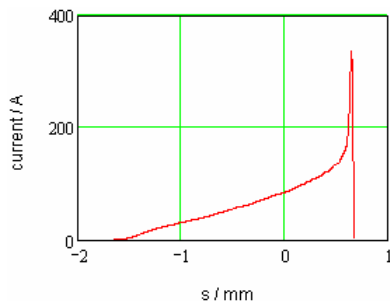
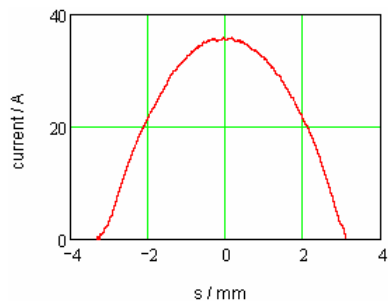
final result

FLASH I before and after upgrade

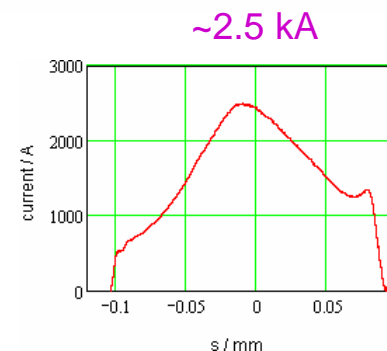
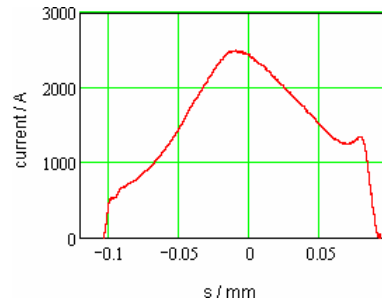
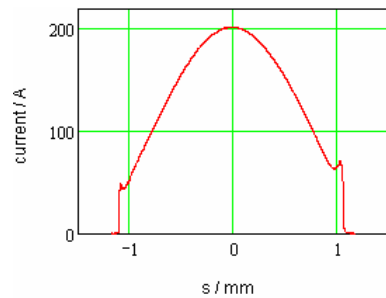
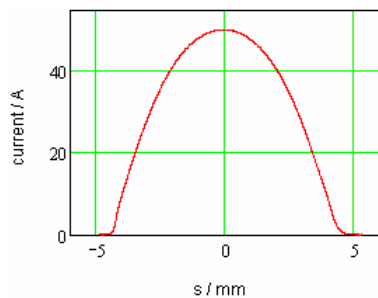
rollover compression vs. linearized compression



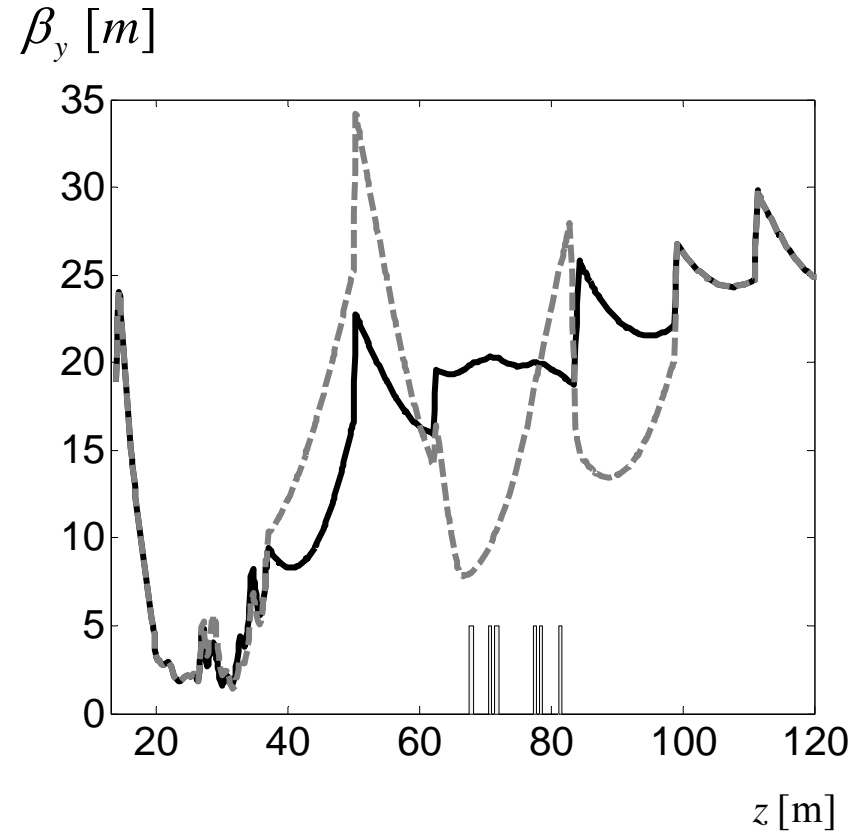
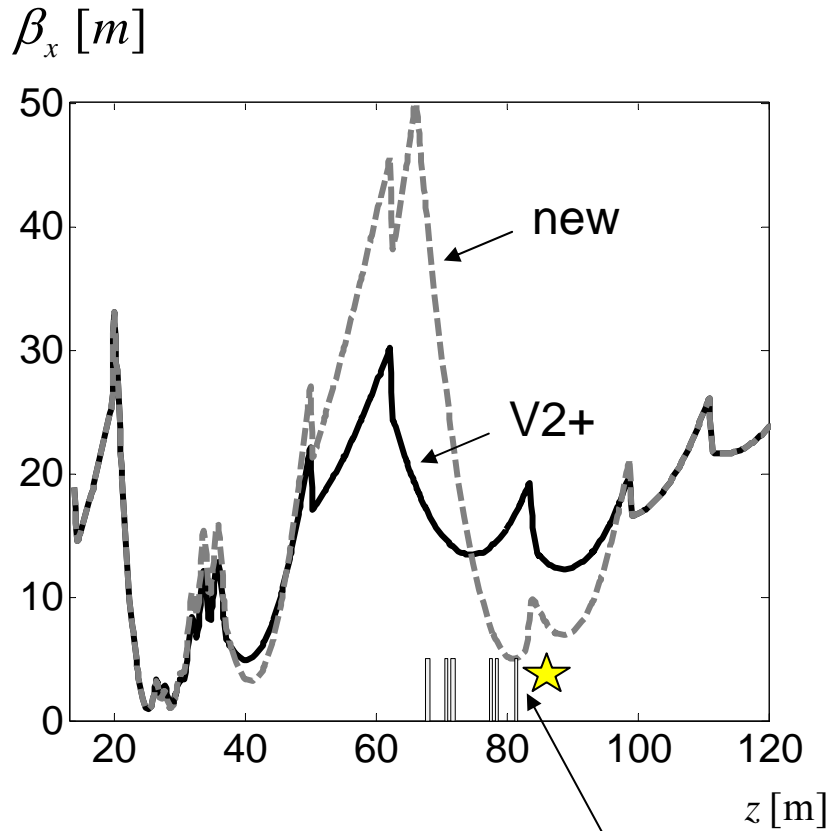
Q=0.5 nC



Q=1 nC



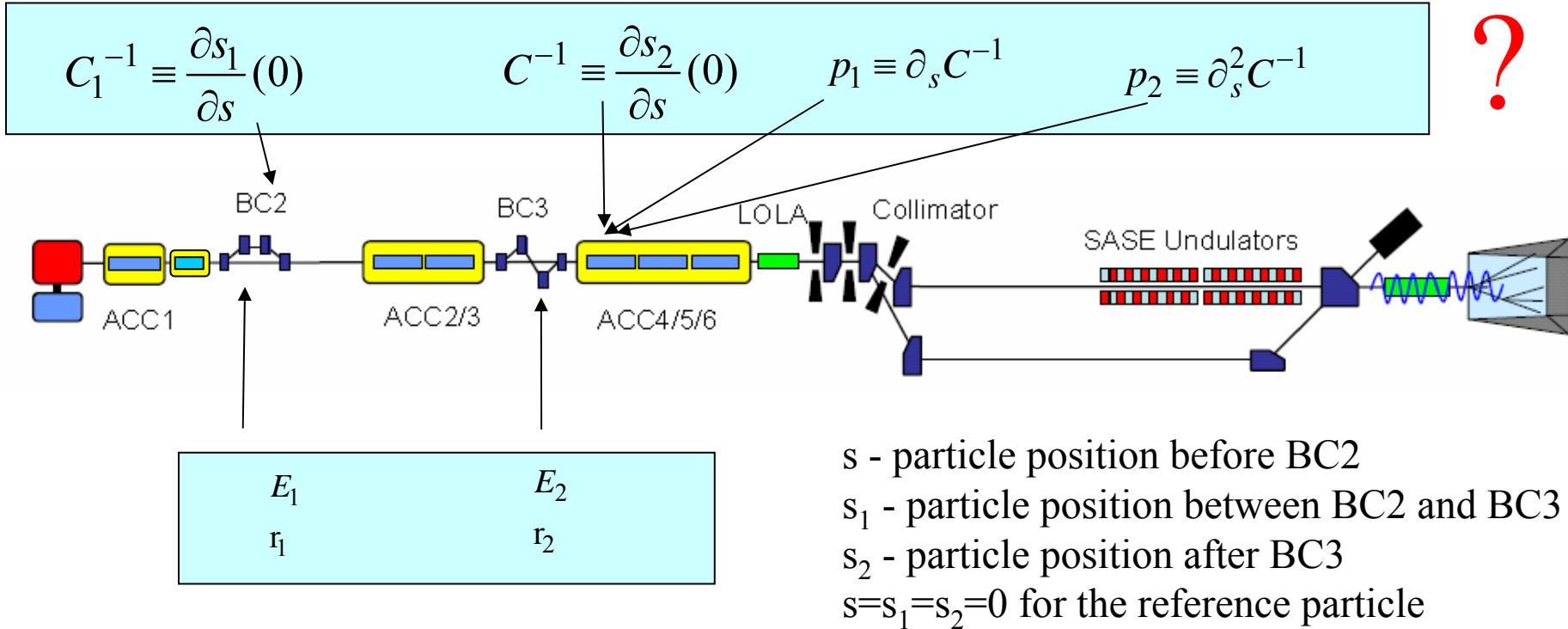
Optics correction



a small transverse bunch size before the last dipole

M.Dohlus, T. Limberg, *Impact of optics on CSR-related emittance growth in bunch compressor chicanes*, PAC 05, 2005

Working points (8 macroparameters)



What is the optimal choice?

Working points (8 macroparameters)

What is the optimal choice?

$$V_1 \leq 150 \text{ MV}$$

5% reserve

$$E_1 = E_0 + 0.95 e V_1 \left(1 - \left(\frac{\omega}{\omega_3} \right)^2 \right) = 5 \text{ MeV} + 0.95 \frac{8}{9} 150 \text{ MeV} \approx 130 \text{ MeV}$$

$$E_1 = 130 \text{ MeV}$$

$$V_2 \leq 360 \text{ MV}$$

10% reserve

$$E_2 = E_1 + e V_2 \cdot 0.9 \approx 450 \text{ MeV}$$

$$E_2 = 450 \text{ MeV}$$

$$E_1 = ?$$

$$E_2 = ?$$

$$r_1 = ?$$

$$r_2 = ?$$

$$C = ?$$

$$C_1 = ?$$

$$\partial_s C^{-1} = ?$$

$$\partial_s^2 C^{-1} = ?$$

Working points (8 macroparameters)

$$1.4 \leq \frac{r_1}{m} \leq 1.93$$

- low compression in BC1 and high compression in BC2
- maximal energy chirp transported through BC1 for the same C_1 (it loses the voltage requirements on RF system ACC2/ACC3)

$$r_1 = 1.93m$$

$$I_0 = 52A$$

$$I_f = 2500A$$

$$C = \frac{I_f}{I_0} = 48$$

$$E_1 = 130MeV$$

$$E_2 = 450MeV$$

$$r_1 = ?$$

$$r_2 = ?$$

$$C = ?$$

$$C_1 = ?$$

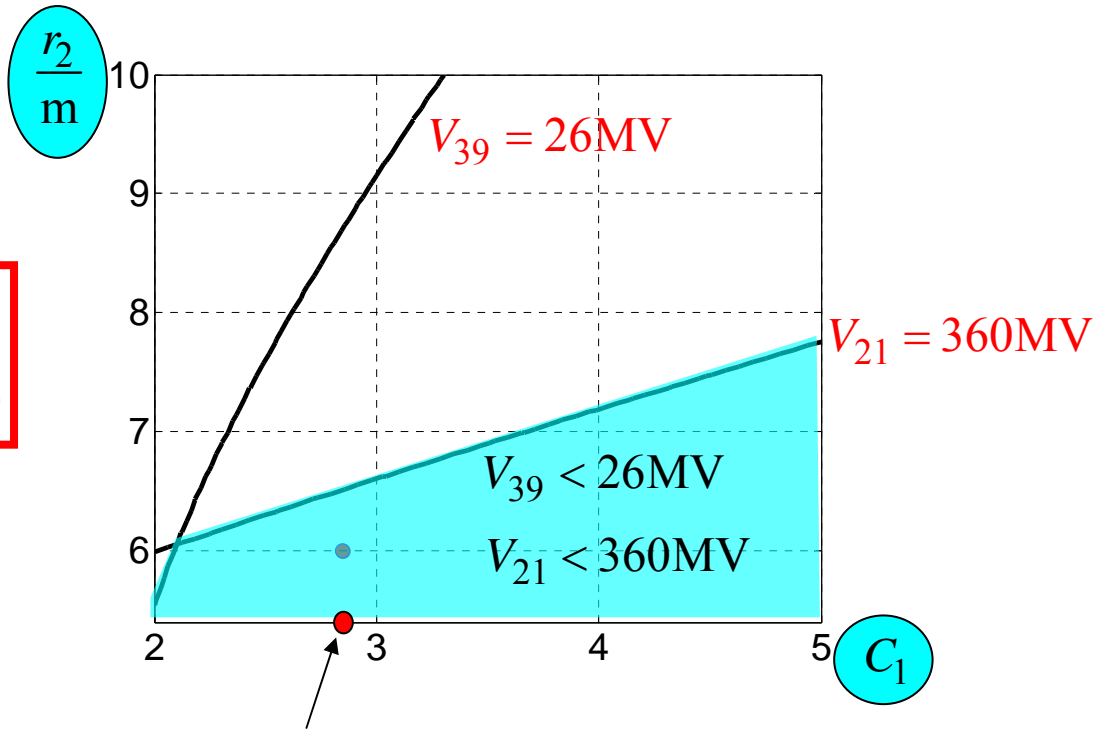
$$\partial_s C^{-1} = ?$$

$$\partial_s^2 C^{-1} = ?$$

Working points (8 macroparameters)

$$p_1 = \partial_s C^{-1} = 0$$

$$p_2 = \partial_s^2 C^{-1} = 0$$



$$C_1 > 2$$

$$C_1 = 2.84$$

$$E_1 = 130\text{MeV}$$

$$E_2 = 450\text{MeV}$$

$$r_1 = 1.93\text{m}$$

$$r_2 = ?$$

$$C = 48$$

$$C_1 = ?$$

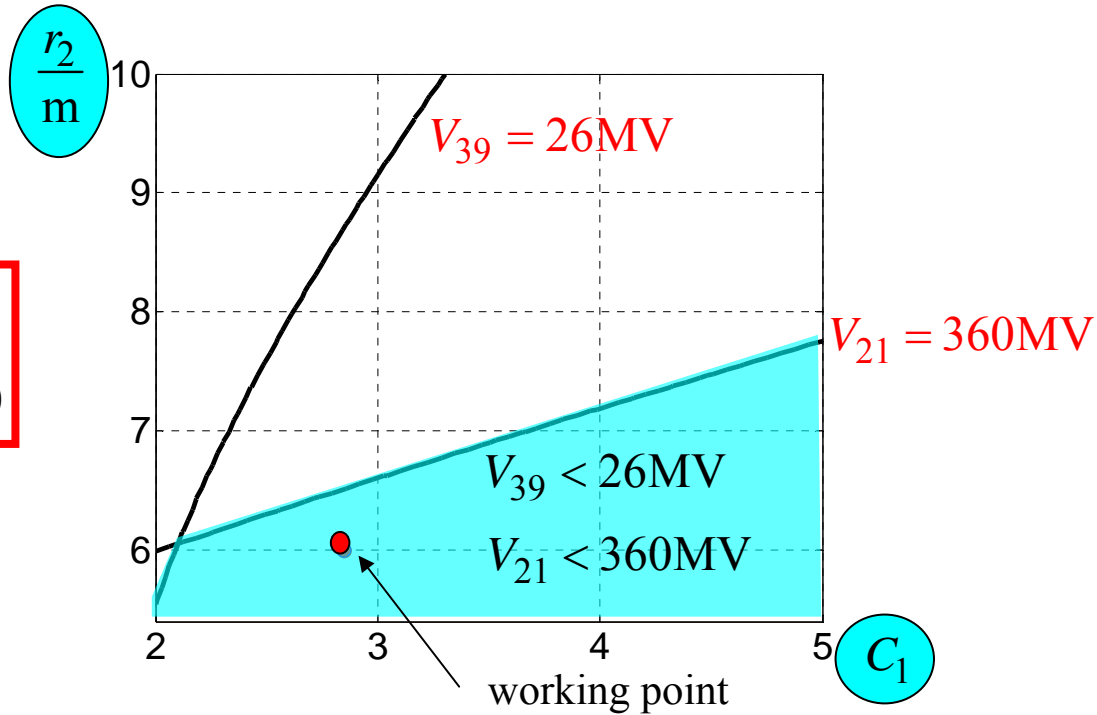
$$\partial_s C^{-1} = ?$$

$$\partial_s^2 C^{-1} = ?$$

Working points (8 macroparameters)

$$p_1 = \partial_s C^{-1} = 0$$

$$p_2 = \partial_s^2 C^{-1} = 0$$



$$E_1 = 130\text{MeV}$$

$$E_2 = 450\text{MeV}$$

$$r_1 = 1.93\text{m}$$

$$r_2 = ?$$

$$C = 48$$

$$C_1 = 2.84$$

$$\partial_s C^{-1} = ?$$

$$\partial_s^2 C^{-1} = ?$$

$$\varphi_2 = \arccos\left(\frac{E_2 - E_1}{\max(V_2) \cdot 0.95}\right) \approx 22^\circ$$

5% reserve

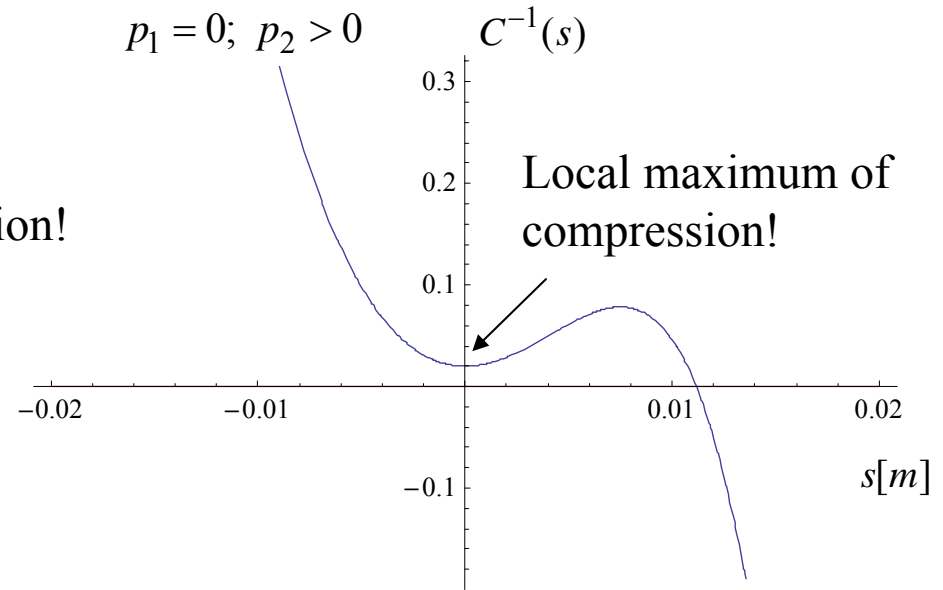
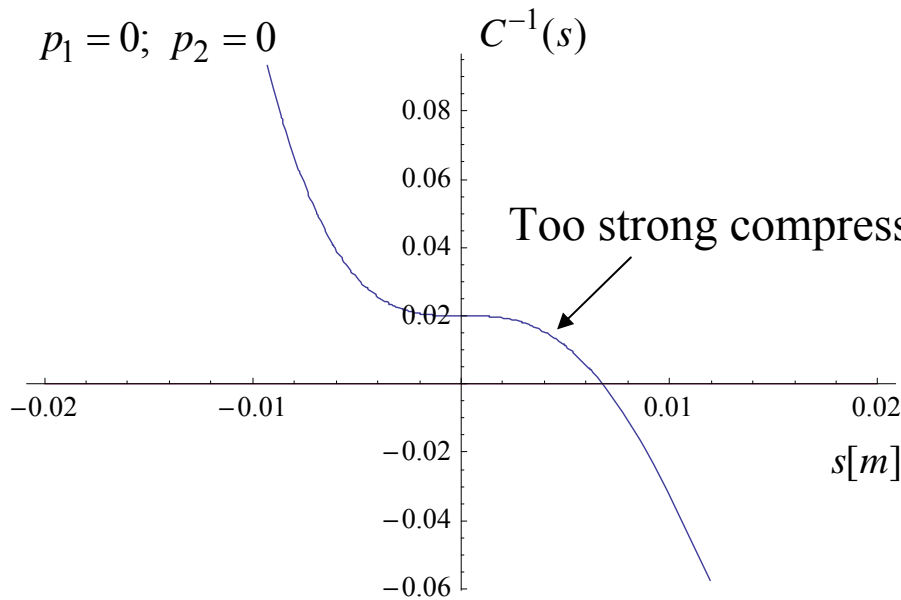
$$r_{562} = \frac{(C_2 - 1)r_{561}}{C_2((C_1 - 1)E_{10}E_{20}^{-1} - g)}$$

$$g = k \frac{V_2}{E_{20}} r_{562} \sin \varphi_2$$

$$r_2 \approx \frac{L_B}{\sin \sqrt{-r_{562} / (3L_B + 4L_D)}}$$

$$r_2 = 6\text{m}$$

Working points (8 macroparameters)



$$p_2 > 0$$

$$E_1 = 130\text{MeV}$$

$$E_2 = 450\text{MeV}$$

$$r_1 = 1.93\text{m}$$

$$r_2 = 6\text{m}$$

$$C = 48$$

$$C_1 = 2.84$$

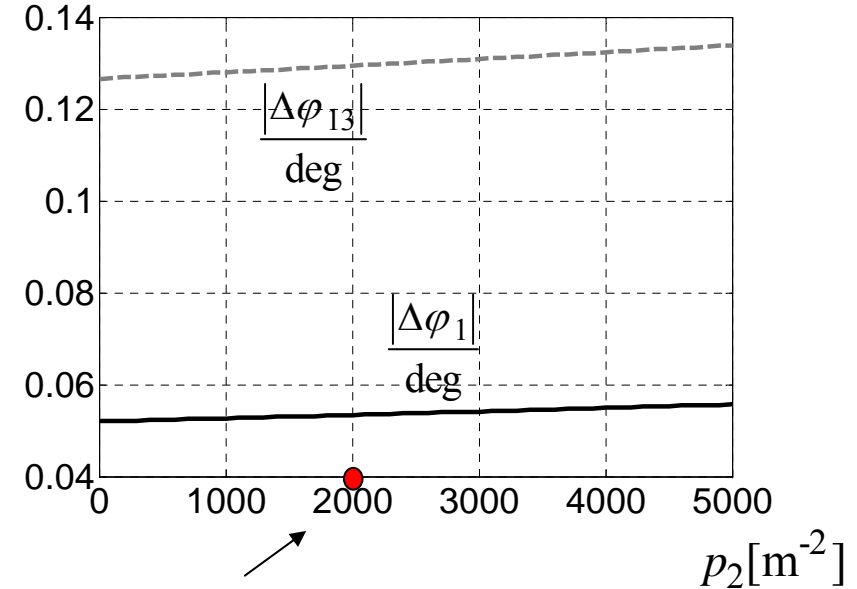
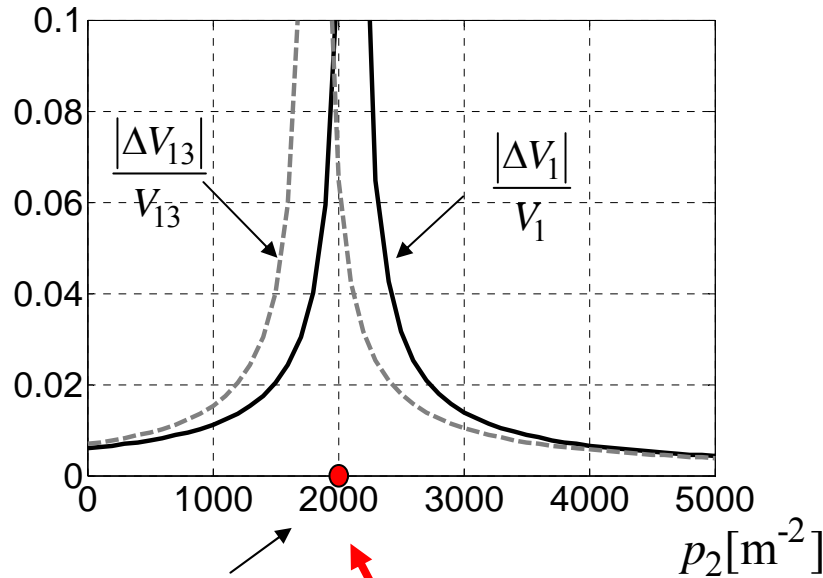
$$\partial_s C^{-1} = ?$$

$$\partial_s^2 C^{-1} = ?$$

Working points (8 macroparameters)

Tolerances (10 % change of compression)

$$p_1 \equiv \partial_s C^{-1} = 0$$



working point

working point

$$\frac{V_{13} \partial C}{C^2 \partial V_{13}} = V_{13} (3Ak \sin(\varphi_{13}) - B \cos(\varphi_{13}))$$

$$\frac{\partial C}{C^2 \partial \varphi_{13}} = V_{13} (B \sin(\varphi_{13}) + 3Ak \cos(\varphi_{13}))$$

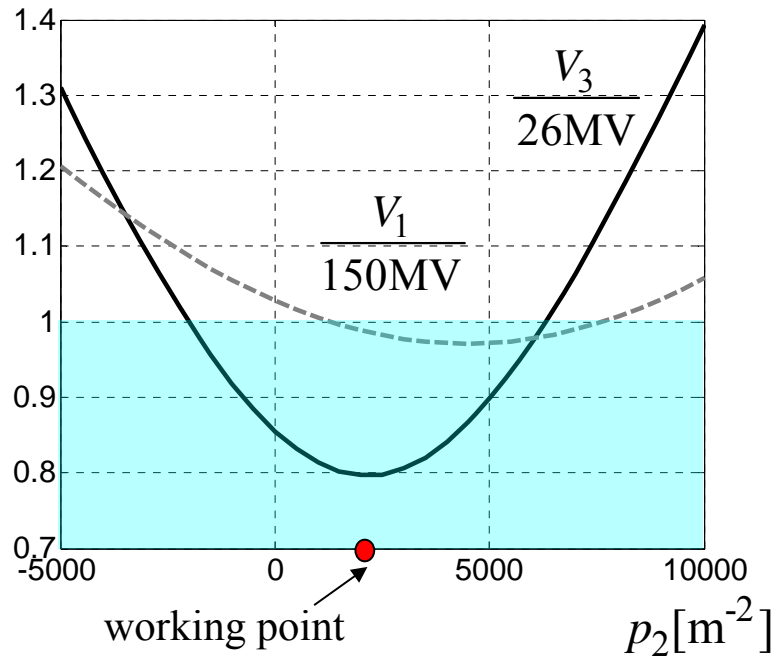
$$\frac{V_1 \partial C}{C^2 \partial V_1} = V_1 (Ak \sin(\varphi_1) - B \cos(\varphi_1))$$

$$\frac{\partial C}{C^2 \partial \varphi_1} = V_1 (B \sin(\varphi_1) + Ak \cos(\varphi_1))$$

$$A = - \left[\frac{r_{561}}{E_1} + \frac{r_{562}}{E_2} + k \frac{r_{561}}{E_1} \frac{r_{562}}{E_2} V_2 \sin(\varphi_2) \right]$$

$$B = \delta_1' \frac{r_{561}}{E_1} + \delta_2' \frac{r_{562}}{E_2} + \delta_1' \frac{r_{561}}{E_1} \frac{r_{562}}{E_2} k V_2 \sin(\varphi_2)$$

Working points (8 macroparameters)



$$E_1 = 130\text{MeV}$$

$$E_2 = 450\text{MeV}$$

$$r_1 = 1.93\text{m}$$

$$r_2 = 6\text{m}$$

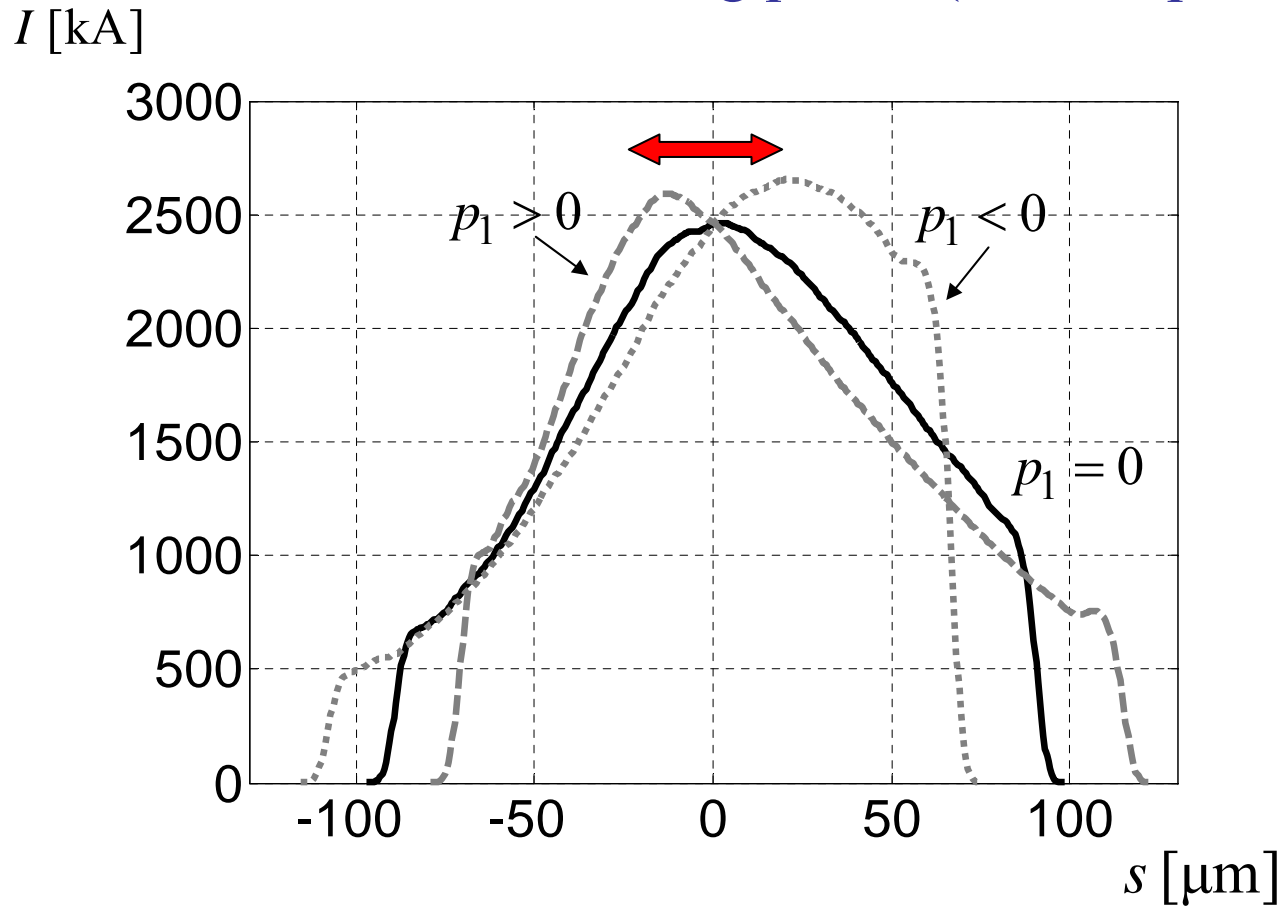
$$C = 48$$

$$C_1 = 2.84$$

$$\partial_s C^{-1} = ?$$

$$\partial_s^2 C^{-1} = 2000\text{m}^{-2}$$

Working points (8 macroparameters)



$E_1 = 130\text{MeV}$
 $E_2 = 450\text{MeV}$
 $r_1 = 1.93\text{m}$
 $C = 48$
 $C_1 = 2.84$
 $r_2 = 6\text{m}$
 $p_2 = 2000\text{m}^{-2}$

$-1 \leq \frac{p_1}{\text{m}^{-1}} \leq 1$ - a free parameter to move the peak

Working points (8 macroparameters)

Charge Q, nC	Energy in BC2 E ₁ , [MeV]	Energy in BC3 E ₂ , [MeV]	Deflecting radius in BC2 r ₁ , [m]	Deflecting radius in BC3 r ₂ , [m]	Compression in BC2 C ₁	Total compression C	First derivative p ₁ , [m ⁻¹]	Second derivative p ₂ , [m ⁻²]
1	130	450	1.93	6	2.84	48	1	2e3
0.5				6.93	4.63	90	1	3.5e3
0.25				7.8	6.57	150	0.7	4e3
0.1				9.3	10.3	240	0	4e3
0.02				15.17	31.8 (12)	1000	-0.5	5e3

C₁ : scaling for different charges

$$x'' + k_x x = \frac{r_e}{ec\gamma^3} \frac{I}{\sigma_x(\sigma_x + \sigma_y)} x \quad \longrightarrow \quad \frac{\max[I_1(Q)]}{\sigma_r^2(Q)} \sim \frac{\max[I_1(Q)]}{\varepsilon(Q)} \sim \frac{\max[I_0(Q)] C_1(Q)}{\sqrt[2]{Q}} \sim const$$

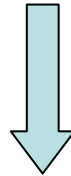
we have used another scaling

$$\frac{\max[I_0(Q)] C_1(Q)}{\sqrt[4]{Q}} \sim const$$

Working points (6 equations \Rightarrow 6 RF parameters)

8 macroparameters define 6 equations \longrightarrow

$$\begin{cases} E_2(0) = E_{20}, & E_1(0) = E_{10} & \frac{\partial s_1}{\partial s}(0) = C_1^{-1}, \\ \frac{\partial s_2}{\partial s}(0) = C^{-1}, & \frac{\partial^2 s_2}{\partial s^2}(0) = p_1, & \frac{\partial^3 s_2}{\partial s^3}(0) = p_2. \end{cases}$$



Analytical solution without self-fields*

$$\mathbf{A}_0(\mathbf{x}_0) = \mathbf{f}_0 \quad \mathbf{x}_0 = \mathbf{A}_0^{-1}(\mathbf{f}_0)$$

\swarrow nonlinear operator
(defined analytically)

*M.Dohlus and I.Zagorodnov,
A semi analytical modelling of two-stage
bunch compression with collective effects, (in preparation)

$$\mathbf{x}_0 = \begin{pmatrix} V_1 \\ \varphi_1 \\ V_{13} \\ \varphi_{13} \\ V_2 \\ \varphi_2 \end{pmatrix} \quad \mathbf{f}_0 = \begin{pmatrix} E_{10} \\ E_{20} \\ C_1 \\ C \\ p_1 \\ p_2 \end{pmatrix}$$

Analytical solution without self-fields

$$\mathbf{x}_0 = \mathbf{A}_0^{-1}(\mathbf{f}_0)$$

Solution with self-fields

$$\mathbf{A}(\mathbf{x}) = \mathbf{f}_0$$

nonlinear operator
(tracking with self-fields)

$$\mathbf{x} = \mathbf{A}_0^{-1}(\mathbf{A}_0(\mathbf{x}) + \mathbf{f}_0 - \mathbf{A}(\mathbf{x}))$$

$$\mathbf{x}_n = \mathbf{A}_0^{-1}(\mathbf{A}_0(\mathbf{x}_{n-1}) + \mathbf{f}_0 - \mathbf{A}(\mathbf{x}_{n-1}))$$

numerical tracking

$$\mathbf{f}_{n-1} = \mathbf{A}(\mathbf{x}_{n-1})$$

$$\Delta \mathbf{f}_{n-1} = \mathbf{f}_0 - \mathbf{f}_{n-1}$$

$$\mathbf{g}_n = \mathbf{g}_{n-1} + \Delta \mathbf{f}_{n-1}$$

$$\mathbf{x}_n = \mathbf{A}_0^{-1}(\mathbf{g}_n)$$

residual in
macroscopic
parameters

analytical correction
of RF parameters

FLASH I

simulation methods (looking for working points)

1d analytical solution without collective effects
(8 macroparameters -> 6 RF settings)

1d tracking with space charge and wakes

~ **seconds**
(1 cpu)

→ accelerator	$E_1(s_1) = E_0(s_0) + V \cos(k s_0 + \varphi)$ $s_1 = s_0$
→ compressor	$E_1(s_1) = E_0(s_0)$ $s_1(s_0) = s_0 + (r_{566} \delta + t_{566} \delta^2 + u_{566} \delta^3)$

quasi 3d tracking with all collective effects

~ **30 min**
(1 cpu)

→ accelerator	$E_1(s_1) = E_0(s_0) + V \cos(k s_0 + \varphi)$ $s_1 = s_0$
→ CSRtrack	matrix transport for x & y

3d tracking with all collective effects

~ **10 h**
(46 cpu-s)

→ Astra
→ CSRtrack

$$\mathbf{x}_0 = \mathbf{A}_0^{-1}(\mathbf{f}_0)$$

$$\mathbf{A}_1(\mathbf{x}_1) = \mathbf{f}_0$$

$$\mathbf{x}_0 = \mathbf{x}_1$$

$$\mathbf{A}_2(\mathbf{x}_2) = \mathbf{f}_0$$

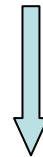
$$\mathbf{A}(\mathbf{x}_2) \rightarrow \mathbf{f}$$

$$\mathbf{f} \approx \mathbf{f}_0$$

initial guess



~ 5 iterations



~ 5 iterations



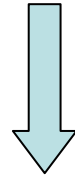
final result

Working points (6 equations => 6 RF parameters)

8 macroparameters
define 6 equations



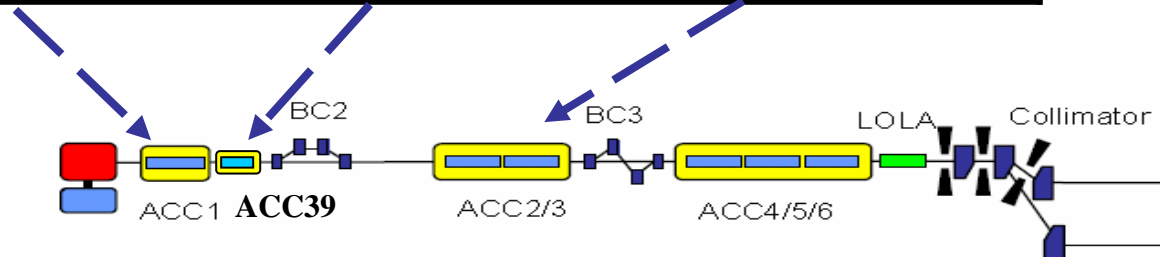
$$\left\{ \begin{array}{l} E_2(0) = E_{20}, \quad E_1(0) = E_{10} \quad \frac{\partial s_1}{\partial s}(0) = C_1^{-1}, \\ \frac{\partial s_2}{\partial s}(0) = C^{-1}, \quad \frac{\partial^2 s_2}{\partial s^2}(0) = p_1, \quad \frac{\partial^3 s_2}{\partial s^3}(0) = p_2. \end{array} \right.$$



**Analytical solution without self-fields
+ iterative procedure with them**

RF settings in accelerating modules

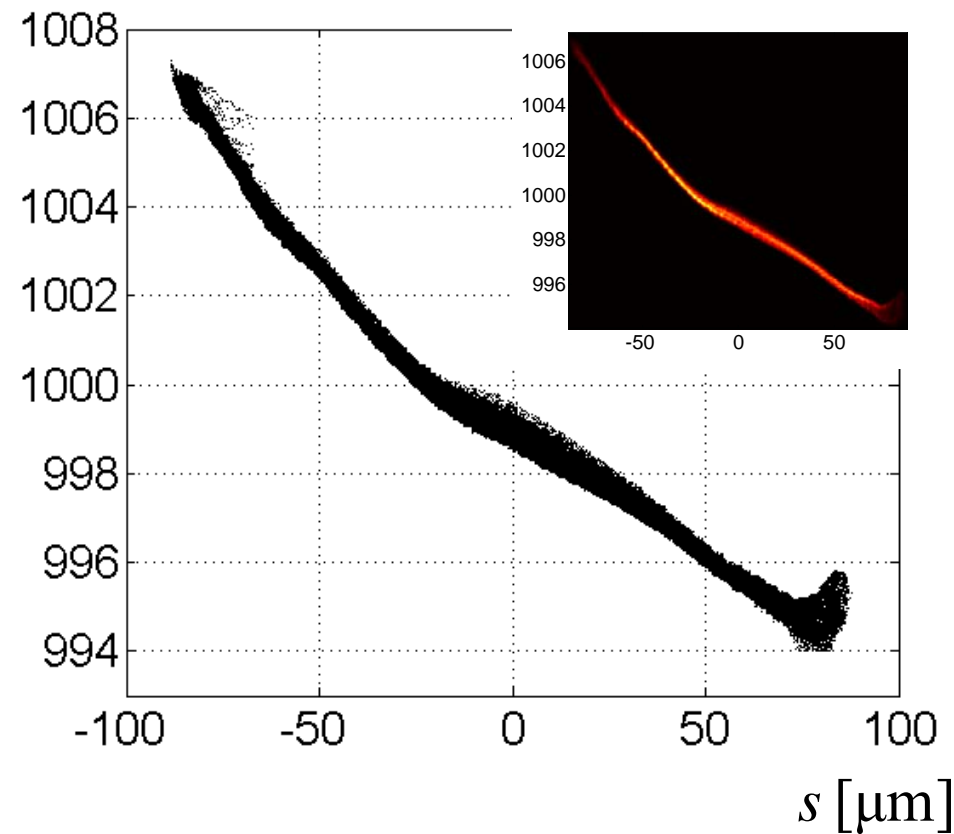
Charge, nC	V_1 , [MV]	ϕ_1 , [deg]	V_{39} , [MV]	ϕ_{39} , [deg]	V_2 , [MV]	ϕ_2 , [deg]
1	144	-4.66	22.6	145	350	23.4
0.5	143.7	4.042	19.65	158.4	351	23.65
0.25	143.36	2.493	20.81	153.9	352.6	23.96
0.1	144.8	-6.31	25.6	137.5	356.5	25.62
0.02	144.9	-3.894	25.58	141.65	339.8	19.385



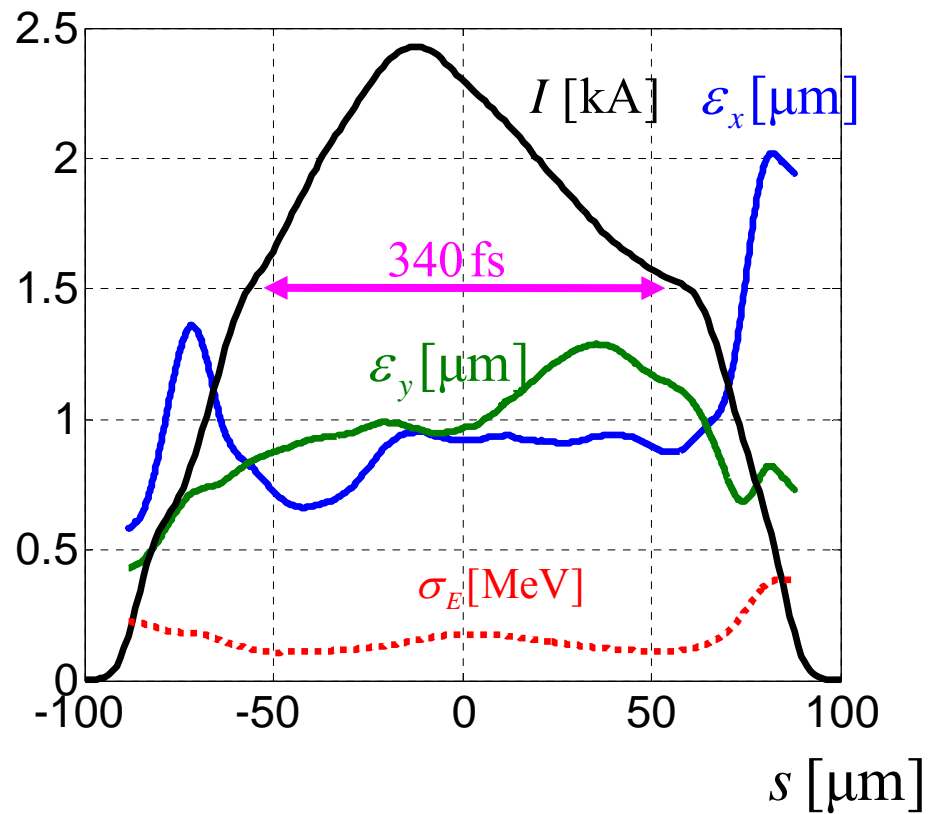
$Q=1$ nC

E [MeV]

Phase space



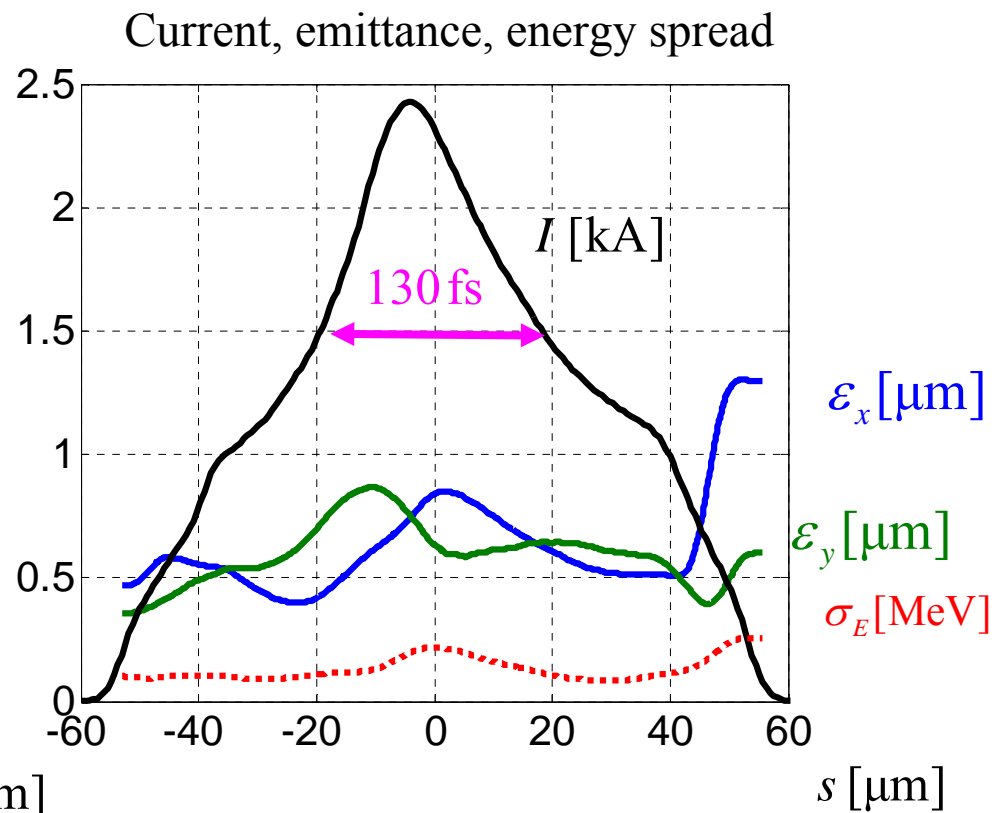
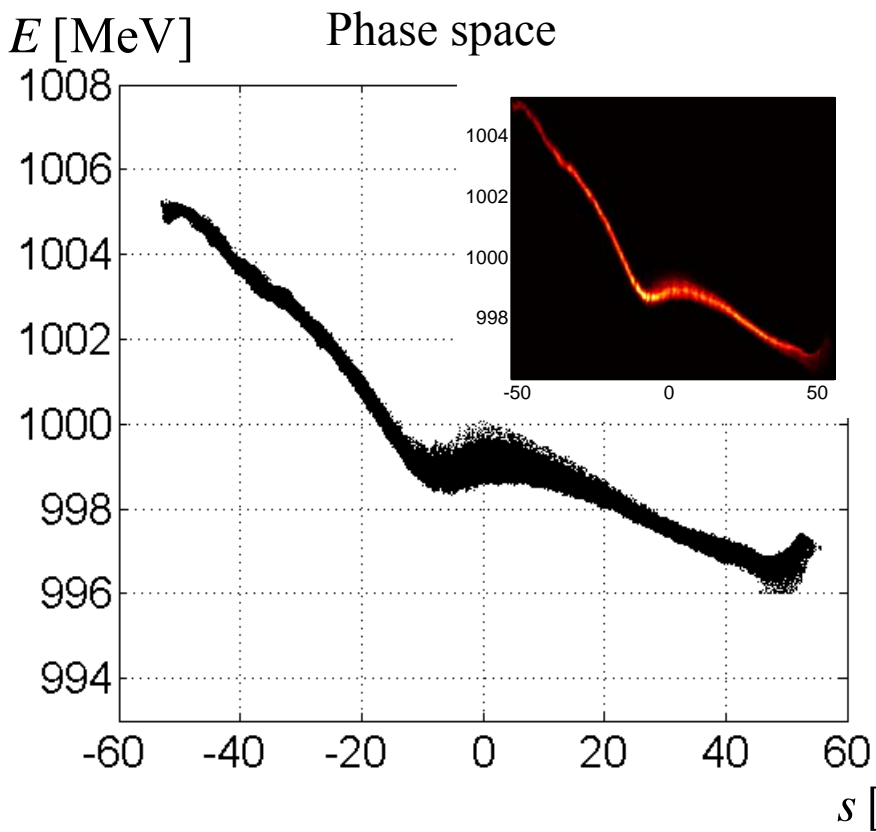
Current, emittance, energy spread



$$\epsilon_x^{proj} = 3 [\mu\text{m}]$$

$$\epsilon_y^{proj} = 1.4 [\mu\text{m}]$$

$Q=0.5$ nC



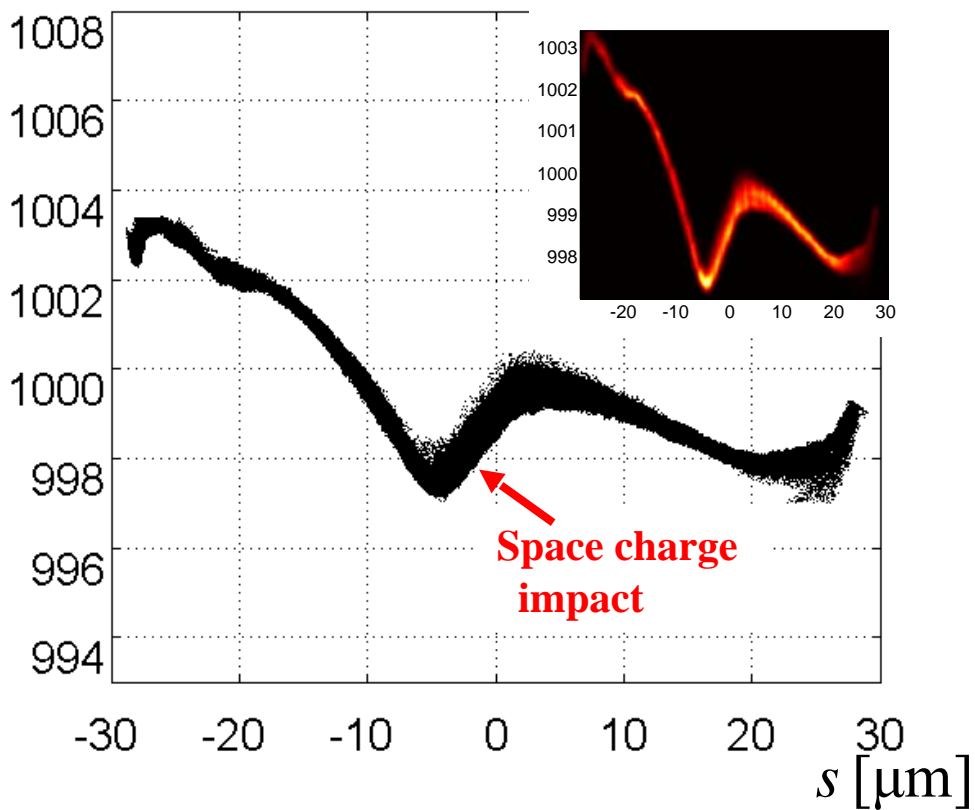
$$\epsilon_x^{proj} = 2.5 \text{ } [\mu\text{m}]$$

$$\epsilon_y^{proj} = 0.84 \text{ } [\mu\text{m}]$$

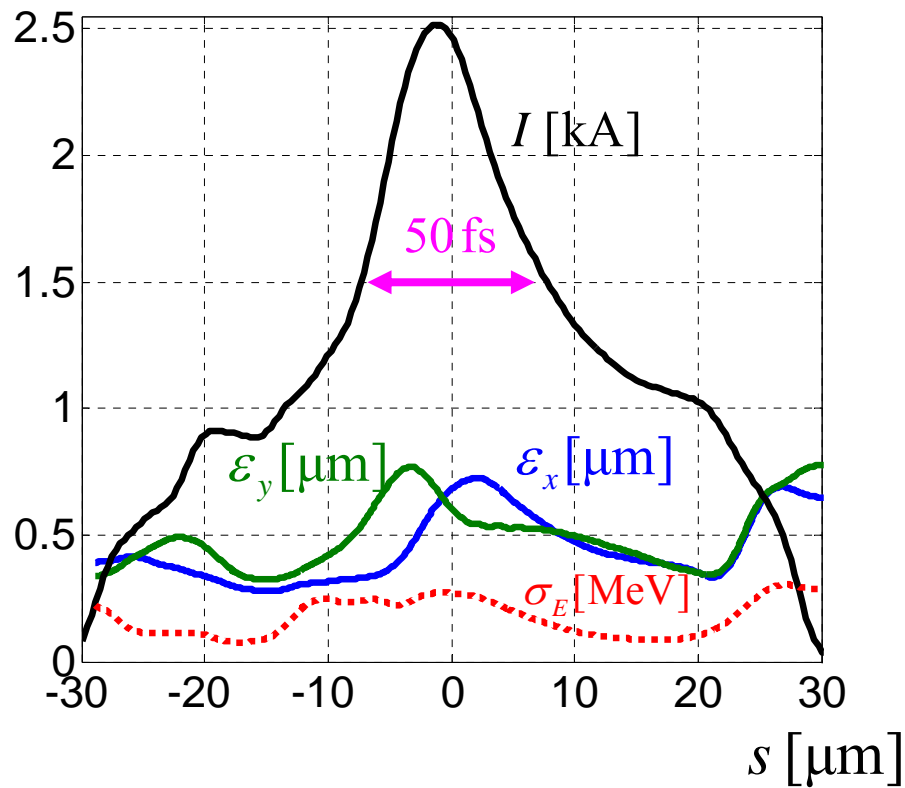
$Q=0.25$ nC

E [MeV]

Phase space



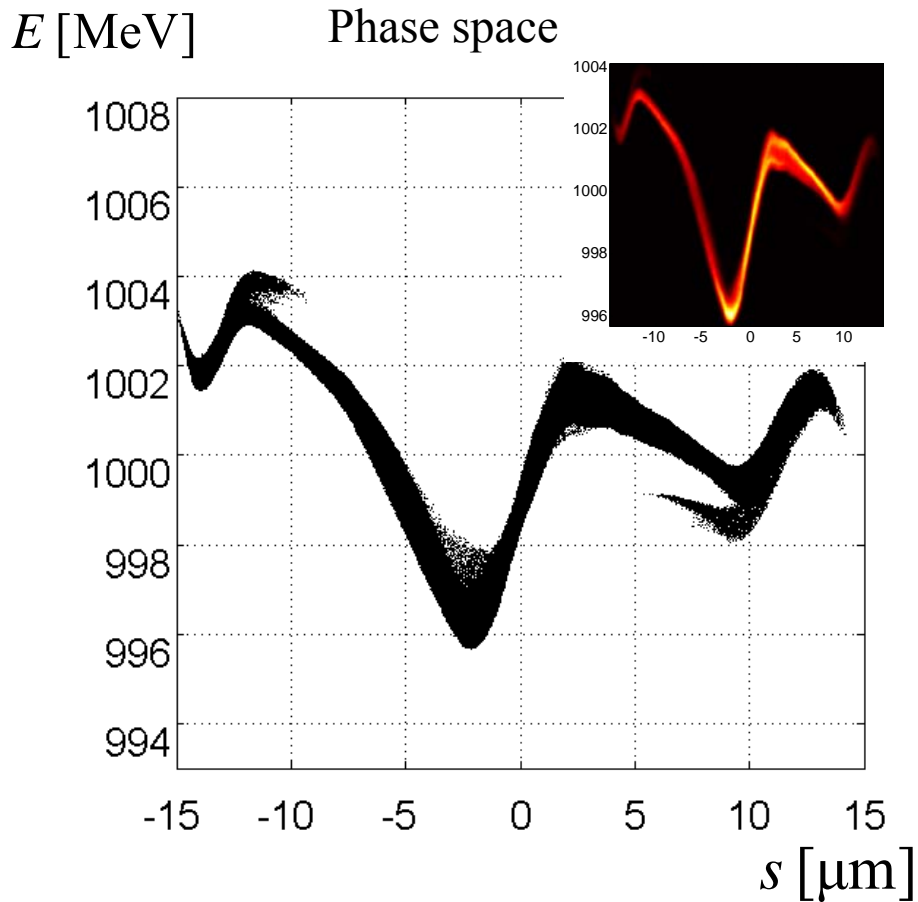
Current, emittance, energy spread



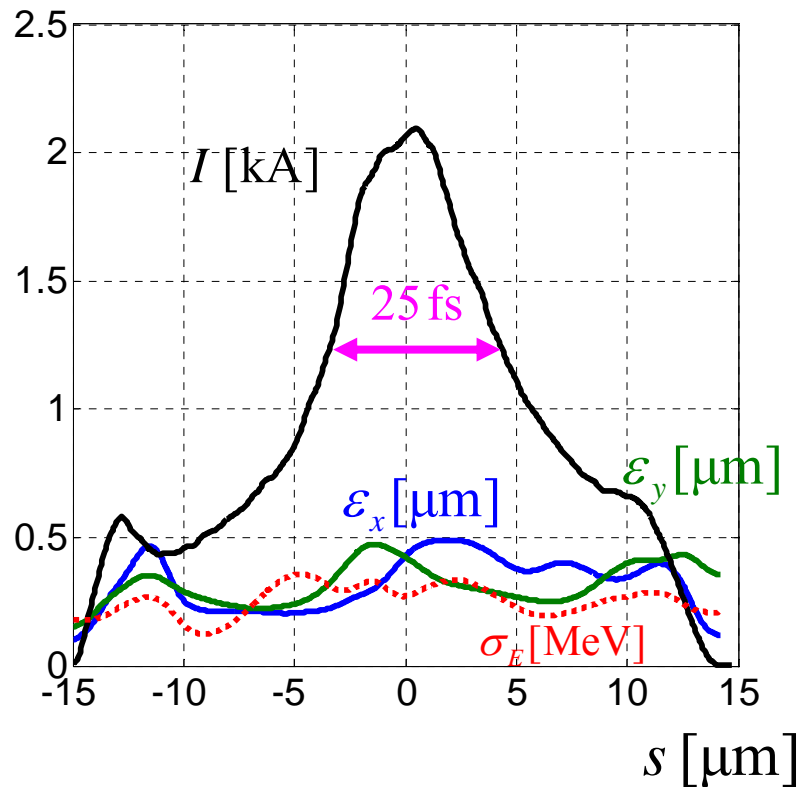
$$\epsilon_x^{proj} = 1.14 [\mu\text{m}]$$

$$\epsilon_y^{proj} = 0.74 [\mu\text{m}]$$

$Q=0.1$ nC



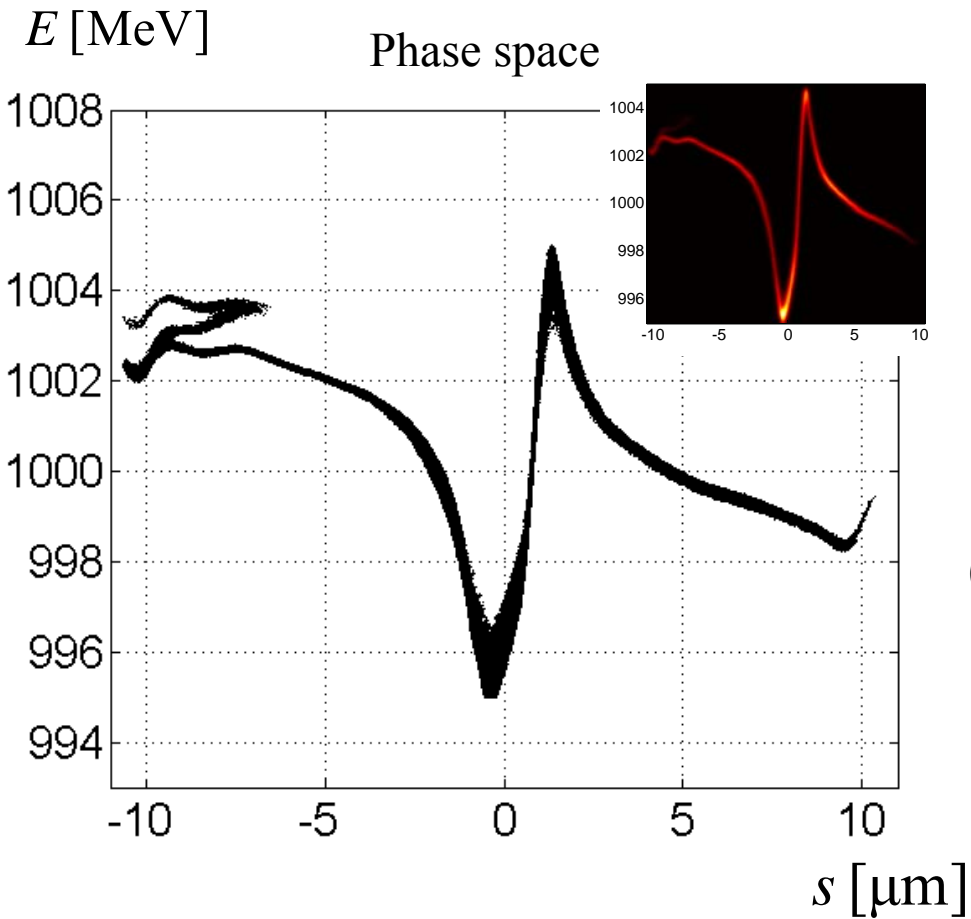
Current, emittance, energy spread



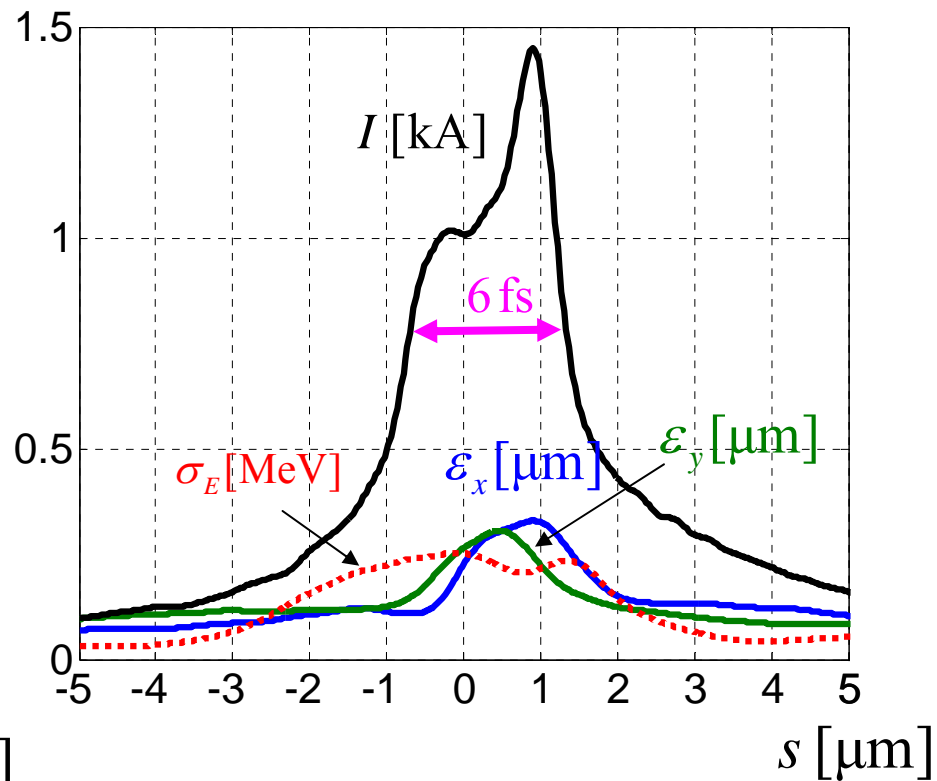
$$\epsilon_x^{proj} = 2 \text{ } [\mu\text{m}]$$

$$\epsilon_y^{proj} = 0.6 \text{ } [\mu\text{m}]$$

$Q=0.02$ nC



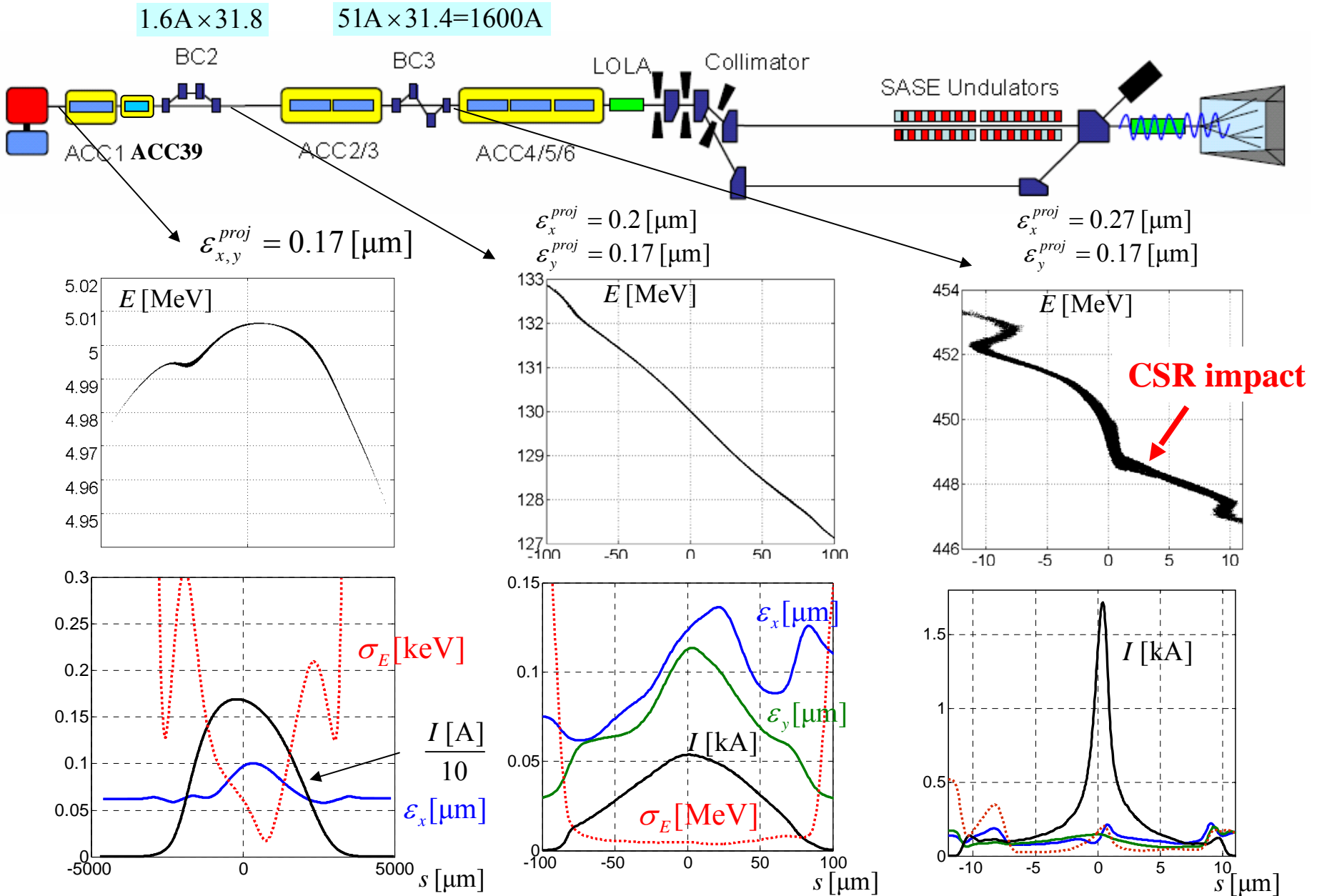
Current, emittance, energy spread



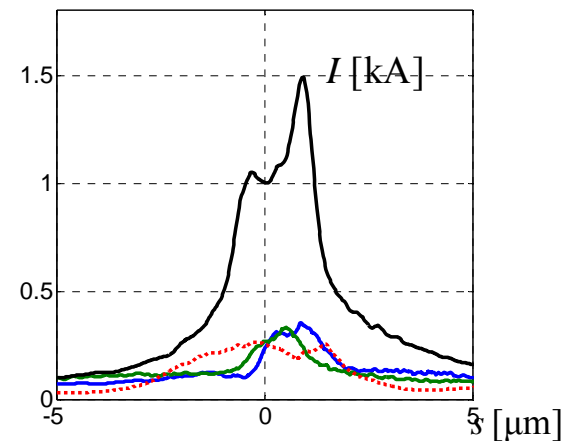
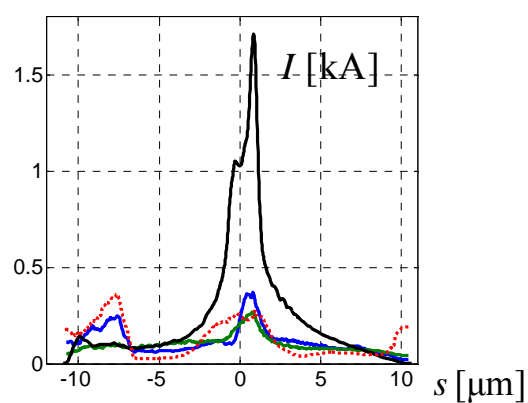
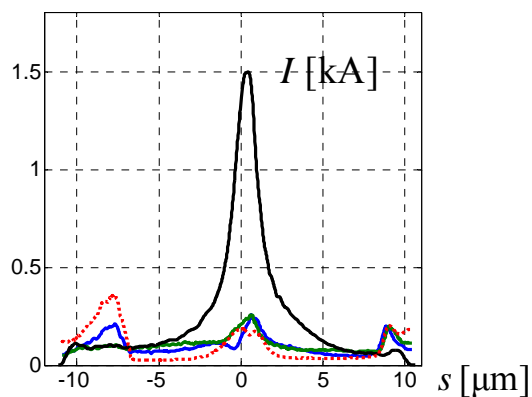
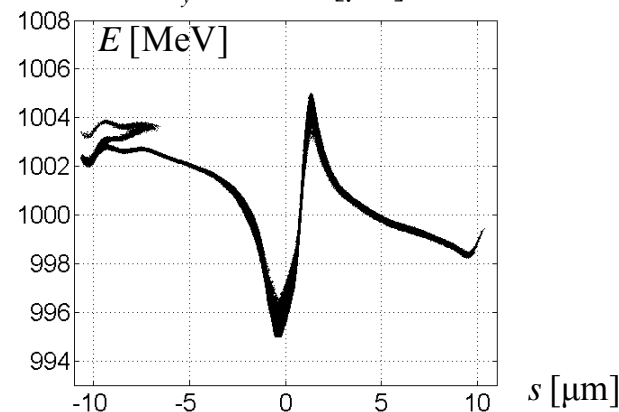
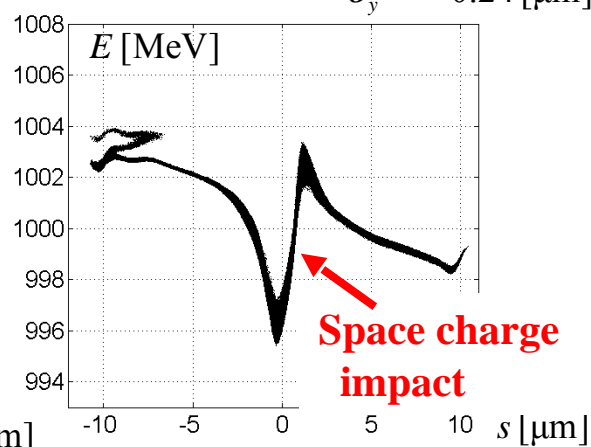
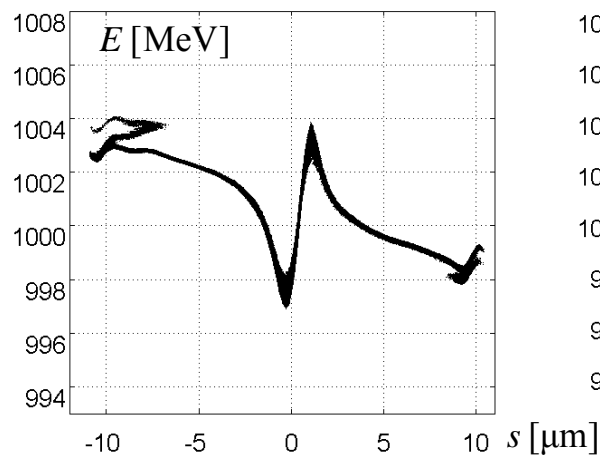
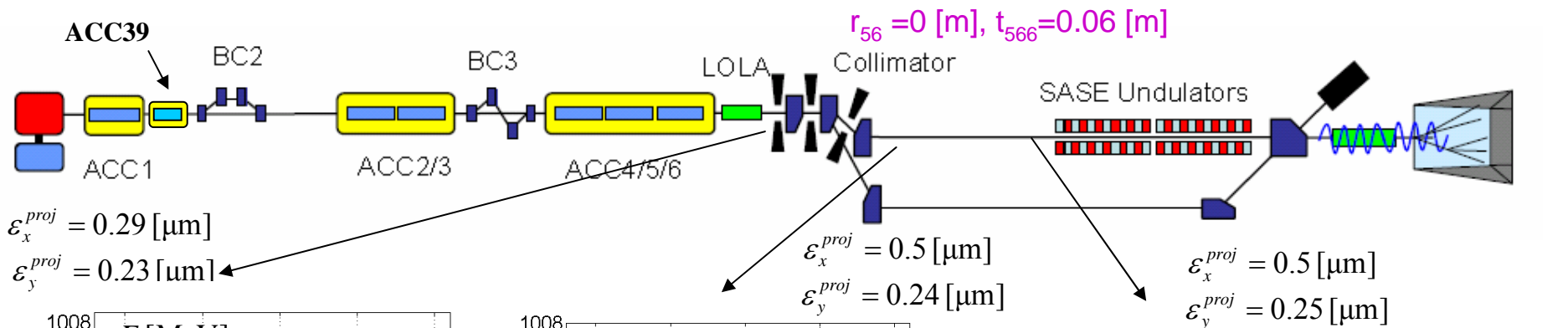
$$\epsilon_x^{proj} = 0.48 [\mu\text{m}]$$

$$\epsilon_y^{proj} = 0.25 [\mu\text{m}]$$

$Q=0.02$ nC



$Q=0.02$ nC



Tolerances (analytically) **without self fields** (10 % change of compression)

Q, nC			1	0.5	0.25	0.1	0.02
ACC1	$ \Delta V /V$	Scaling $\sim O(C^{-1})$	0.34	0.013	0.006	0.0014	0.0002
	$ \Delta\phi $, degree		0.05	0.024	0.013	0.008	0.0016
ACC39	$ \Delta V /V$		0.05	0.007	0.0035	0.0011	0.0002
	$ \Delta\phi $, degree		0.13	0.061	0.033	0.019	0.004
ACC2/3	$ \Delta V /V$		0.09	0.023	0.014	0.01	0.0054
	$ \Delta\phi $, degree		$\sim O(C_2^{-1})$	0.19	0.21	0.22	0.28

Tolerances (from tracking) **with self fields** (10 % change of compression)

Q, nC			1	0.5	0.25	0.1	0.02
ACC1	$ \Delta V /V$	0.0041	0.0035	0.0015	0.0004	0.0001	
	$ \Delta\phi $, degree	0.063	0.026	0.015	0.009	0.0019	
ACC39	$ \Delta V /V$	0.0037	0.0027	0.0011	0.0004	0.0001	
	$ \Delta\phi $, degree	0.16	0.07	0.04	0.024	0.005	
ACC2/3	$ \Delta V /V$	0.24	0.026	0.015	0.01	0.0054	
	$ \Delta\phi $, degree	0.18	0.2	0.2	0.26	0.35	

FLASH

parameters

How to provide (1) a well conditioned electron beam and (2) what are the properties of the radiation?

(1) Self consistent beam dynamics simulations.

We are able to provide the well conditioned electron beam for different charges.

But RF tolerances for small charges are tough.

(2) FEL simulations (next slides).

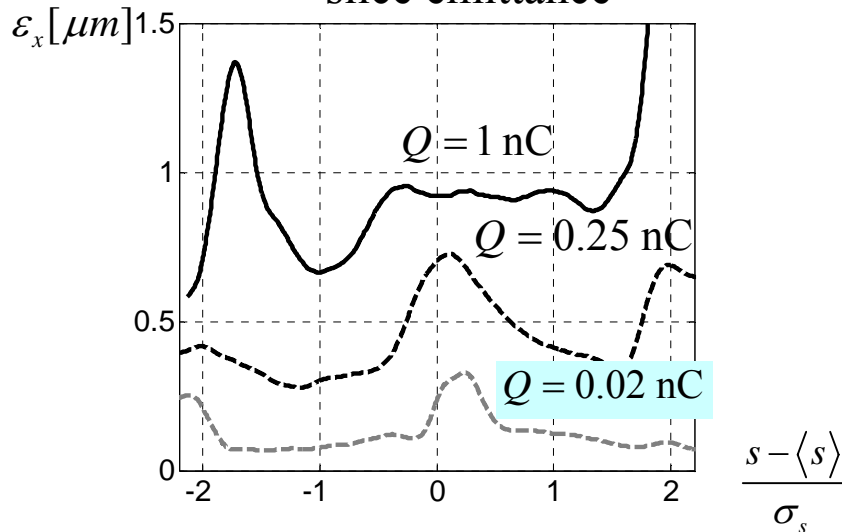
Slice parameters for SASE simulations

Slice parameters are extracted from S2E simulations for SASE simulations

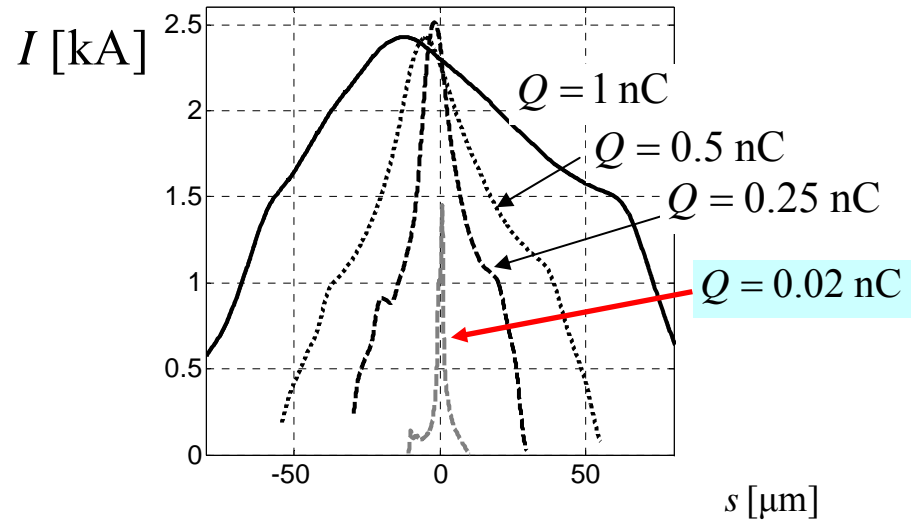
γ $\Delta\gamma$ ε_x ε_y β_x β_y $\langle x \rangle$ $\langle y \rangle$ $\langle x' \rangle$ $\langle y' \rangle$ α_x α_y I



slice emittance



current

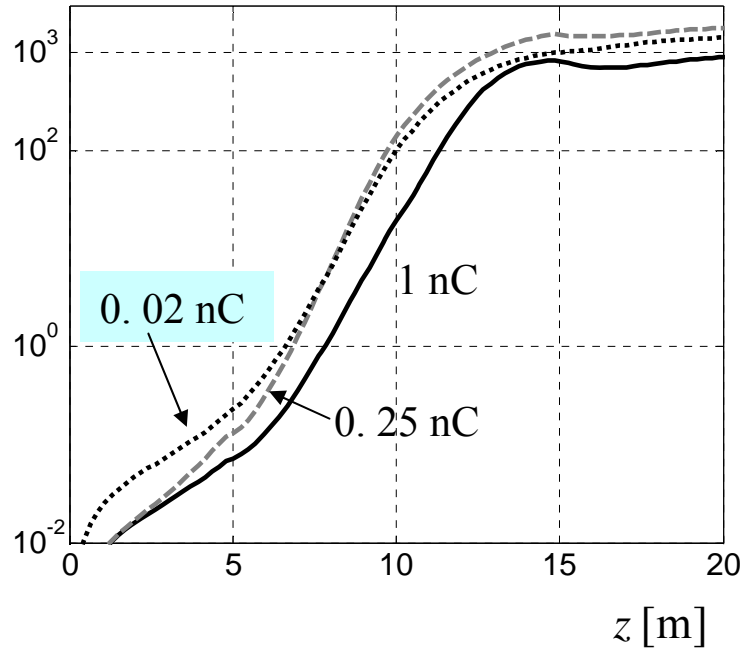


Charge Q , nC	1	0.25	0.02
Longitudinal electron beam size σ_s , μm	42	13	3.6
Transverse electron beam size σ_r , μm	80	68	36

Radiation energy statistics (200-500 runs)

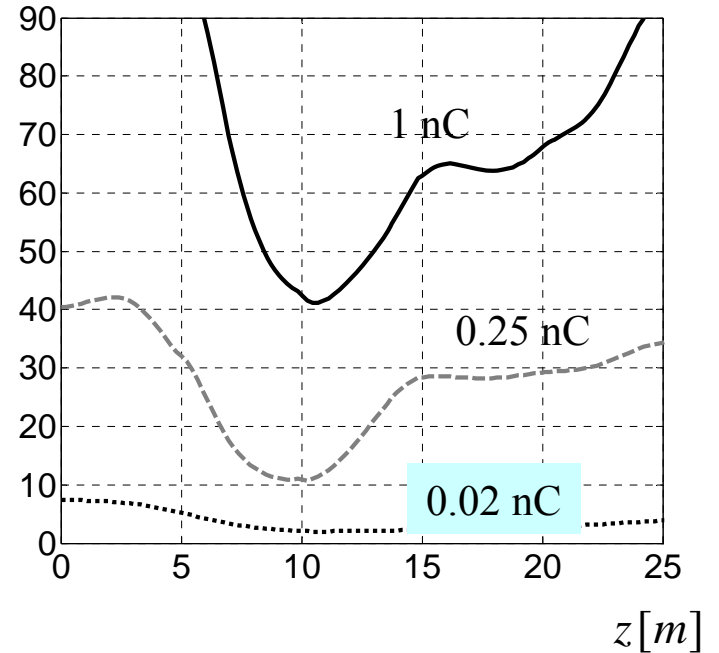
$$\frac{\langle E \rangle}{Q} \left[\frac{\mu\text{J}}{\text{nC}} \right]$$

Mean energy



$$\frac{\sigma_z}{\text{fs}}$$

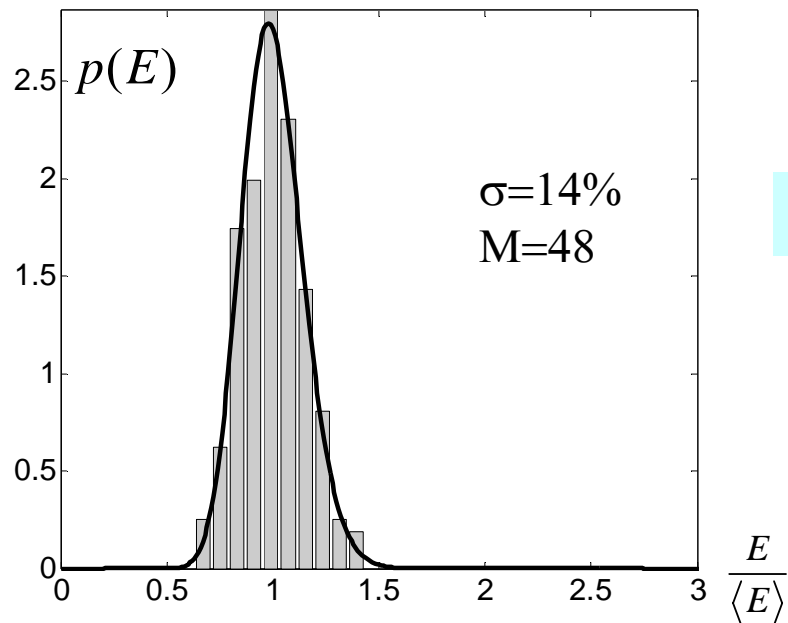
Radiation pulse width (RMS)



Charge, nC	1	0.5	0.25	0.1	0.02
Mean radiation energy, μJ	1000-1400	700	500	200	30
Pulse radiation width (FWHM), fs	70	30	17	7	2

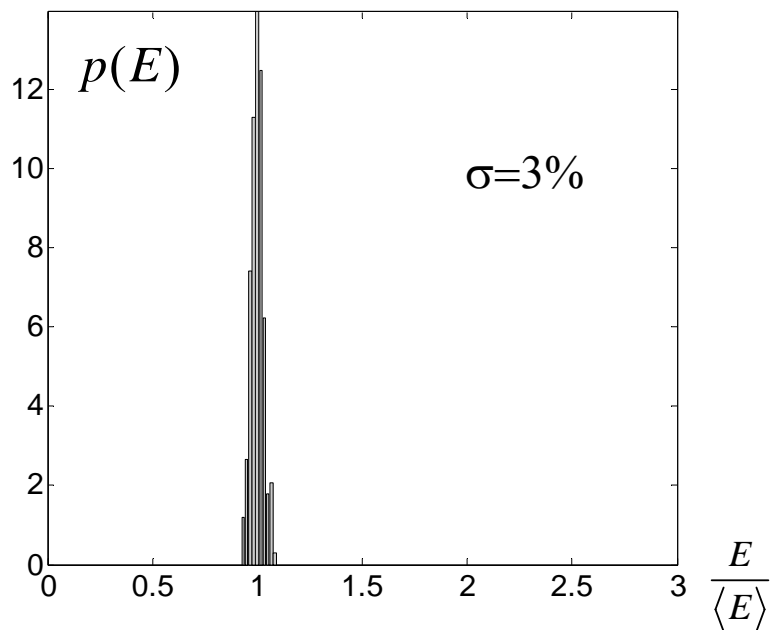
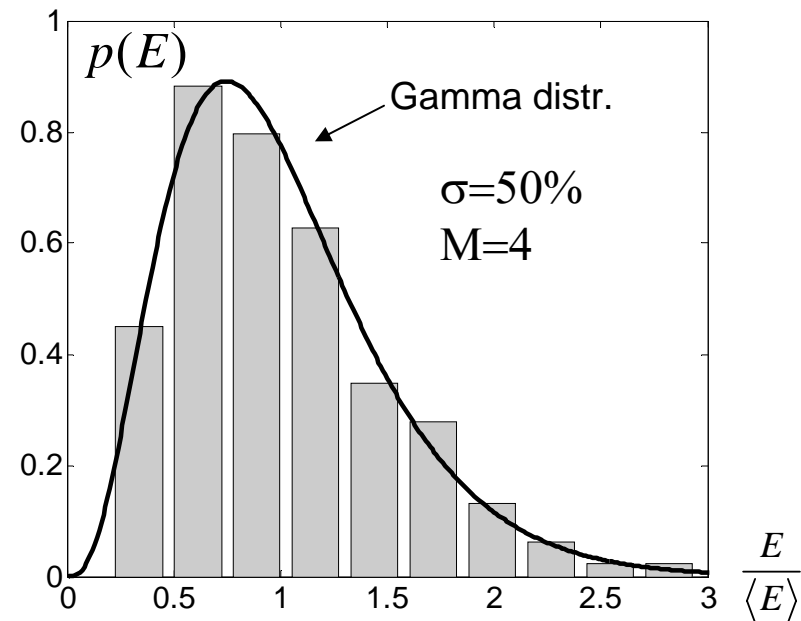
Radiation energy statistics

$Q=1$ nC

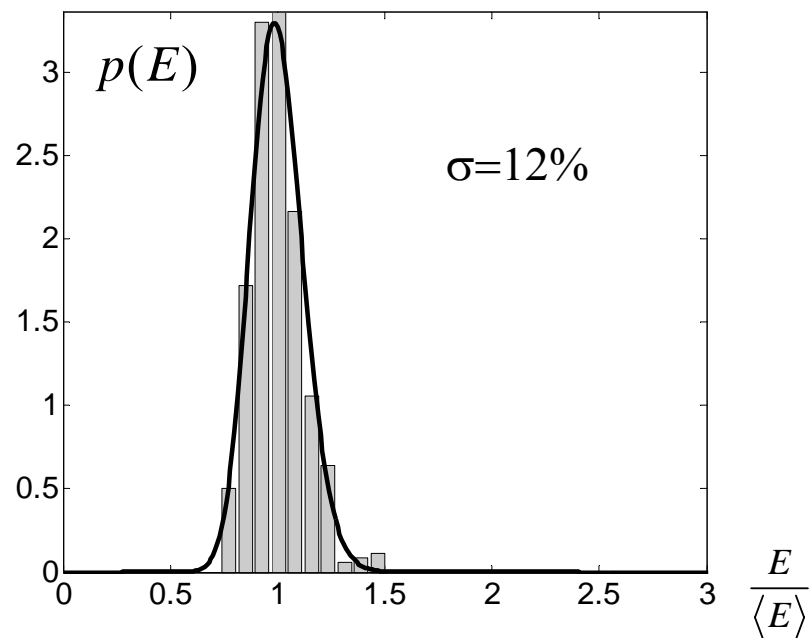


$z=10$ m

$Q=0.02$ nC



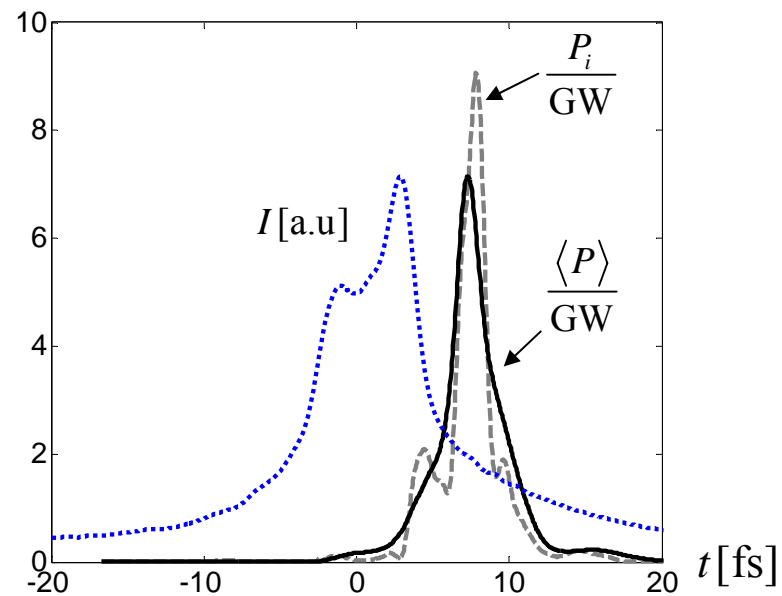
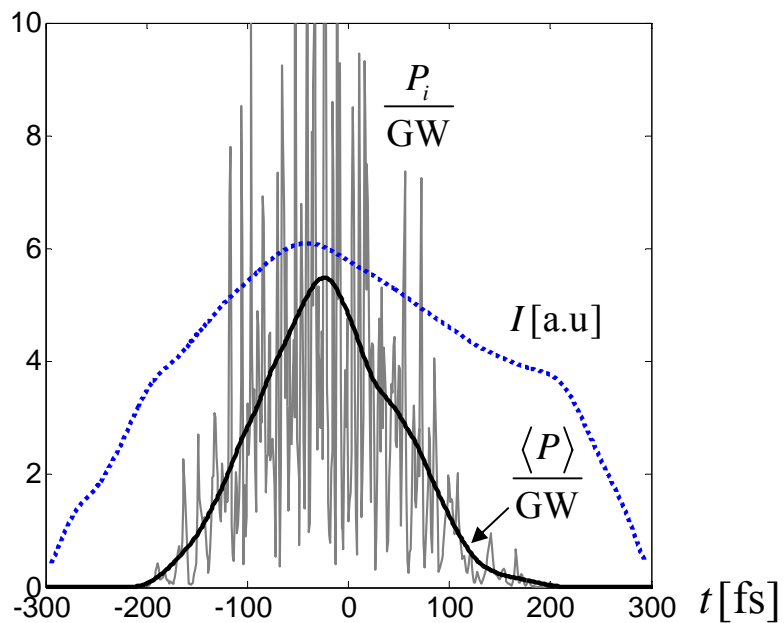
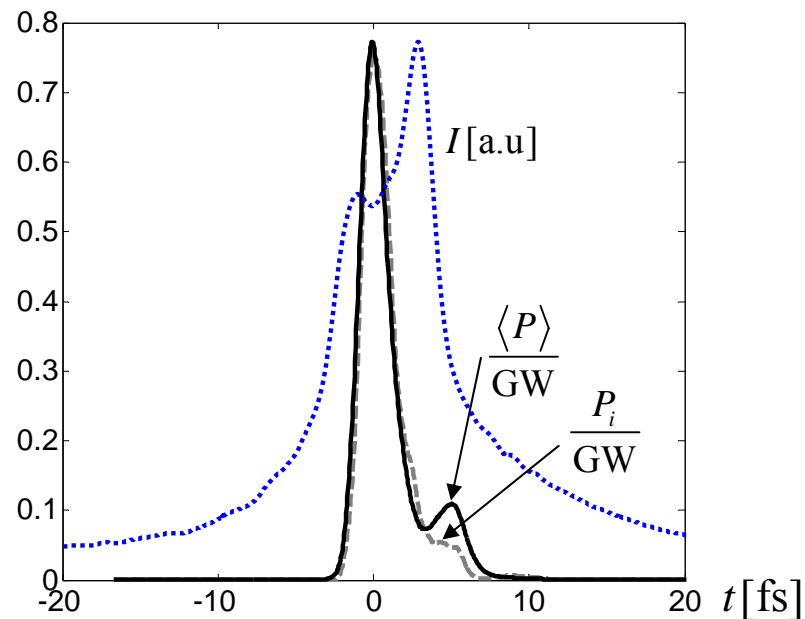
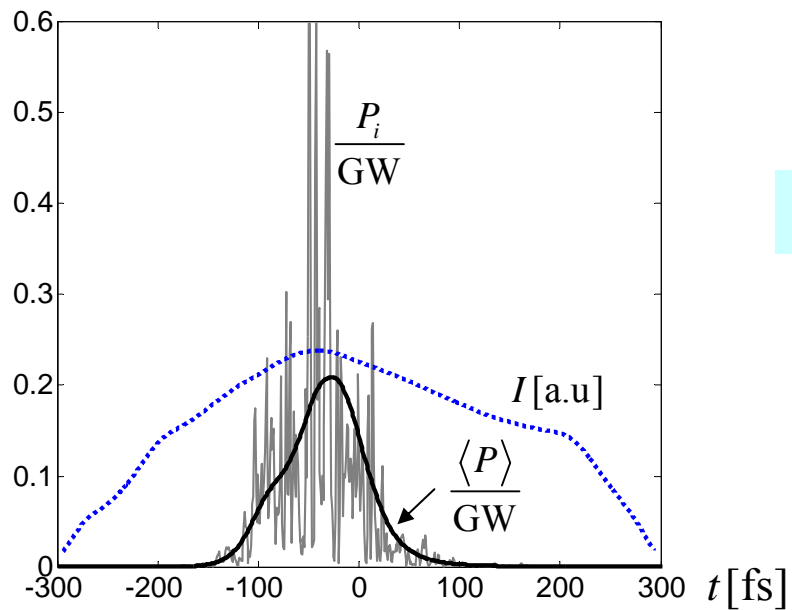
$z=20$ m



Q= 1 nC

Temporal structure

Q=0.02 nC



Summary

	with harmonic module					without*
Bunch charge, nC	1	0.5	0.25	0.1	0.02	0.5-1
Wavelength, nm	6.5					6
Beam energy, MeV	1000					1000
Peak current, kA	2.5			2.1	1-1.5	1.3-2.2
Slice emittance, mm-mrad	1-1.3	0.7-0.9	0.5-0.7	0.4-0.5	0.3-0.4	1.5-3.5
Slice energy spread, MeV	0.1-0.2	0.1-0.2	0.25	0.2-0.4	0.25	0.3
Saturation length, m	13	12	11	10	11	22-32
Energy in the rad. pulse, μ J	1000-1400	700	500	200	30	50-150
Radiation pulse duration FWHM, fs	70	30	17	7	2	15-50
Averaged peak power, GW	5-7					2-4
Spectrum width, %	0.4-0.6			0.8-1		0.4-0.6
Coherence time, fs	4-5			-	-	-

*) E.L.Saldin et al, Expected properties of the radiation from VUV-FEL at DESY, TESLA FEL 2004-06, 2004.

(1) Self consistent beam dynamics simulations

We are able to provide the well conditioned electron beam for different charges.

But RF tolerances for small charges are tough.

(2) FEL simulations

The charge tuning (20-1000 pC) in SASE mode allows to tune

- the radiation pulse energy (30-1400 mJ)
- the pulse width (FWHM 3-70 fs).